DESIGN OF HIGHWAY BRIDGE ABUTMENTS AND FOUNDATIONS

Project Manager: Juan Alcantar, P.E.

Submitted By:

Upul Attanayake, Ph.D., P.E. Presidential Innovation Professor Western Michigan University (269) 276-3217 upul.attanayake@wmich.edu

Yufeng Hu, Ph.D., P.E. Master Faculty Specialist Western Michigan University (269) 276-3310 yufeng.hu@wmich.edu

Western Michigan University

Department of Civil & Construction Engineering College of Engineering and Applied Sciences Kalamazoo, MI 49008-5316

May 10, 2023

DISCLAIMER

This publication is disseminated in the interest of information exchange. The Michigan Department of Transportation (hereinafter referred to as MDOT) expressly disclaims any liability, of any kind, or for any reason, that might otherwise arise out of any use of this publication or the information or data provided in the publication. MDOT further disclaims any responsibility for typographical errors or accuracy of the information provided or contained within this information. MDOT makes no warranties or representations whatsoever regarding the quality, content, completeness, suitability, adequacy, sequence, accuracy, or timeliness of the information and data provided, or that the contents represent standards, specifications, or regulations.

ACKNOWLEDGEMENTS

This project is funded by the Michigan Department of Transportation. It is carried out by the Michigan Department of Transportation Center of Excellence for Structural Durability at Western Michigan University. We, the authors, would like to acknowledge Mr. Juan Alcantar as the project manager and the advisory panel members for their assistance in finding relevant information, reviewing the drafts, and responding to our questions in a timely manner to successfully complete this example. We appreciate the contribution of Ms. Kanchani Basnayake and Mr. Harsha Amunugama for the development of this example.

Table of Contents

Section 1 Design Criteria

Section 2 Abutment with Spread Footing

Step 2.1 Preliminary Abutment Dimensions

Step 2.2 Application of Dead Load

Step 2.3 Application of Live Load

Step 2.4 Application of Other Loads

Step 2.5 Combined Load Effects

Step 2.6 Geotechnical Design of the Footing

Step 2.7 Backwall Design

Step 2.8 Abutment Wall Design

Step 2.9 Structural Design of the Footing

Appendix 2.A Braking Force and Wind Load Calculation

Appendix 2.B Sliding Resistance Check for Spread Footings on Clay

Section 3 Abutment with Spread Footing and EPS Backfill

Step 3.1 Preliminary Abutment Dimensions

Step 3.2 Application of Dead Load

Step 3.3 Application of Live Load

Step 3.4 Application of Other Loads

Step 3.5 Combined Load Effects

Step 3.6 Geotechnical Design of the Footing

Step 3.7 Backwall Design

Step 3.8 Abutment Wall Design

Step 3.9 Structural Design of the Footing

Section 4 Abutment with Piles

Step 4.1 Preliminary Abutment Dimensions

Step 4.2 Application of Dead Load

Step 4.3 Application of Live Load

Step 4.4 Application of Other Loads

Step 4.5 Combined Load Effects

Step 4.6 Pile Size and Layout Design

Step 4.7 Pile Capacity Check

Step 4.8 Backwall Design

Step 4.9 Abutment Wall Design

Step 4.10 Structural Design of the Footing

Appendix 4.A Tremie Seal Design

Section 1 Design Criteria

Description

This example illustrates the design of an abutment with shallow and deep (pile) foundations for an interstate freeway bridge. The design is implemented in accordance with the Michigan Department of Transportation

(MDOT) policies published as of 09/30/2022. The requirements of the 9th Edition of the AASHTO LRFD Bridge Design Specification; as modified and supplemented by the Bridge Design Manual (BDM), Bridge Design Guides (BDG), and 2020 Standard Specifications for Construction (SSFC); are followed. Certain material and design parameters are selected to be in compliance with MDOT practice reflected in the Bridge Design System (BDS), the MDOT legacy software.

This step provides the design criteria, the bridge information, material properties, soil types and properties, along with loads from the superstructure analysis.

Bridge Information

This is a zero-skew, 200-ft long, two-span continuous, interstate freeway bridge. Each span consists of seven steel plate girders spaced at 9 ft - $8\frac{5}{8}$ in. on center. The vertical profile and typical cross-section of the bridge are shown below. The girders are designed for composite behavior with a 9-in. thick cast-in-place reinforced concrete deck to resist superimposed dead, live, and impact loads. The superstructure design is presented in the *Two-Span Continuous Bridge Steel Plate Girder Design Example* developed by Attanayake et al. (2021), which is cited in this example as the *Steel Plate Girder Design Example*.

Vertical Profile

Typical Cross-Section

Bridge design span length $L_{\text{span}} = 100 \text{ ft}$ Number of beams $N_{\text{beams}} = 7$ Beam spacing BeamSpacing $\text{Beam} = 9\text{ft} + 8.625\text{in} = 9.72\text{ ft}$ Out-to-out deck width $W_{deck} = 63.75 \text{ ft}$ Roadway clear width $Rdwy_{width} = 60.5 \cdot ft$ Number of design traffic lanes per roadway $N_{lanes} := floor$ Rdwywidth $12 \cdot ft$ ſ L \setminus \setminus $t = \text{floor}\left(\frac{3 \text{ Wldiff}}{12 \cdot \text{ft}}\right) = 5$ **LRFD 3.6.1.1.1** Deck slab thickness $t_{\text{Deck}} \coloneqq 9$ in **BDM 7.02.08**

Note: The type of barrier used in this example is for illustrative purposes only. It is the section used in the *Steel Plate Girder Design Example* to provide superstructure loads for this design. The BDG provides standard barrier section details.

Reinforcing Steel Concrete Cover Requirements BDG 5.16.01, 5.18.01, 5.22.01 The minimum concrete cover 4 in. for the top and bottom of footing 3 in. for walls against soil Backwall back cover Cover_{bw} $= 3$ in Abutment wall cover Coverwall $\text{Cover}_{\text{wall}} := 3\text{in}$

Footing top and bottom cover Cover_{ft} := 4in

Soil Types and Properties

Bridge designers must interact closely with the Geotechnical Services Section since site conditions may make each substructure design unique.

Soil boring results showed the following soil profile. The Geotechnical Services Section uses this information to determine applicable bearing capacity, settlement, sliding resistance, etc.

The groundwater table is not located within the vicinity of the foundation.

Unit weight of backfill soil **Compacted Sand,** $\gamma_s := 0.12 \text{kef}$ **Compacted Sand,**

The active lateral earth pressure coefficient $k_a = 0.3$

LRFD Table 3.5.1-1

Loads from Superstructure

Dead Load

The superstructure dead load reactions at each girder end are taken from the *Steel Plate Girder Design Example*.

Live Load

MDOT uses a modified version of the HL-93 loading specified in the LRFD Specifications. A single design truck load, a single 60-kip load (axle load), a two design truck load for continuous spans, and a design lane load are multiplied by a factor of 1.2 to designate the design loading as HL-93 Mod.

According to the calculation presented in the *Steel Plate Girder Design Example,* the truck + lane load combination resulted in the maximum and minimum girder end reactions over the abutment. The unfactored girder support reactions for a single lane loaded case are listed below.

Maximum and minimum girder reactions due to truck load:

 $V_{\text{TruckMax}} = 63.9 \text{kip}$ $V_{\text{TruckMin}} = -5.9 \text{kip}$ Table A-4 of the Steel Plate Girder Design Example

Maximum and minimum girder reactions due to lane load:

 $V_{\text{LaneMax}} = 28.1 \text{kip}$ $V_{\text{LaneMin}} = -3.5 \text{kip}$ Table A-4 of the Steel Plate Girder Design Example

Section 2 Design of Abutment with a Spread Footing

Step 2.1 Preliminary Abutment Dimensions

Description

This step presents the selected preliminary abutment dimensions.

The minimum footing width for cantilever abutments is 6 ft.

The designers select the preliminary dimensions based on state-specific standards and past experience. The preliminary footing dimensions are selected such that the resultant of the vertical loads falls within the middle one-third. As needed, the guidelines shown in the following figure can be used to establish the initial dimensions that correlate with the minimum requirements in the BDM.

The following figure shows the selected abutment geometry and dimensional variables:

The preliminary dimensions selected for this example are given below.

This abutment includes an independent cantilevered backwall, similar to the one shown in BDG 6.20.03A.

The thickness of an abutment wall is controlled by several factors including the space required to fit bearings and anchor bolts with an adequate edge distance. Since the bearing pad design is not included in this example, a 3ft-2in. thick abutment wall is selected by referring to a similar bridge to provide an adequate space to accommodate bearings and edge distances.

. Passive earth pressure is excluded from the footing design.

BDM 7.03.02 F

Step 2.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$
DC_{Sup} := \frac{2 \cdot R_{DCEx} + (N_{beams} - 2) \cdot R_{DCln}}{L_{abut}} = 5.66 \cdot \frac{kip}{ft}
$$

\n
$$
DW_{Sup} := \frac{2 \cdot R_{DWEx} + (N_{beams} - 2) \cdot R_{DWIn}}{L_{abut}} = 0.89 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{backwall} := h_{backwall} \cdot t_{backwall} \cdot W_c = 0.96 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{wall} := h_{wall} \cdot t_{wall} \cdot W_c = 8.33 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{foothing} := B_{foothing} \cdot t_{fording} \cdot W_c = 7.65 \cdot \frac{kip}{ft}
$$

Step 2.3 Application of Live Load

Description

This step describes the application of live load on the abutment.

Page Content

- **17 Live Load on the Backwall**
- **17 Live Load on the Abutment Wall**
- **18 Live Load on the Footing**

Live Load on the Backwall

The live load on the bridge has no impact on the backwall.

The live load on the approach slab is represented by a live load surcharge. The live load surcharge results in a lateral load on the backwall. Please refer to Step 2.4 for further details.

Live Load on the Abutment Wall

Depending on the number of design lanes, a multiple presence factor is applied to the HL-93 truck and lane loads.

```
MPF(lanes) := 1.2 if lanes = 1
                1.0 if lanes = 20.85 if lanes = 30.65 otherwise
                                    LRFD Table 3.6.1.1.2-1
```
Live Load on Bridge Superstructure

The total of live load girder end reactions is divided by the abutment length to calculate the load on a per-foot basis.

Note: Even though the LRFD specifications recommend including the dynamic impact in the design of substructures that are not completely buried, the MDOT practice is to exclude them from the design of bridge abutments.

lanes := 1

\n
$$
R_{LLWall1} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{abut}} = 2.08 \cdot \frac{\text{kip}}{\text{ft}}
$$
\nlanes := 2

\n
$$
R_{LLWall2} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{abut}} = 3.46 \cdot \frac{\text{kip}}{\text{ft}}
$$
\nlanes := 3

\n
$$
R_{LLWall3} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{abut}} = 4.42 \cdot \frac{\text{kip}}{\text{ft}}
$$
\nlanes := 4

\n
$$
R_{LLWall4} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{abut}} = 4.5 \cdot \frac{\text{kip}}{\text{ft}}
$$
\nlanes := 5

\n
$$
R_{LLWall5} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{abut}} = 5.63 \cdot \frac{\text{kip}}{\text{ft}}
$$

The controlling live load on the abutment wall is

$$
R_{LLWallMax} := max \Big(R_{LLWall1}, R_{LLWall2}, R_{LLWall3}, R_{LLWall4}, R_{LLWall5}\Big) = 5.63 \cdot \frac{kip}{ft}
$$

Live Load on Bridge Approach

The live load on the approach is represented by a surcharge load. This surcharge results in a lateral load on the abutment wall. Please refer to Step 2.4 for further details.

Live Load on the Footing

Live Load on Bridge Superstructure

The total of live load girder reactions is divided by the footing length to calculate the load on a per-foot basis. The dynamic impact is not included in the design of foundations. **LRFD 3.6.2.1**

lanes := 1

\n
$$
R_{LLFooting1} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{footing}} = 2.01 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{lanes := 2}
$$
\n
$$
R_{LLFooting2} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{footing}} = 3.36 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{lanes := 3}
$$
\n
$$
R_{LLFooting3} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{footing}} = 4.28 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{lanes := 4}
$$
\n
$$
R_{LLFooting4} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{footing}} = 4.37 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{lanes := 5}
$$
\n
$$
R_{LLFooting5} := \frac{\text{lanes} \cdot (V_{TruckMax} + V_{LaneMax}) \cdot f_{HL93Mod} \cdot \text{MPF} \cdot (\text{lanes})}{L_{footing}} = 5.46 \cdot \frac{\text{kip}}{\text{ft}}
$$

The controlling live load on the footing is

$$
R_{LLFoothingMax}\coloneqq max\Big(R_{LLFoothing1}\,,\,R_{LLFoothing2}\,,\,R_{LLFoothing3}\,,\,R_{LLFoothing4}\,,\,R_{LLFoothing5}\Big)=5.46\cdot\frac{kip}{ft}
$$

Live Load on Bridge Approach

Live load on the approach is represented by a surcharge load. Please refer to Step 2.4 for further details.

Step 2.4 Application of Other Loads

Description

This step describes the application of braking force, wind load, earth load, and temperature load.

 21 Temperature Load

Braking Force

Since the abutment in this example has expansion bearings, the fixed bearings located at the pier resist the horizontal component of the braking force. Therefore, a horizontal braking force is not applied at the abutment. The braking force calculation is presented in Appendix 2.A and the pier design example.

Note: Although there is a possibility to develop a vertical force component at the bearings due to the braking force applied at 6 ft above the bridge deck, MDOT practice is to exclude this load from substructure design.

Wind Load

Since the abutment has expansion bearings, the fixed bearings located at the pier resist the longitudinal component of the wind load on the superstructure. The relevant calculations are presented in the pier design example.

Note: Although the transverse component of the wind load acts on the abutment, it is often small and does not impact the design. The MDOT practice is to exclude this load from the abutment design. The wind load calculation is described in the pier design example.

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. Hydrostatic pressure should be avoided if possible in all abutment and retaining wall design cases through the design of an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral pressure and the resultant load are calculated. This load acts at a distance of one third the height from the base of the components being investigated.

Backwall

kip
ft

Live Load Surcharge

Live load surcharge is applied to account for a vehicular load acting on the backfill surface within a distance equal to one-half the wall height behind the back face of the wall. **LRFD 3.11.6.4**

Height of the abutment $h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} = 24.79 \text{ ft}$

Note: The equivalent height of soil for the surcharge load is defined as a function of the abutment height.

Temperature Load

The forces transferred from the superstructure to the substructure due to temperature are influenced by the shear stiffness of the bearing pads.

Thermal expansion coefficient of steel $(^{\circ}F)$

 $\alpha := 6.5 \cdot 10^{-6}$

Note: MDOT uses a 45° F drop and 35° F rise from the temperature at the time of construction.

BDM 7.01.07 cold climate temperature range

Since the pier bearings are fixed, the total superstructure deformation is imposed on the abutment bearings.

The force acting on a bearing due to superstructure contraction

$$
H_{buContr} := \frac{G_{\text{bearing}} \cdot A_{\text{bearing}} \cdot \Delta_{\text{TContr}}}{h_{rt}} = 2.53 \cdot \text{kip} \qquad \frac{\text{LRFD Eq.}}{14.6.3.1-2}
$$

Total force acting on the abutment due to superstructure contraction

The force acting on a bearing due to superstructure expansion

Total force acting on the abutment due to superstructure expansion

$$
TU_{\text{Contr}} := \frac{N_{\text{beams}} \cdot H_{\text{buContr}}}{L_{\text{abut}}} = 0.28 \cdot \frac{kip}{ft}
$$

$$
H_{b u Exp} := \frac{G_{\text{bearing}} \cdot A_{\text{bearing}} \cdot \Delta_{\text{TExp}}}{h_{\text{rt}}} = 1.97 \cdot \text{kip} \qquad \begin{array}{c} \text{LRFD Eq.} \\ 14.6.3.1-2 \end{array}
$$

$$
TU_{Exp} := \frac{N_{beams} \cdot H_{bulExp}}{L_{abut}} = 0.22 \cdot \frac{kip}{ft}
$$

N_{beams} H_{buContr}

Step 2.5 Combined Load Effects

Description

This step presents the procedure for combining all load effects and calculates total factored forces and moments acting at the base of the backwall, abutment wall, and footing.

Page Contents

- **25 Forces and Moments at the Base of the Backwall**
- **27 Forces and Moments at the Base of the Abutment Wall**
- **31 Forces and Moments at the Base of the Footing**

Strength I, Strength III, Strength V, and Service I limit states are considered for the analysis and design of an abutment.

LRFD 3.4.1

Strength $I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU$

Strength III = $1.25DC + 1.5DW + 1.5EH + 1.35EV + 1.0WS + 0.5TU$

Strength V = $1.25DC + 1.5DW + 1.35LL + 1.35BR + 1.0WS + 1.0WL + 1.5EH + 1.35EV + 1.35LS + 0.5TU$

Service $I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU$

- $BR =$ vehicular braking force
- $DC = dead$ load of structural components and nonstructural attachments
- $DW =$ dead load of future wearing surface and utilities
- $EH = horizontal$ earth pressure load
- $EV = vertical pressure from the earth fill$
- LL $=$ vehicular live load
 $I.S =$ live load surcharge
- $=$ live load surcharge
- $WL = wind on$ live load
- $WS = wind load on structure$
- $TU =$ force effect due to uniform temperature

Limit states that are not shown either do not control or are not applicable. Generally, Strength III or Strength V may control the design of abutments with fixed bearings when the wind load is considered.

Note: These load combinations should include the maximum and minimum load factors; only the maximum factors are shown for clarity.

Since the MDOT practice is to exclude wind load from the abutments design, only Strength I and Service I limit states are included in this section.

Four load cases are considered in the design of an abutment: **BDM 7.03.01**

Case II Bridge open to traffic with traffic loading on the approach only.

Case III Bridge with traffic on it and no load on the approach.

Case I Construction state: abutment built and backfilled to grade.

 Case IV Contraction: Loading forces of Case II plus the effects of temperature contraction in the deck transmitted to the abutment.

Since Case IV always governs over Case II for the bridge abutment selected for this example (independent cantilever abutment), only Cases I, III, and IV are considered.

The temperature force in Load Case IV is due to contraction; therefore

$$
TU := TU_{Contr} = 0.28 \cdot \frac{\text{kip}}{\text{ft}}
$$

The base of the backwall, the base of the abutment wall, and the base of the footing are the three critical locations where the force effects need to be combined and analyzed for the design of an abutment. Horizontal loads parallel to the longitudinal axis of the abutment are not considered for backwall and abutment wall design because of the high moment of inertia about the longitudinal axis of the bridge. However, such loads, even though relatively small, are considered at the base of the footing.

Strength I

Strength I = $1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU$

Load Case I

Factored vertical force $F_{VBWLClStrI} = 1.25 \cdot DC_{backwall} = 1.2 \cdot \frac{kip}{ft}$ $:= 1.25 \cdot DC_{\text{backwall}} = 1.2 \cdot$ Factored shear force parallel to the Factored shear force parallel to the
transverse axis of the backwall $V_{\text{uBwLC1StrI}} = 1.5 \cdot P_{\text{EHBackwall}} = 0.49 \cdot \frac{\text{kip}}{\text{ft}}$ $:= 1.5 \cdot P_{\text{FHRackwall}} = 0.49$ $\cdot \frac{\text{h} \text{backward}}{3} = 0.69 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 $M_{\text{uBwLC1StrI}} \coloneqq 1.5 \cdot P_{\text{EHBackwall}}$

 $M_{\text{uBwLC3StrI}} \coloneqq 1.5 \cdot P_{\text{EHBackwall}}$

 $= 1.5 \cdot P_{\text{FHRackwall}} \cdot \frac{3.00 \times 10^{10}}{2} = 0.69$

 $= 1.5 \cdot P_{\text{FHRackwall}} \cdot \frac{3.00 \times 10^{10}}{2} = 0.69$

 $V_{\text{uBwLC4StrI}}$:= 1.5 P_{EHBackwall} + 1.75 P_{LSBackwall} = 1.02 $\frac{\text{kip}}{\text{ft}}$

 $:= 1.5 \cdot P_{\text{FHRackwall}} + 1.75 \cdot P_{\text{I SRackwall}} = 1.02 \cdot$

 $\cdot \frac{\text{h} \text{backward}}{3} = 0.69 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 $:= 1.5 \cdot P_{\text{FHRackwall}} = 0.49$

Factored moment about the longitudinal axis of the backwall

Load Case III

Fortune Execution Force

Fortune Force Figure 1.25 DC_{backwall} = 1.2. $\frac{kip}{ft}$

Factored shear force parallel to the transverse axis of the backwall Factored shear force parallel to the
transverse axis of the backwall $V_{\text{uBwLC3StrI}} = 1.5 \cdot P_{\text{EHBackwall}} = 0.49 \cdot \frac{\text{kip}}{\text{ft}}$

Factored moment about the longitudinal axis of the backwall

Load Case IV

Fortune Execution Force

Fortune Force Force For Figure 1.25 DC_{backwall} = 1.2 kip

Factored shear force parallel to the transverse axis of the backwall

Factored moment about the longitudinal axis of the backwall

$$
M_{uBwLC4StrI} := 1.5 \cdot P_{EHBackwall} \cdot \frac{h_{backwall}}{3} + 1.75 \cdot P_{LSBackwall} \cdot \frac{h_{backwall}}{2} = 1.83 \cdot \frac{kip \cdot ft}{ft}
$$

Service I

Service $I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU$

Since Load Case IV controls the Service I limit state, related calculations are shown below.

Factored vertical force $F_{\text{VBackwallSerI}} \coloneqq DC_{\text{backwall}} = 0.96 \cdot \frac{\text{kip}}{\text{ft}}$ $\mu = DC_{\text{backwall}} = 0.96$

Factored shear force parallel to the transverse axis of the backwall

$$
V_{uBackwallSerI} := P_{EHBackwall} + P_{LSBackwall} = 0.63 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the backwall

$$
M_{uBackwallSerI} := P_{EHBackwall} \cdot \frac{h_{backwall}}{3} + P_{LSBackwall} \cdot \frac{h_{backwall}}{2}
$$

$$
M_{uBackwallSerI} = 1.11 \cdot \frac{kip \cdot ft}{ft}
$$

Summary of Forces and Moments at the Base of the Backwall

Factored shear force parallel to the Factored vertical force, F_{VBw} (kip/ft)
transverse axis of the backwall, V_{uBw} (kip/ft)

Factored moment about the longitudinal axis of the backwall, $\rm M_{uBw}$ (kip[.]ft/ft)

Forces and Moments at the Base of the Abutment Wall

Load Cases I, III, and IV are considered below. The superstructure dead and live loads and the uniform temperature induced loads are considered in addition to the backwall and abutment wall dead loads, lateral earth pressure, and lateral surcharge pressure.

Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU

Load Case I

Factored shear force parallel to the transverse axis of the abutment wall

Factored vertical force
\n
$$
F_{VWallLC1StrI} := 1.25 \cdot (DC_{backwall} + DC_{wall}) = 11.61 \cdot \frac{kip}{ft}
$$
\n
$$
V_{uWallLC1StrI} := 1.5 \cdot P_{EHWall} = 12.82 \cdot \frac{kip}{ft}
$$
\n
$$
V_{uWallLC1StrI} := 1.5 \cdot P_{EHWall} = 12.82 \cdot \frac{kip}{ft}
$$

The backwall weight reduces the critical moment at the base of the abutment wall. This requires using the minimum load factor of 0.9 for the dead load (DC) instead of the factor 1.25 in the Strength I combination.

LRFD 3.4.1 LFRD Table 3.4.1-2

Similar conditions are applied for the moments calculated about the longitudinal axis of the abutment wall for all the load cases and all the limit states.

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC1StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + 1.5 \cdot P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3} = 92.4 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force

$$
F_{VWallLC3StrI} := 1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} \right) + 1.5DW_{Sup} + 1.75R_{LLWallMax}
$$

$$
F_{VWallLC3StrI} = 29.86 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the abutment wall

$$
V_{\text{uWallLC3StrI}} := 1.5 \cdot P_{\text{EHWall}} = 12.82 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC3StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} ...
$$

$$
+ (1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLWallMax}) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) ...
$$

$$
+ 1.5 \cdot P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3}
$$

$$
M_{uWallLC3StrI} = 106.09 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force
$$
F_{VWallLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall}) + 1.5DW_{Sup} = 20.01 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the abundant wall $V_{uWallLC4StrI} := 1.5 \cdot P_{EHWall} + 1.75 \cdot P_{LSWall} + 0.5TU = 15.7 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC4StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} \dots
$$

+ $(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup}) \cdot (t_{brtowall} - \frac{t_{wall}}{2}) \dots$
+ $1.5 \cdot P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3} + 1.75 \cdot P_{LSWall} \cdot \frac{(h_{backwall} + h_{wall})}{2} + 0.5 \cdot TU \cdot h_{wall}$
 $M_{uWallLC4StrI} = 131.04 \cdot \frac{kip \cdot ft}{ft}$

Service I

Service $I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU$

Load Case I

Factored vertical force $F_{\text{VWallLC1SerI}} := DC_{\text{backwall}} + DC_{\text{wall}} = 9.29 \cdot \frac{\text{kip}}{\text{ft}}$ $\mu = DC_{\text{backwall}} + DC_{\text{wall}} = 9.29$ Factored shear force parallel to the
transverse axis of the abutment wall Factored shear force parallel to the
transverse axis of the abutment wall $V_{\text{uWallLC1SerI}} = P_{\text{EHWall}} = 8.55 \cdot \frac{\text{kip}}{\text{ft}}$ $=$ P_{FHWall} = 8.55.

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC1SerI} := DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3}
$$

$$
M_{uWallLC1SerI} = 61.28 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force

$$
F_{\text{VWallLC3SerI}} := \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} \right) + \text{DW}_{\text{Sup}} + R_{\text{LLWallMax}} = 21.46 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the abutment wall

$$
V_{\text{uWallLC3SerI}} := P_{\text{EHWall}} = 8.55 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC3SerI} := DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} ... + (DC_{Sup} + DW_{Sup} + R_{LLWallMax}) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2} \right) ... + P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3} M_{uWallLC3SerI} = 70.41 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force
\n
$$
F_{VWallLC4SerI} := (DC_{Sup} + DC_{backwall} + DC_{wall}) + DW_{Sup}
$$
\n
$$
F_{VWallLC4SerI} = 15.83 \cdot \frac{kip}{ft}
$$
\n
$$
V_{uWallLC4SerI} := P_{EHWall} + P_{LSWall} + TU = 10.39 \cdot \frac{kip}{ft}
$$

Factored shear for transverse axis of the abutment wall

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC4SerI} := DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} ... + (DC_{Sup} + DW_{Sup}) \cdot (l_{brtowall} - \frac{t_{wall}}{2}) ... + P_{EHWall} \cdot \frac{(h_{backwall} + h_{wall})}{3} + P_{LSWall} \cdot \frac{(h_{backwall} + h_{wall})}{2} + TU \cdot h_{wall} M_{uWallLC4SerI} = 88.15 \cdot \frac{kip \cdot ft}{ft}
$$

Summary of Forces and Moments at the Base of the Abutment Wall

Factored vertical force, F_{VWall} (kip/ft)

Factored moment about the longitudinal axis of the abutment wall, M_{u Wall (kip[.]ft/ft)

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered below. In addition to all the loads considered for the abutment wall, weight of soil (i.e. the earth load on the footing toe and heel) and live load on the backwall are considered.

The dynamic load allowance is excluded from the live load for foundation components that are entirely below ground level.

LRFD 3.6.2.1

Strength I

Strength $I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU$

Load Case I

Factored vertical force

 $F_{\text{VFLC1StrI}} \coloneqq 1.25 \cdot \left(\text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{footing}} \right) + 1.35 \cdot \left(\text{EV}_{\text{earthBk}} + \text{EV}_{\text{earthFt}} \right) = 56.79 \cdot \frac{\text{kip}}{\text{ft}}$ $= 1.25 \cdot (DC_{\text{backwall}} + DC_{\text{wall}} + DC_{\text{foothing}}) + 1.35 \cdot (EV_{\text{earthRk}} + EV_{\text{earthFt}}) = 56.79 \cdot$

 $:= 1.5 \cdot P_{\text{FHEooting}} = 16.59$

Factored shear force parallel to the Factored shear force parallel to the
transverse axis of the footing $V_{\text{uFtLC1StrI}} \coloneqq 1.5 \cdot P_{\text{EHFooting}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}$

The backfill soil weight reduces the critical moment at the base of the footing. This requires using the minimum load factor of 1.0 for the vertical earth load (EV) instead of the factor 1.35 in the Strength I combination. Similar conditions are applied for the moments calculated about the longitudinal axis of the footing for all the load cases.

LRFD 3.4.1 LFRD Table 3.4.1-2

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLCIStrI}} \coloneqq 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backward}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} + 1.35EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{to}}}{2} \right) \dots + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right)
$$

$$
M_{\text{uFtLCIStrI}} = 87.92 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case III

Factored vertical force $F_{VFLC3StrI} = 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing}) + 1.5DW_{Sup}$... $+1.75R_{LLFoothingMax} + 1.35 (EV_{earthBk} + EV_{earthFt})$

$$
F_{VFLC3StrI} = 74.75 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the footing = 16.59. $\frac{kip}{ft}$

$$
V_{uFtLC3StrI} := 1.5 \cdot P_{EHFooting} = 16.59 \cdot \frac{kip}{ft}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3StrI}} \coloneqq 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(1.25 \cdot DC_{\text{Sup}} + 1.5 \cdot DW_{\text{Sup}} + 1.75 \cdot R_{\text{LLFootingMax}} \right) \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backward}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} \dots + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.35 \cdot EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right)
$$

$$
M_{\text{uFtLC3StrI}} = 143.27 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case IV

Factored vertical force

$$
F_{VFLLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing}) + 1.5DW_{Sup} ... + 1.35 \cdot (EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFoothing}
$$

$$
F_{VFLC4StrI} = 69.08 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the
transverse axis of the footing
$$
V_{\text{uFtLC4StrI}} := 1.5 \cdot P_{\text{EHFooting}} + 1.75 P_{\text{LSFooting}} + 0.5 \text{TU} = 19.85 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC4StrI}} \coloneqq 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(1.25 \cdot DC_{\text{Sup}} + 1.5 \cdot DW_{\text{Sup}} \right) \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \left(\frac{h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}}}{3} \right) + 1.75V_{\text{LSFooting}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.75 \cdot P_{\text{LSFooting}} \left(\frac{h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}}}{2} \right) + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{h_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.35 \cdot EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{1_{\text{toe}}}{2} \right) + 0.5 \cdot TU \cdot (h_{\text{wall}} + t_{\text{footing}}) + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{h_{\text{hel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(\frac{h_{\text{terth}}}{2} + 1.35 \cdot EV_{\text{earthFt}} \right) \left(\frac{B_{\text{footing}}}{2} - \frac{1_{\text{toe}}}{2} \right) + 0.5 \cdot TU \cdot (h_{\text{wall}} + t_{\text{footing}}) + \left(\frac{h_{\text{perth}}}{2} + \frac{1.35 \cdot EV_{\text{earthFt}}}{2} \right) \dots + \left(\frac{h_{\text{refth}}}{2} + \frac{B_{\text{footing}}}{2} \right) \dots + \left(\frac{h_{\text{refth}}}{2} + \frac
$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU Load Case I

Factored vertical force

$$
F_{VFLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 43.32 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the footing = V_{uFtLC1SerI} := P_{EHFooting} = 11.06 \cdot \frac{kip}{ft}

Factored moment about the longitudinal axis of the footing

$$
M_{uFtLC1SerI} := DC_{backwall} \cdot \left(I_{\text{heel}} + \frac{t_{backwall}}{2} - \frac{B_{\text{footing}}}{2} \right) + DC_{wall} \cdot \left(I_{\text{heel}} + \frac{t_{wall}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + P_{EHFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{\text{footing}} \right)}{3} \dots + EV_{earthBk} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right)
$$

$$
M_{uFtLC1SerI} = 32.22 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force

$$
F_{VFLC3SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFootingMax} ... + (EV_{earthFt} + EV_{earthBk})
$$

$$
F_{\text{VFtLC3SerI}} = 55.33 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the footing\n
$$
V_{\text{uFtLC3SerI}} := P_{\text{EHFooting}} = 11.06 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3SerI}} \coloneqq DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) + DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) \dots
$$

$$
+ \left(DC_{\text{Sup}} + DW_{\text{Sup}} + R_{\text{LLFootingMax}} \right) \left(l_{\text{heel}} + l_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots
$$

$$
+ P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} \dots
$$

$$
+ EV_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{to}}}{2} \right)
$$

$$
M_{\text{uFtLC3SerI}} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force
\n
$$
F_VFtLC4SerI := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing} + DW_{Sup} ...
$$
\n
$$
+ EV_{earthFt} + EV_{earthBk} + V_{LSFoothing}
$$
\n
$$
F_VFtLC4SerI = 52.09 \cdot \frac{kip}{ft}
$$
\nFactored shear force parallel to the
\ntransverse axis of the footing
\nFactored moment about the longitudinal axis of the footing
\n
$$
V_uFtLC4SerI := P_{EHFoothing} + P_{LSFoothing} + TU = 13.12 \cdot \frac{kip}{ft}
$$
\n
$$
F_{VFtLC4SerI} := P_{EHFoothing} + PU_{S} + TU = 13.12 \cdot \frac{kip}{ft}
$$
\n
$$
V_uFtLC4SerI := PC_{backwall} - \frac{V_uFtC4SerI}{2} - \frac{P_{foothing}}{2} + DC_{wall} \cdot \left(1_{heel} + \frac{V_{wall}}{2} - \frac{B_{foothing}}{2} \right) ...
$$

$$
M_{\text{uFtLC4SerI}} \coloneqq DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right)
$$
\n
$$
\left(DC_{\text{max}} - DU_{\text{total}} \right) \left(l_{\text{heat}} - \frac{B_{\text{footing}}}{2} \right)
$$

+
$$
(DC_{Sup} + DW_{Sup}) \cdot \left(I_{heel} + I_{brtowall} - \frac{B_{footing}}{2} \right) + P_{EHFooting} \cdot \frac{\left(h_{background} + h_{wall} + t_{footing} \right)}{3} \dots
$$

+ $EV_{earthBk} \cdot \left(\frac{I_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{I_{toe}}{2} \right) \dots$
+ $VL_{SFooting} \cdot \left(\frac{I_{heel}}{2} - \frac{B_{footing}}{2} \right) + P_{LSFooting} \cdot \frac{\left(h_{background} + h_{wall} + t_{footing} \right)}{2} \dots$
+ $TU \cdot \left(h_{wall} + t_{footing} \right)$
 $M_{uFtLC4SerI} = 71.62 \cdot \frac{kip \cdot ft}{ft}$

2

...

Summary of Forces and Moments at the Base of the Footing

Factored shear force parallel to the transverse Factored vertical force, F_{VFt} (kip/ft)
axis of the footing, V_{uFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Step 2.6 Geotechnical Design of the Footing

Description

This step presents the geotechnical design of a spread footing considering the following strength and serviceability limit states:

LRFD 10.6.1.1

- 1. bearing resistance strength limit state
- 2. settlement service limit state
- 3. sliding resistance strength limit state
- 4. load eccentricity (overturning) strength limit state.

Step 2.9 presents the evaluation of structural resistance of the footing (internal stability).

Page Contents

- **37 Bearing Resistance Check**
- **41 Settlement Check**
- **41 Sliding Resistance Check**
- **43 Eccentric Load Limitation (Overturning) Check**
Forces and Moments at the Base of the Footing

Step 2.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored shear force parallel to the transverse axis Factored vertical force, F_{VFt} (kip/ft) F_{VFt} of the footing, V_{VFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Bearing Resistance Check

For eccentrically loaded footings, the use of a reduced effective area is allowed for bearing resistance or settlement calculation. The point of load application shall be at the centroid of the reduced area.

Note: As a practice, the average pressure and the values at the toe and heel under different load cases and limit states are provided to the MDOT Geotechnical Services Section for verification.

This example presents the LRFD and MDOT methods.

Load Case I, Strength I

Factored moment about the longitudinal $M_{\text{uFtLC1StrI}} = 87.92 \cdot \frac{\text{kip·ft}}{\text{ft}}$

Factored vertical force
\nFactored moment about the longitudinal
\naxis of the footing
\nEccentricity in the footing width direction
\n
$$
\epsilon_{\text{B}} := \frac{M_{\text{uFtLC1StrI}}}{F_{\text{vFtLC1StrI}}} = 1.55 \text{ ft}
$$

Eccentricity in the footing width direction

LRFD Method

A reduced effective footing width is used for bearing resistance and settlement design. **LRFD 10.6.1.3**

Effective footing width B_{eff} = $B_{footing} - 2 \cdot e_B = 13.9 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure qbearing LC1 FVFtLC1StrI B_{eff} $=$ $\frac{4.08 \text{ kfs}}{2}$ = 4.08 ksf

LRFD 10.6.1.3

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case III, Strength I

Factored vertical force

Factored moment about the longitudinal $M_{\text{uFtLC3StrI}} = 143.27 \cdot \frac{\text{kip·ft}}{\text{ft}}$

Eccentricity in the footing width direction

LRFD Method

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case IV, Strength I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

$$
q_{avgLC1} := \frac{F_{VFLC1StrI}}{B_{footing}} = 3.34 \cdot \text{ksf}
$$
\n
$$
q_{toeLC1} := \frac{F_{VFLC1StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 5.17 \cdot \text{ksf}
$$
\n
$$
q_{heelLC1} := \frac{F_{VFLC1StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.52 \cdot \text{ksf}
$$

$$
F_{VFLLC3StrI} = 74.75 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC3StrI} = 143.27 \cdot \frac{kip}{ft}
$$

$$
e_B := \frac{M_{uFtLC3StrI}}{F_{VFtLC3StrI}} = 1.92 \text{ ft}
$$

Effective footing width B_{eff} = $B_{foothing} - 2 \cdot e_B = 13.17 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure qbearing LC3 FVFtLC3StrI B_{eff} $=$ $\frac{1.68656 \text{m}}{2}$ = 5.68 ksf

$$
q_{avgLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} = 4.4 \cdot ksf
$$

$$
q_{toeLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 7.37 \cdot ksf
$$

$$
q_{heelLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.42 \cdot ksf
$$

$$
F_{VFLC4StrI} = 69.08 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC4StrI} = 140.34 \cdot \frac{kip \cdot ft}{ft}
$$

$$
e_B := \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrI}} = 2.03 \text{ ft}
$$

LRFD Method

MDOT Method

Average bearing pressure quality of quality qu

Bearing pressure at the toe

Bearing pressure at the heel

Load Case I, Service I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

LRFD Method

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case III, Service I

Factored vertical force

Factored moment about the longitudinal $M_{\text{uFtLC3SerI}} = 69.22 \cdot \frac{\text{kip·ft}}{\text{ft}}$

Effective footing width B_{eff} = $B_{footing} - 2 \cdot e_B = 12.94 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure qbearing LC4 F_{VFtLC4StrI} B_{eff} $=$ $\frac{1.35 \times 10^{10}}{2} = 5.34$ ksf

$$
I_{avgLC4} := \frac{F_{VFtLC4StrI}}{B_{footing}} = 4.06 \text{ ksf}
$$

$$
q_{\text{toeLC4}} := \frac{\text{FvFtLc4StrI}}{\text{B}_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_B}{\text{B}_{\text{footing}}} \right) = 6.98 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC4}} := \frac{\text{FvFtLc4StrI}}{\text{B}_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_B}{\text{B}_{\text{footing}}} \right) = 1.15 \cdot \text{ksf}
$$

$$
F_{VFLC1SerI} = 43.32 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC1SerI} = 32.22 \cdot \frac{kip}{ft}
$$

$$
e_B := \frac{M_{uFtLC1SerI}}{F_{VFLC1SerI}} = 0.74 \text{ ft}
$$

Effective footing width

\n
$$
B_{eff} := B_{footing} - 2 \cdot e_B = 15.51 \text{ ft}
$$
\nLRFD Eq. 10.6.1.3-1

\nBearing pressure

\n
$$
q_{\text{bearing_LC1SerI}} := \frac{F_{\text{VFtLC1SerI}}}{B_{\text{eff}}} = 2.79 \cdot \text{ksf}
$$

$$
q_{avgLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}} = 2.55 \cdot \text{ksf}
$$
\n
$$
q_{toeLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.22 \cdot \text{ksf}
$$
\n
$$
q_{heelLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.88 \cdot \text{ksf}
$$

$$
F_{VFLC3SerI} = 55.33 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

Eccentricity in the footing width direction e_F

LRFD Method

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case IV, Service I

Factored vertical force

Factored moment about the longitudinal $M_{\text{uFtLC4SerI}} = 71.62 \cdot \frac{\text{kip·ft}}{\text{ft}}$

Eccentricity in the footing width direction

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

$$
B := \frac{M_{\text{uFtLC3SerI}}}{F_{\text{VFtLC3SerI}}} = 1.25 \text{ ft}
$$

Effective footing width $B_{eff} = B_{footing} - 2 \cdot e_B = 14.5 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure qbearing LC3SerI FVFtLC3SerI B_{eff} $\frac{3.82 \cdot \text{ksf}}{2} = 3.82 \cdot \text{ksf}$

$$
q_{avgLC3SerI} := \frac{F_{VFLC3SerI}}{B_{footing}} = 3.25 \text{ ksf}
$$

$$
q_{\text{toeLC3SerI}} := \frac{F_{\text{VFtLC3SerI}}}{B_{\text{footing}}}. \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 4.69 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC3SerI}} := \frac{F_{\text{VFtLC3SerI}}}{B_{\text{footing}}}. \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 1.82 \cdot \text{ksf}
$$

$$
F_{VFLC4SerI} = 52.09 \cdot \frac{kp}{ft}
$$

$$
M_{uFtLC4SerI} = 71.62 \cdot \frac{kip \cdot ft}{ft}
$$

$$
e_B := \frac{M_{uFtLC4SerI}}{F_{VFLC4SerI}} = 1.37 ft
$$

$$
B_{eff} := B_{footing} - 2 \cdot e_B = 14.25 \text{ ft}
$$
 LRFD Eq. 10.6.1.3-1

$$
q_{\text{bearing_LC4SerI}} := \frac{F_{\text{VFLC4SerI}}}{B_{\text{eff}}} = 3.66 \cdot \text{ksf}
$$

$$
q_{avgLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} = 3.06 \cdot \text{ksf}
$$
\n
$$
q_{toLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.55 \cdot \text{ksf}
$$
\n
$$
q_{heelLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.58 \cdot \text{ksf}
$$

Summary

LRFD Method

The controlling bearing pressure under strength limit states

 $q_b := max (q_{\text{learning}} \text{ LC1}$, $q_{\text{learning}} \text{ LC3}$, $q_{\text{bearing}} \text{ LC4}) = 5.68$ ksf

The controlling bearing pressure needs to be checked with the factored bearing resistance of the soil provided by the Geotechnical Services Section.

MDOT Method

A summary of bearing pressure values (in psf) is shown in the following table:

The Geotechnical Services Section uses these values for the verification of bearing resistance and settlement limits. If the bearing pressure exceeds the bearing strength of the soil, the size of the footing needs to be increased.

BDM 7.03.02G

Settlement Check

The Geotechnical Services Section uses the controlling bearing pressure from the service limit state to check if the total settlement of foundation is less than 1.5 in., the allowable limit.

BDM 7.03.02G 2b

LRFD 10.6.3.4

For the LRFD method, the controlling bearing pressure for settlement analysis is

 q_b settlement = max $(q_{\text{bearing LC1SerI}}$, $q_{\text{bearing LC3SerI}}$, $q_{\text{bearing LC4SerI}}$ = 3.82 ksf

The Geotechnical Services Section uses this controlling bearing pressure to calculate the foundation total settlement.

For the MDOT method, the bearing pressures under service limit state are provided to the Geotechnical Services Section to calculate the settlement.

Note: Besides the total settlement, considerations should be given to prevent the differential settlement between the abutments and pier from exceeding the tolerable differential settlement limit. Differential settlement limits are given in the *Steel Plate Girder Design Example.*

Sliding Resistance Check

Spread footings must be designed to resist lateral loads without sliding. The sliding resistance of a footing on cohesionless soil is a function of the normal force and the interface friction between the foundation and the soil.

The Geotechnical Services Section should provide a coefficient of sliding resistance (μ) for a design. MDOT typically uses a sliding resistance coefficient of 0.5 for cast-in-place concrete footings. Consult the Geotechnical Services Section to identify the most suitable coefficient for a specific design.

Coefficient of sliding resistance $\mu = 0.5$

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used:

- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Load Case I

Factored shear force parallel to the Factored shear force parallel to the

transverse axis of the footing $V_{\text{uFtLC1StrI}} = 16.59 \cdot \frac{kip}{ft}$

 $V_{\text{uFtI}} \text{C1StrI} = 16.59$

 ϕ_{τ} : μ · F_{VFtI} $C1$ StrIMin = 16.65·

Factored sliding force $V_{\text{sliding}} = V_{\text{uFtLC1StrI}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}$

Minimum vertical load

$$
F_{VFLC1StrIMin} = 0.9 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 41.63 \cdot \frac{kip}{ft}
$$

Resistance factor for sliding ϕ_{τ} = 0.8 **BDM 7.03.02.F, LRFD Table 10.5.5.5.2-1**

Sliding resistance
 $V_{\text{resistance}} = \phi_{\text{T}} \cdot \mu \cdot F_{\text{VFtLC1StrIMin}} = 16.65 \cdot \frac{\text{kip}}{\text{ft}}$

Check if $V_{\text{resistance}} > V_{\text{sliding}}$ Check $V_{\text{resistance}} > V_{\text{sliding}}$, "OK", "Not OK" $) = "OK"$

Load Case III

Factored shear force parallel to the Factored shear force parallel to the

transverse axis of the footing $V_{\text{uFtLC3StrI}} = 16.59 \cdot \frac{kip}{ft}$ Factored sliding force $V_{\text{sliding}} = V_{\text{uFtLC3StrI}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}$ V_{uFtI} $C3\text{StrI} = 16.59$

When calculating the minimum vertical force for sliding and checking eccentric load limitation, the live load on the superstructure is excluded to develop a conservative design.

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Factored sliding force without the live Factored sliding force without the live
 $V_{\text{sliding}} = V_{\text{uFtLC4StrI}} - 1.75P_{\text{LSFooting}} = 16.73 \cdot \frac{\text{kip}}{\text{ft}}$ $V_{\text{uFtI C4StrI}} - 1.75 P_{\text{I SEooting}} = 16.73$ Minimum vertical load without the live load surcharge $F_{\text{VFtLC4StrIMin} \text{ } n0\text{LS}} \coloneqq 0.9 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{foothing}} \right) ...$ $+1.0\cdot (EV_{earthBk} + EV_{earthFt})$ F_V FtLC4StrIMin_noLS = 46.72 $\cdot \frac{kip}{ft}$ Sliding resistance

V_{resistance} ϕ_{τ} + μ F_{VFtLC4StrIMin_noLS} = 18.69 $\frac{kip}{ft}$ ϕ_{τ} : μ · F_{VFtI} $C4$ StrIMin noI S = 18.69· Check if $V_{\text{resistance}} > V_{\text{sliding}}$ Check $V_{\text{resistance}} > V_{\text{sliding}}$, "OK", "Not OK" $) = "OK"$ *With the live load surcharge:* Factored shear force parallel to the Factored shear force parallel to the
transverse axis of the footing $V_{\text{uFtLC4StrI}} = 19.85 \cdot \frac{\text{kip}}{\text{ft}}$ Factored sliding force $V_{\text{sliding}} = V_{\text{uFtLC4StrI}} = 19.85 \cdot \frac{\text{kip}}{\text{ft}}$ $V_{\text{uFtI C4StrI}} = 19.85$ Minimum vertical load with the live load surcharge $F_{\text{VFtLC4StrIMin}} \coloneqq 0.9 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{foothing}} \right) ...$ $+1.0 \cdot (EV_{earthBk} + EV_{earthFt}) + 1.75V_{LSFooting}$ $F_{VFLC4StrIMin} = 50.61 \cdot \frac{kip}{ft}$ Sliding resistance

V_{resistance} $= \phi_{\tau} \cdot \mu \cdot F_{VFLC4StrIMin} = 20.24 \cdot \frac{kip}{ft}$ $= \phi_{\tau} \cdot \mu \cdot F_{\text{VF1}}$ $C4\text{StrMin} = 20.24 \cdot$ Check if $V_{\text{resistance}} > V_{\text{sliding}}$ Check $V_{\text{resistance}} > V_{\text{sliding}}$, "OK", "Not OK" $) = "OK"$

Eccentric Load Limitation (Overturning) Check

The eccentricity of loading at the strength limit state, evaluated based on factored loads, shall not exceed one-sixth of the corresponding dimension measured from the centerline of the footing for stability. **LRFD 10.6.3.3**

The eccentricity in the abutment length direction is not a concern. The following calculations present the evaluation of the eccentricity in the abutment width direction for the Strength I limit state:

Load Case I

Minimum vertical force

Moment about the longitudinal axis of the footing

Eccentricity in the footing width direction measured from the centerline

 $1/6$ of footing width

Check if the eccentric load limitation is satisfied

$$
F_{VFLC1StrIMin} = 41.63 \cdot \frac{kip}{ft}
$$

\n
$$
M_{uFtLC1StrI} = 87.92 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
e_B := \frac{M_{uFtLC1StrI}}{F_{VFtLC1StrIMin}} = 2.11 \text{ ft}
$$

\n
$$
\frac{B_{footing}}{6} = 2.83 \cdot ft
$$

B_{footing} 6

ſ L \setminus

 $\lt \frac{1000 \text{mJg}}{2}$, "OK", "Not OK"

 $\mathcal{C} = \text{if} \left(e_\mathbf{B} < \frac{\text{round}}{6}, \text{``OK''}, \text{``Not OK''} \right) = \text{``OK''}$

 \setminus

Load Case III

Two cases need to be considered: without and with the live load

Without the live load:

Minimum vertical force without the live load $F_{VFtLC3StrIMin_n0LL} = 46.72 \cdot \frac{\text{kip}}{\text{ft}}$

Moment about the longitudinal axis of the footing (with the live load)

$$
M_{\text{uFtLC3StrI}} = 143.27 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Moment about the longitudinal axis of the footing (without the live load)

$$
M_{\text{uFtLC3StrI_noLL}} := M_{\text{uFtLC3StrI}} - (1.75 \cdot R_{\text{LL}FoothingMax}) \cdot \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) = 113.82 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Eccentricity in the footing width direction m_{e} measured from the centerline eB

Check if the eccentric load limitation is satisfied

$$
P_{\text{B}} := \frac{M_{\text{uFtLC3StrI_noLL}}}{F_{\text{VFtLC3StrIMin noLL}}} = 2.44 \text{ ft}
$$

Check := if
$$
\left(e_B < \frac{B_{\text{footing}}}{6}, \text{"OK"}\right)
$$
, "Not OK" $\right) = \text{"OK"}$

With the live load:

Minimum vertical force with the live load FVFtLC3StrIMin FVFtLC3StrIMin_noLL 1.75RLLFootingMax

Moment about the longitudinal axis of the footing (with the live load)

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$
F_VFtLC3StrIMin := F_VFtLC3StrIMin_n0LL + 1./5RLLFootingMax
$$

$$
F_{VFLC3StrIMin} = 56.27 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft}
$$

$$
e_B := \frac{M_{\text{uFtLC3StrI}}}{F_{\text{VFtLC3StrIMin}}} = 2.55 \text{ ft}
$$

Check := if
$$
\left(e_B < \frac{B_{\text{footing}}}{6}, \text{"OK"}\right)
$$
, "Not OK" = "OK"

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Minimum vertical force without the live load surcharge

Moment about the longitudinal axis of the footing (with the live load surcharge)

$$
F_VFtLC4StrlMin_n oLS = 46.72 \cdot \frac{kip}{ft}
$$

$$
M_uFtLC4StrI = 140.34 \cdot \frac{kip \cdot ft}{ft}
$$

Moment about the longitudinal axis of the footing (without the live load surcharge)

$$
M_{\text{uFtLC4StrI_noLS}} := M_{\text{uFtLC4StrI}} - 1.75 V_{\text{LSFooting}} \cdot \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2}\right) ... + -1.75 \cdot P_{\text{LSFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}}\right)}{2}
$$

$$
M_{\text{uFtLC4StrI_noLS}} = 116.67 \cdot \frac{k_{\text{ip}} \cdot ft}{ft}
$$

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$
e_B := \frac{M_{uFtLC4StrI_n0LS}}{F_{VFtLC4StrIMin_n0LS}} = 2.5 \text{ ft}
$$

Check := if
$$
\left(e_B < \frac{B_{\text{footing}}}{6}, \text{"OK"}\right)
$$
, "Not OK" = "OK"

With the live load surcharge:

Minimum vertical force with the live load surcharge

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

Minimum vertical force with the live load

\nStve that the longitudinal axis of the footing

\nComment about the longitudinal axis of the footing

\nElectro the rotating

\nElectro the starting in the footing width direction

\nCheck if the eccentric load limitation is satisfied

\nCheck if the eccentric load limitation is satisfied

\nCheck:

\n
$$
\frac{M_{\text{UFLC4Str1}}}{F_{\text{VFLC4Str1}}}
$$
\nCheck:

\n
$$
\frac{B_{\text{footing}}}{F_{\text{VFLC4Str1}}}
$$
\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFLC4Str1}} = 2.77 \, \text{ft}
$$

\nCheck:

\n
$$
F_{\text{VFL
$$

Step 2.7 Backwall Design

Description

This step presents the design of the backwall.

Page Contents 47 Forces and Moments at the Base of the Backwall 47 Design for Flexure

- **50 Design for Shear**
- **52 Shrinkage and Temperature Reinforcement Design**

Forces and Moments at the Base of the Backwall

Step 2.5 presents the load effects at the base of the backwall under different load cases and limit states. A summary is presented in the following tables:

Factored shear force parallel to the Factored vertical force, F_{VBW} (kip/ft) Factored sites axis of the backwall, V_{UBW} (kip/ft)

Factored moment about the longitudinal axis of the backwall, $\rm M_{uBw}$ (kip[.]ft/ft)

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

Moment demand at the base of the backwall \blacksquare

$$
M_{\text{DemandBackwall}} := M_{\text{uBwLC4StrI}} = 1.83 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Flexural Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

LRFD 5.10.3.2

Note: MDOT limits reinforcement spacing to a maximum of 18 in. **BDG 6.20.03 and 6.20.03A**

Backwall thickness t

 $t_{\text{backwall}} = 18 \cdot \text{in}$ Select a spacing for reinforcing steel bars $s_{bar} := 18 \cdot in$

47

Select a 1-ft wide strip for the design.

Area of reinforcing steel provided in a 1-ft wide section

Effective depth

Resistance factor for flexure

Width of the compression face of the section

Stress block factor

Solve the following equation of A_s to calculate the required area of steel to satisfy the moment demand. Use an assumed initial A_s value to solve the equation.

Initial assumption

Required area of steel

Check if $A_{sProvided} > A_{sRequired}$

Moment capacity of the section with the provided steel

Distance from the extreme compression fiber to the neutral axis

Check the validity of assumption, $f_s = f_v$ Ch

Limits for Reinforcement LRFD 5.6.3.3 The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

A_{sProvided} :=
$$
\frac{A_{bar} \cdot 12in}{s_{bar}} = 0.29 \cdot in^2
$$

\n d_e := t_{backwall} - Cover_{bw} = 15 in
\n ϕ_f := 0.9 LRFD 5.5.4.2
\nb := 12in LRFD 5.6.2.2
\n β_1 := min $\left[\max\left[0.85 - 0.05 \cdot \left(\frac{f_c - 4ksi}{ksi}\right), 0.65\right], 0.85\right] = 0.85$
\nrequired area of steel to satisfy the moment demand. Use an
\n A_s := 0.3in²
\nGiven M_{DemandBackwall} if = $\phi_f \cdot A_s \cdot f_y \cdot \left[d_e - \frac{1}{2} \cdot \left(\frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot b}\right)\right]$
\n $A_{s,req}$:= Find $(A_s) = 0.03 \cdot in^2$
\nCheck := if $(A_s$ provided > A_{s,req}, "OK", "Not OK") = "OK"
\n $\left[d_e - \frac{1}{2} \cdot \left(\frac{A_s$ Provided $\cdot f_y}{0.85 \cdot f_c \cdot b}\right)\right]$
\nM_{CapacityBackwall} := $\phi_f \cdot A_s$ provided $\cdot f_y \cdot \frac{\left[d_e - \frac{1}{2} \cdot \left(\frac{A_s$ Provided $\cdot f_y}{0.85 \cdot f_c \cdot b}\right)\right]}{ft}$
\n ϕ_f

$$
0.85 \cdot f_c \cdot \beta_1 \cdot b
$$

heck _{$-$} $f_s := i f\left(\frac{c}{d_e} < 0.6, "OK", "Not OK"\right) = "OK"$

Flexural cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental $\gamma_3 := 0.67$ For ASTM A615 Grade 60 reinforcement

Section modulus

Cracking moment

Factored moment to satisfy the minimum reinforcement requirement

1.33 times the factored moment demand

Check the adequacy of the section capacity \overline{C}

$$
S_{c} := \frac{1}{6} \cdot b \cdot t_{backwall}^{2} = 648 \cdot in^{3}
$$
\n
$$
M_{cr} := \frac{\gamma_{3} \cdot \gamma_{1} \cdot f_{r} \cdot S_{c}}{ft} = 24.06 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
1.33 \cdot M_{DemandBackwall} = 2.43 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{req} := \min(1.33 M_{DemandBackwall}, M_{cr}) = 2.43 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
heck := \text{if} \left(M_{CapacityBackwall} > M_{req}, \text{"OK", "Not OK"} \right) = \text{"OK"}
$$

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement does not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

> 1 2

 $x := 3 \cdot in$

 \cdot b \cdot x² = $\frac{E_s}{E}$

Assumed distance from the extreme compression fiber to the neutral axis

Given

Position of the neutral axis

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to service limit state moment

 f_{ss} (not to exceed $0.6f_v$) f

$$
s \le \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c
$$
 LRFD Eq. 5.6.7-1

$$
\gamma_e := 1.00
$$

$$
d_c := \text{Cover}_{bw} = 3 \cdot \text{in}
$$

$$
\beta_{cs} := 1 + \frac{d_c}{\beta_{cs}} = 1.29
$$

$$
\beta_{\rm s} \coloneqq 1 + \frac{a_{\rm c}}{0.7 \left(t_{\rm backwall} - d_{\rm c} \right)} = 1.29
$$

 $=$ $\frac{1}{F}$ A_sProvided $\left(d_e - x\right)$

$$
E_{\rm c} = \text{Find}(x) = 2.234 \cdot \text{in}
$$

$$
T_{s} := \frac{M_{uBackwallSerI}}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 0.9 \cdot kip
$$

$$
f_{ss1} := \frac{T_{s}}{A_{sProvided}} = 3.19 \cdot ksi
$$

$$
f_{\text{SS}} := \min\left(f_{\text{SS}1}, 0.6f_{\text{V}}\right) = 3.19 \text{ k}
$$

max

L L L L L L L

II II II II II II Ц

L L ŀ L

L L L L L L L

II II II II II II Ц $0.11 \frac{\text{in}^2}{\text{}}$ ft

 $1.3 \cdot h_{\text{backwall}} \cdot t_{\text{backwall}} \cdot \frac{kip}{in \text{ ft}}$

 $2(h_{\text{backwall}} + t_{\text{backwall}}) \cdot f_{\text{y}}$

Check := if $(A_{sProvided} > A_{shrink,temp}, "OK", "Not OK") = "OK"$

 \setminus $\overline{}$ J

> I 1 1 \rfloor

I 1 1 1 1 I $\overline{}$

 \parallel $\mathop{||}$ $\mathop{||}$ $\mathop{||}$ $\mathop{||}$ \parallel ∐ $\overline{}$ $\overline{}$ $\overline{}$ $\overline{}$ $\overline{}$ $\overline{}$ \perp

II II II II II II Ц

ſ L \setminus

Minimum area of shrinkage and temperature reinforcement

 $A_{shrink,temp} \coloneqq \min$ ft 0.14 in²

Check if the provided area of steel > the required area of shrinkage and temperature steel

Design for Shear

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

Note: Since there is no transverse reinforcement in the backwall and the overall depth of the backwall is greater than 16 in., the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used.

The factored N_u, V_u, and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the backwall.

Factored axial force at the critical section (use negative if compression)

Load at the critical section due to live load surcharge

Factored shear force (demand) at the critical section

Check M_{u} since it cannot be taken less than $V_u d_v$

Net longitudinal tensile strain in the section at the centroid of the tension reinforcement

Crack spacing parameter as influenced by the maximum aggregate size

 $N_{\text{uBackwallShear}} \coloneqq -\left\lfloor 1.25 \cdot \left(\text{DC}_{\text{backwall}} - \text{d}_{\text{v}} \cdot \text{t}_{\text{backwall}} \cdot \text{W}_{\text{c}} \right) \right\rfloor$ $N_{\text{uBackwallShear}} = -0.85 \cdot \frac{kip}{ft}$ PEHBackwallShear $=$ $\frac{1}{2}$ Lateral earth load at the critical section $P_{\text{EHBackwallShear}} := \frac{1}{2} k_a \gamma_s \left(h_{\text{backwall}} - d_v \right) \left(h_{\text{backwall}} - d_v \right)$ $P_{EHBackwallShear} = 0.16 \cdot \frac{kip}{ft}$ PLSBackwallShear $:= k_a \cdot \gamma_s \cdot h_{eq} \cdot (h_{backwall} - d_v) = 0.22 \cdot \frac{kip}{ft}$ $k = k_a \cdot \gamma_s \cdot h_{eq} \cdot (h_{backwall} - d_v) = 0.22$ $V_{\text{uBackwallShear}} = 1.5 \cdot P_{\text{EHBackwallShear}} + 1.75 \cdot P_{\text{LSBackwallShear}}$ $V_{\text{uBackwallShear}} = 0.63 \cdot \frac{kip}{ft}$ Factored moment at the critical section $M_{\text{uBackwallShear}} \coloneqq 1.5 \cdot P_{\text{EHBackwallShear}}$ $(h_{\text{backwall}} - d_{\text{v}})$ $\frac{3}{3}$ 1.75 PLSBackwallShear $(h_{\text{backwall}} - d_{\text{v}})$ 2 $+1.75 \cdot P_{ISRackwallShear}$ \approx 1.5. P_{FHRackwallShear} $\frac{\sqrt{3.00 \text{ m/s}}}{2}$... $M_{\text{uBackwallShear}} = 0.82 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ $M_{\text{uWallShear}} \coloneqq \max \left(M_{\text{uBackwallShear}}, V_{\text{uBackwallShear}} \cdot d_{\text{v}} \right)$ $M_{\text{uWallShear}} = 0.82 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ $\varepsilon_{\rm s}$ M_{uBackwallShear} $\mathbf{d}_{\mathbf{v}}$ $+ 0.5 \cdot N_{\text{uBackwallShear}} + V_{\text{uBackwallShear}}$ ſ L \setminus \setminus $\cdot \rceil$ J $E_{\rm s}$ A_sProvided $\frac{1}{\sqrt{t}}$ $:=$ $\varepsilon_{\rm e} = 1.03 \times 10^{-4}$ **LRFD Eq. 5.7.3.4.2-4** Crack spacing parameter $s_x := d_v = 1.23 \text{ ft}$ **MDOT Standard Specifications For Construction Table 902-1** Maximum aggregate size (in.) **and Superversion Construction Table 902-1 ag** $= 1.5$ **b 1.5 b 1.5 for Construction Table 902-1** $(80in)$ max $(12in)$ s x $\left(s_{\text{X}}\!\cdot\!\frac{1.38}{\text{a}_{\text{g}}+0.63}\right)$ \setminus \setminus $\overline{}$ J L L L L $\overline{}$ $\overline{}$ $\overline{}$ \perp II II II Ц II II II Ц \mathbf{r} L L L L I 1 1 I $\overline{}$ \parallel II II II Ц \parallel $\mathop{||}$ $\mathop{||}$ II ∐ $=$ min $||$ $||$ \sim $\frac{1}{2}$ \sim $||$ $||$ $=$ 12 \cdot in LRFD Eq. **5.7.3.4.2-7**

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear $β := \frac{4.8}{(1.75)}$ $(1 + 750 \cdot \varepsilon_{\rm s})$ 51 39 s xe in $\ddot{}$ ſ L \setminus \setminus $\overline{}$ J $\frac{4.6}{\sqrt{1.156}} = 4.46$ **LRFD Eq. 5.7.3.4.2-2** Nominal shear resistance of concrete, V_n , is calculated as follows: V_{c1} = 0.0316 β $\sqrt{f_c$ ksi b d_e = 43.9 kip **LRFD Eq. 5.7.3.3-3** V_{c2} = 0.25f_c·b·d_e = 135·kip **LRFD Eq. 5.7.3.3-2** $V_n := min(V_{c1}, V_{c2}) = 43.9$ ·kip Resistance factor for shear $\phi_{\rm v} = 0.9$ **LRFD 5.5.4.2** Factored shear resistance (capacity) $V_r := \phi_V \cdot V_n = 39.51 \cdot \text{kip}$ Check if the shear capacity is greater than Check is the demand $\text{Check} := \text{if}$ $V_{\mathbf{r}}$ $\frac{1}{\text{ft}}$ > V_{uBackwallShear}, "OK", "Not OK" ſ L \setminus \setminus $:= \text{if} \left(\frac{1}{\text{ft}} > V_{\text{uBackwallShear}}, \text{''OK''}, \text{''Not OK''} \right) = \text{''OK''}$ **Shrinkage and Temperature Reinforcement Design** The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the backwall. The spacing of the main reinforcing steel bars in walls and slabs shall not be greater than the lesser of 1.5 times the thickness of the member or 18 in. **LRFD 5.10.6** The spacing of shrinkage and temperature reinforcement shall not exceed the following: 12 in. for walls and footings greater than 18 in. For all other situations, 3 times the component thickness but not less than 18 in. **LRFD 5.10.6** Note: MDOT limits reinforcement spacing to a maximum of 18 in. **BDG 6.20.03 and 6.20.03A** Select a trial bar size \Box Nominal diameter of a reinforcing steel bar $d_{bST} = Dia(bar) = 0.75 \cdot in$ Cross-section area of the bar A_{barST} := Area (bar) = 0.44 in² Select a spacing for reinforcing steel bars $s_{barST} = 18 \cdot in$ For the 18 in. thick backwall Horizontal reinforcing steel area provided in the section A_{sProvidedST} A_{barST} 12in sbarST $= \frac{PbarST^{-12}m}{T} = 0.29 \cdot in^2$

The required minimum shrinkage and temperature reinforcement area at the backwall was previously calculated during the design of flexural reinforcement.

Required shrinkage and required surinkage and
temperature steel area $A_{\text{shrink.temp}} = 0.14 \cdot \text{in}^2$

Check if the provided steel area > the required area of shrinkage and temperature steel

Check := if $(A_{sProvidedST} > A_{shrink.temp}$, "OK", "Not OK" $) =$ "OK"

The backwall design presented in this step provides the following details:

- No. 6 bars @ 18.0 in. spacing $(A_s = 0.29 \text{ in.}^2/\text{ft})$ as the back face flexural reinforcement
- No. 6 bars @ 18.0 in. spacing $(A_s = 0.29 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 18.0 in. spacing $(A_s = 0.29 \text{ in.}^2/\text{ft})$ as the front and back face horizontal shrinkage and temperature reinforcement.

Step 2.8 Abutment Wall Design

Description

This step presents the design of the abutment wall.

Forces and Moments at the Base of the Abutment Wall

Step 2.5 presents the load effects at the base of the abutment wall under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VWall} (kip/ft) Factored shear force parallel to the transverse axis of the abutment wall, $V_{\text{uWall}}^{\dagger}$ (kip/ft)

Factored moment about the longitudinal axis of the abutment wall, M_{u Wall (kip[.]ft/ft)

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

 $= M_{\text{uWallI}} C4S_{\text{trI}} = 131.04$

Moment demand at the base of the wall $M_{\text{DemandWall}} \coloneqq M_{\text{uWallLC4StrI}} = 131.04 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

Flexural Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial har size bar $\ln 9$

Check if $A_{sProvided} > A_{sRequired}$
Check $i = \text{if } (A_{sProvided} > A_{sRequired}, "OK", "Not OK") = "OK"$

Moment capacity of the section with the provided steel area

Distance from the extreme compression fiber to the neutral axis

Check the validity of assumption, $f_s = f_v$

 A _SProvided f_y $0.85 \cdot f_c \cdot b$

ft

 \setminus $\overline{}$).

ا۱ II Ц

 $d_e - \frac{1}{2}$ 2

> \setminus $\overline{}$ J

L

 $\Big| d_e - \frac{1}{2}$.

ſ L \setminus

Limits for Reinforcement LRFD 5.6.3.3

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

1

Flexural cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

The factored moment to satisfy the

Check the adequacy of the section capacity

6 $=$ $\frac{1}{6}$ ·b·t_{wall}² = 2.89 × 10³·in³ $\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c$ ft $107.25 \cdot \frac{\text{kip} \cdot \text{ft}}{2}$ ft $:=\frac{3+1+2}{2}=107.25$

 $M_{\text{CapacityWall}} \coloneqq \Phi_{f} \cdot A_{\text{sProvided}} \cdot f_{\text{y}} \cdot$

 $M_{\text{CapacityWall}} = 153.09 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 A _SProvided f_y $0.85 \cdot f_c \cdot \beta_1 \cdot b$ $\frac{2.31 \times 10^{10} \text{ m/s}}{2.31 \times 10^{10} \text{ m}} = 2.31 \cdot \text{in}$

 d_e

 \setminus

 $\frac{c}{d}$ < 0.6 , "OK" , "Not OK"

 $\gamma_3 = 0.67$ For ASTM A615 Grade 60 reinforcement

 $:=$ if $\left| \frac{1}{\cdot} \right| < 0.6$, "OK", "Not OK" $\left| = \text{"OK"} \right|$

1.33 times the factored moment demand $1.33 \cdot M_{\text{DemandWall}} = 174.29 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

The factored moment to satisfy the minimum reinforcement requirement requirement\n
$$
M_{req} := \min(1.33 M_{\text{DemandWall}}, M_{cr}) = 107.25 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Check := if
$$
(M_{\text{CapacityWall}} > M_{\text{req}}, \text{"OK"}
$$
, "Not OK") = "OK"

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement does not exceed the service limit state stress.

Spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

$$
s \le \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c
$$
 LRFD Eq. 5.6.7-1

$$
\gamma_e := 1.00
$$

57

Distance from extreme tension fiber to center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

2

 \cdot b \cdot x² = $\frac{E_s}{E}$

 $E_{\rm c}$

 $=$ $\frac{1}{F}$ A_sProvided $\left(d_e - x\right)$

Given $\frac{1}{2}$

Assumed distance from the extreme Example distance from the externe
compression fiber to the neutral axis $x := 6 \cdot in$

Position of the neutral axis $x_{n_0} := \text{Find } (x) = 6.197 \cdot \text{in}$

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to service limit state moment

 f_{ss} (not to exceed 0.6f_y)

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement Requirement LRFD 5.10.6

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the wall:

Minimum area of shrinkage and

Check if the provided area of steel > the required area of shrinkage and temperature steel

Minimum area of shrinkage and temperature reinforcement

\nCheck if the provided area of sterile > the required area of shrinkage and

\n
$$
A_{\text{shrink.temp}} := \min \left[\left[\frac{0.60 \frac{\text{in}^{2}}{\text{ft}}}{2 \left(h_{\text{wall}} + t_{\text{wall}} \right) \cdot f_{\text{y}}} \right] \right] \cdot \text{ft} = 0.35 \cdot \text{in}^{2}
$$
\nCheck if the provided area of shrinkage and

\n
$$
C \cdot \text{heat} = \text{if} \left(A_{\text{sProvided}} > A_{\text{shrink.temp}}, \text{``OK''}, \text{``Not OK''} \right) = \text{``OK''}
$$

$$
T_{s} := \frac{M_{uWallLC4SerI}}{d_{e} - \frac{x_{na}}{3}}
$$

$$
f_{ss1} := \frac{T_{s}}{A_{sProvided}} = 32.12 \text{ ksi}
$$

$$
f_{ss} := \min(f_{ss1}, 0.6f_{y}) = 32.12 \text{ ksi}
$$

$$
f_{ss} := \min(f_{ss1}, 0.6f_{y}) = 32.12 \text{ ksi}
$$

$$
B_{barRequired} := \frac{700 \text{ s} \cdot f_{\text{ss}}}{\beta_{s} \cdot f_{\text{ss}}} - 2 \text{ d}_{c} = 13.42 \text{ in}
$$

Check $:=$ if $(s_{bar} < s_{barn$ Requred $, "OK" , "Not OK") = "OK"$

$$
d_{\mathbf{c}} \coloneqq \text{Cover}_{\text{wall}} = 3 \cdot \text{in}
$$

$$
\beta_S := 1 + \frac{d_C}{0.7(t_{wall} - d_C)} = 1.12
$$

Design for Shear

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

The maximum factored shear force The maximum factored shear force
at the base of the abutment wall $V_{\text{uWallLC4StrI}} = 15.7 \cdot \frac{\text{kip}}{\text{ft}}$ Effective width of the section $b_v := b = 12 \cdot in$ Depth of the equivalent rectangular as
tress block a A _SProvided f_y $0.85 \cdot f_c \cdot b$ $\frac{1}{2} = \frac{1.96 \times 10^{14} \text{ J}}{2.95 \times 10^{14} \text{ J}} = 1.96 \cdot \text{in}$ Effective shear depth $d_V := max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{wall} \right) = 34.02 \cdot in$ **LRFD** \setminus $= max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{wall} \right) = 34.02 \cdot in$

Note: Since there is no transverse reinforcement in the wall and the overall depth of the wall is greater than 16 in., the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used.

The factored N_u , V_u , and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the abutment wall.

Factored axial force at the critical section (use negative if compression)

 $N_{\text{uWallShear}} \coloneqq -[1.25 \cdot (\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} - d_{\text{v}} \cdot t_{\text{wall}} \cdot W_{\text{c}}) + 1.5 \text{DW}_{\text{Sup}}] = -18.33 \cdot \frac{\text{kip}}{\text{ft}}$ $= -1.25 \cdot [DC_{Sun} + DC_{backwall} + DC_{wall} - d_V t_{wall} \cdot W_c] + 1.5DW_{Sun} = -18.33$

Lateral earth load at the critical section

Load at the critical section

critical section

Lateral earth load at the critical
\nsection

\n
$$
P_{EHWallShear} := \frac{1}{2} \cdot \left[k_a \cdot \gamma_s \cdot \left(h_{backwall} + h_{wall} - d_v \right) \right] \cdot \left(h_{backwall} + h_{wall} - d_v \right)
$$
\nEach term of the vertical section

\n
$$
P_{EHWallShear} = 6.47 \cdot \frac{kip}{ft}
$$
\nLocal at the critical section

\n
$$
P_{LSWallShear} := k_a \cdot \gamma_s \cdot h_{eq} \cdot \left(h_{backwall} + h_{wall} - d_v \right) = 1.36 \cdot \frac{kip}{ft}
$$
\nFactored shear force (demand) at the
\ncritical section

\n
$$
V_{uWallShear} := 1.5 \cdot P_{EHWallShear} + 1.75 \cdot P_{LSWallShear} + 0.5 \cdot TU
$$
\n
$$
V_{uWallShear} = 12.23 \cdot \frac{kip}{ft}
$$

Factored moment at the critical section

$$
M_{\text{uWallShear}} := 0.9 \cdot \text{DC}_{\text{backwall}} \cdot \frac{(t_{\text{backwall}} - t_{\text{wall}})}{2} + (1.25 \cdot \text{DC}_{\text{Sup}} + 1.5 \cdot \text{DW}_{\text{Sup}}) \cdot \left(1_{\text{brtowall}} - \frac{t_{\text{wall}}}{2} \right) \dots
$$

+ 1.5 \cdot P_{\text{EHWallShear}} \cdot \frac{(h_{\text{backwall}} + h_{\text{wall}} - d_{\text{v}})}{3} \dots
+ 1.75 \cdot P_{\text{LSWallShear}} \cdot \frac{(h_{\text{backwall}} + h_{\text{wall}} - d_{\text{v}})}{2} + 0.5 \cdot \text{TU} \cdot (h_{\text{wall}} - d_{\text{v}}) + 0.5 \cdot \text{TU} \cdot (h_{\text{wall}} - d_{\text{v}}) \right)

Check less than $V_u d_v$ $M_{\text{uWallShear}} \coloneqq \max \left(M_{\text{uWallShear}}, V_{\text{uWallShear}} \cdot d_{\text{v}} \right) = 91.55 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ ft

60

Net longitudinal tensile strain in the section at the centroid of the tension reinforcement $\varepsilon_{\rm s}$ $M_{\rm uWallShear}$ d_V $+0.5\cdot N_{\text{uWallShear}} + V_{\text{uWallShear}}$ ſ L \setminus \setminus $\cdot \rceil$ J $E_{\rm s}$ A_sProvided $\frac{1}{\sqrt{t}}$ $\frac{1}{2}$ = 1.22 × 10⁻³ **LRFD Eq. 5.7.3.4.2-4** Crack spacing parameter $s_x := d_v = 2.83 \text{ ft}$ **MDOT Standard Specifications** Maximum aggregate size (in.)
For Construction Table 902-1 ag $= 1.5$ **ag** $= 1.5$ **for Construction Table 902-1** Crack spacing parameter as influenced by the maximum aggregate size $(80in)$ max $(12in)$ $\left(s_{\text{X}}\!\cdot\!\frac{1.38}{\text{a}_{\text{g}}+0.63}\right)$ \setminus \setminus $\overline{}$ J L L L L $\overline{}$ $\overline{}$ $\overline{}$ \perp II II II Ц II II II Ц \mathbf{r} L L L L I 1 1 I $\overline{}$ \parallel II II II Ц \parallel $\mathop{||}$ $\mathop{||}$ II ∐ $=$ min $||$ $||$ \sim \sim $||$ $||$ = 22.04 in **LRFD Eq. 5.7.3.4.2-7** Factor indicating the ability of diagonally cracked concrete to transmit tension and shear $β := \frac{4.8}{(1.75)}$ $(1 + 750 \cdot \varepsilon_{\rm s})$ 51 39 s xe in $\ddot{}$ ſ L \setminus \setminus $\overline{}$ J $\frac{12}{(1+750.5)} \cdot \frac{21}{(1+750.5)} = 2.09$ **LRFD Eq. 5.7.3.4.2-2** Nominal shear resistance of concrete, V_n , is calculated as follows: V_{c1} = 0.0316·β $\sqrt{f_c$ ·ksi·b·d_e = 48.2·kip **LRFD Eq. 5.7.3.3-3** V_{c2} = 0.25f_c·b·d_e = 315·kip **LRFD Eq. 5.7.3.3-2** $V_n := min(V_{c1}, V_{c2}) = 48.16$ ·kip Resistance factor for shear $\phi_{\rm v} = 0.9$ **LRFD 5.5.4.2** Factored shear resistance (capacity) $V_r := \phi_V \cdot V_n = 43.34 \cdot \text{kip}$

Check if the capacity $>$ the demand

Development Length of Reinforcement

The flexural reinforcing steel must be developed on each side of the critical section for its full development length.

Basic development length

Reinforcement location factor $\lambda_{r} = 1$ No more than 12 in. concrete below

Distance from center of the bar to the nearest concrete surface
 $\text{c}_b := \text{Cover}_{\text{wall}} = 3 \cdot \text{in}$ **LRFD 5.10.8.1.2, 5.10.8.2.1**

 $db \coloneqq 2.4 \cdot d_{bar}$ f y f_c ·ksi $\frac{1}{2}$ = 2.4 $\frac{d_{\text{bar}}}{f_{\text{f}}$ Lesi = 7.82 ft **LRFD Eq. 5.10.8.2.1a-2**

 $V_{\mathbf{r}}$

ſ L \setminus

Coating factor $\lambda_{cf} = 1.5$ Epoxy coated bars with less than 3d_b cover

 \setminus

 $\frac{1}{\text{ft}}$ > V_{uWallShear}, "OK", "Not OK"

 $:= \text{if} \left(\frac{1}{\text{ft}} > V_{\text{uWallShear}}, \text{''OK''}, \text{''Not OK''} \right) = \text{''OK''}$

Shrinkage and Temperature Reinforcement

Required shrinkage and Required shrinkage and
temperature steel area $A_{\text{shrink.temp}} = 0.35 \cdot \text{in}^2$ Check if the provided steel area > the required area of shrinkage and temperature steel Check := if $(A_{sProvidesST} > A_{shrink.temp}$, "OK", "Not OK" $) =$ "OK"

The abutment wall design presented in this step provides the following details:

- No. 9 bars @ 12.0 in. spacing $(A_s = 1.0 \text{ in.}^2/\text{ft})$ as the back face flexural reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front and back face horizontal shrinkage and temperature reinforcement.

Step 2.9 Structural Design of the Footing

Description

This step presents the structural design of the abutment footing.

Forces and Moments at the Base of the Abutment Footing

Step 2.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VFt} (kip/ft)

LC III 16.59 11.06 LC IV | 19.85 | 13.12

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Note: In this example, the length of the footing and the abutment wall is 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Toe Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:

For structural design of an eccentrically loaded foundation, a triangular or trapezoidal bearing pressure distribution is used.

LRFD 10.6.5

According to the loads in the summary tables, Load Case III under the Strength I limit state is identified as the governing load case for the design of flexure and shear at the toe.

$$
F_{VFLC3StrI} = 74.75 \cdot \frac{kip}{ft}
$$

$$
M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft}
$$

Eccentricity in the footing width direction

$$
e_{\text{B}} := \frac{M_{\text{uFtLC3StrI}}}{F_{\text{VFtLC3StrI}}} = 1.92 \cdot \text{ft}
$$

Maximum and minimum bearing pressure

$$
q_{\text{max}} := \frac{F_{\text{VFLC3StrI}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 7.37 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFLC3StrI}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 1.42 \cdot \text{ksf}
$$

The critical section for flexural design is at the front face of the wall. **LRFD 5.12.8.4**

Bearing pressure at the critical section

$$
q_{\text{toe}} := q_{\text{min}} + \frac{\left(q_{\text{max}} - q_{\text{min}}\right)}{B_{\text{footing}}} \cdot \left(B_{\text{footing}} - l_{\text{toe}}\right) = 5.77 \cdot \text{ksf}
$$

A simplified analysis method is used in this example to determine the maximum moments at the front face of the wall by selecting load factors to produce the maximum bearing pressure and minimum resisting loads. This method is conservative and eliminates the need for using multiple combinations.

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum moment at the front face of the wall.

The moment demand at the critical section

$$
M_{rDemand} := q_{toe} \cdot \frac{1_{toe}^{2}}{2} + (q_{max} - q_{toe}) \cdot \frac{1_{toe}^{2}}{3} - 0.9 \cdot W_{c} \cdot t_{footing} \cdot \frac{1_{toe}^{2}}{2} - 1.0 \gamma_{s} \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{1_{toe}^{2}}{2}
$$

$$
M_{rDemand} = 62.51 \cdot \frac{kip \cdot ft}{ft}
$$

Flexural Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Solve the following equation of A_s to calculate the required area of steel to satisfy the moment demand. Use an assumed initial A_s value to solve the equation.

Moment capacity of the section with the provided steel $M_{Provided} := \phi_f \cdot A_{sProvided} \cdot f_y$

Distance from the extreme compression fiber to the neutral axis

Check the validity of the assumption, $f_s = f$ $= f_y$ Check_f_s := if $\frac{c}{d}$

Limits for Reinforcement LRFD 5.6.3.3

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

1.33 times the factored moment demand

The factored moment to satisfy the minimum reinforcement requirement

Check the adequacy of section capacity

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

$\frac{1}{\sqrt{1.825 \cdot 8.81}} = 1.82 \cdot \text{in}$ $\frac{c}{d}$ < 0.6 , "OK" , "Not OK" \setminus $\overline{}$ J $:=$ if $\left| \frac{1}{\cdot} \right| < 0.6$, "OK", "Not OK" $\left| = \text{"OK"} \right|$

 $d_e - \frac{1}{2}$ 2

L

 $:= \Phi_f \cdot A_s p_{\text{rovided}} \cdot f_v$

 $M_{\text{Provided}} = 111.01 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 d_e

 \setminus

 A _SProvided f_y $0.85 \cdot f_c \cdot \beta_1 \cdot b$

 $\Big| d_e - \frac{1}{2}$.

ſ L \setminus

$$
\gamma_1 := 1.6
$$
 For concrete structures that are not precast segmental
\n
$$
\gamma_3 := 0.67
$$
 For ASTM A615 Grade 60 reinforcement
\n
$$
S_c := \frac{1}{6} \cdot b \cdot t_{footing}^2 = 2.59 \times 10^3 \cdot in^3
$$
\n
$$
M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.25 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
1.33 \cdot M_{rDemand} = 83.14 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{req} := min(1.33 M_{rDemand}, M_{cr}) = 83.14 \cdot \frac{kip \cdot ft}{ft}
$$
\nCheck := if (M_{provided} > M_{req}, "OK", "Not OK") = "OK"

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement does not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest bar

$$
s \le \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c
$$

LRFD Eq. 5.6.7-1

$$
\gamma_e := 1.00
$$

$$
d_c := \text{Cover}_{ft} = 4 \cdot in
$$

 A _SProvided f_y $0.85 \cdot f_c \cdot b$

ft

 \setminus $\overline{}$).

ا۱ II Ц Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

$$
\beta_{\rm S} \coloneqq 1 + \frac{d_{\rm c}}{0.7 \left(t_{\rm footing} - d_{\rm c}\right)} = 1.18
$$

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, $f_{\rm ss}$, requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme compression fiber to the neutral axis

$$
x := 5 \cdot in
$$

Given
$$
\frac{1}{2} \cdot b \cdot x^2 = \frac{E_s}{E_c} \cdot A_{sProvided} \cdot (d_e - x)
$$

$$
x_{\text{max}} := \text{Find}(x) = 5.303 \cdot in
$$

Position of the neutral axis $x_{na} := Find(x)$

Vertical force and moment at the base of the footing from Load Case III under the Service I limit state are:

$$
F_{VFLC3SerI} = 55.33 \cdot \frac{kip}{ft}
$$

\nEccentricity in the footing width
\ndirection under Service I limit state
\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
F_{VFLC3SerI} = 1.25 \cdot ft
$$

\n
$$
F_{VFL
$$

The moment at the critical section under the Service I limit state:

$$
M_{rSerI} := q_{toeSerI} \cdot \frac{l_{toe}^{2}}{2} + (q_{maxSerI} - q_{toeSerI}) \cdot \frac{l_{toe}^{2}}{3} - W_{c} \cdot t_{footing} \cdot \frac{l_{toe}^{2}}{2} - \gamma_{s} \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{l_{toe}^{2}}{2}
$$

\n
$$
M_{rSerI} = 36.8 \cdot \frac{kip \cdot ft}{ft}
$$

\nTensile force in the reinforcing steel due
\nto the service limit state moment
\n
$$
T_{s} := \frac{M_{rSerI}}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 14.6 \cdot kip
$$

\n
$$
d_{e} - \frac{x_{na}}{3} = 18.49 \cdot ksi
$$

\n
$$
f_{ss1} := \frac{T_{s}}{A_{sProvided}} = 18.49 \cdot ksi
$$

$$
f_{\rm ss} \text{ (not to exceed } 0.6f_{\rm y})
$$

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement Requirement LRFD 5.10.6

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the toe:

Minimum area of shrinkage and temperature reinforcement

\nCheck if the provided area of steel > the required area of shrinkage and temperature steel

\nCheck if the provided area of steel > the required area of shrinkage and temperature steel

\nCheck:

\n
$$
F = \frac{\text{min} \left[\frac{\text{max} \left[\frac{1.3 \cdot B_{\text{footing}} \cdot t_{\text{footing}} \cdot \frac{k_{\text{ip}}}{\text{min} \cdot f_{\text{p}}}}{2 \left(B_{\text{footing}} + t_{\text{footing}} \right) \cdot f_{\text{y}}} \right] \right]}{\text{Check}} = \frac{\text{max} \left[\frac{1.3 \cdot B_{\text{footing}} \cdot t_{\text{footing}} \cdot \frac{k_{\text{ip}}}{\text{min} \cdot f_{\text{p}}}}{2 \left(B_{\text{footing}} + t_{\text{footing}} \right) \cdot f_{\text{y}}} \right] \right] \cdot \text{max} \cdot
$$

Design for Shear

Effective width of the section

Depth of the equivalent rectangular stress block a

Effective shear depth

The critical section for shear at the toe is located at a distance d_v from the front face of the wall.

Distance from the toe to the critical section

Bearing pressure at the critical section

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum shear at the front face of the wall.

Factored shear force (demand) at the critical section

$$
V_{\text{uFtToe}} := \frac{(q_{\text{max}} + q_{\text{d}})}{2} \cdot l_{\text{shear}} - 0.9 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{shear}} - 1.0 \cdot \gamma_{\text{s}} \cdot (h_{\text{toeDepth}} - t_{\text{footing}}) \cdot l_{\text{shear}} = 12.16 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
f_{ss} \text{ (not to exceed 0.6f)} \qquad f_{SS} := \min \Big(f_{SS1}, 0.6f_y \Big) = 18.49 \cdot \text{ksi}
$$
\n
$$
\text{Required reinforcement spacing} \qquad 700 \cdot \gamma_e \cdot \frac{\text{kip}}{\text{in}} \qquad 700 \cdot \gamma_e \cdot \frac{\text{kip}}{\text{in}} \qquad 700 \cdot \gamma_e \cdot \frac{\text{kip}}{\text{in}} \qquad 24.13 \cdot \text{in}
$$
\n
$$
\text{Check if the spacing provided } \leq \text{the}
$$
\n
$$
\text{Check if the spacing provided } \leq \text{the}
$$
\n
$$
\text{Check } \mathcal{F} \text{ is the same in } \mathbb{C} \text{ and } \mathbb{C} \text{ is the same in } \mathbb{C} \text{ and } \mathbb{
$$

Check := if
$$
(s_{bar} < s_{barRequired}, "OK", "Not OK") = "OK"
$$

$$
b = 12 \cdot \text{in}
$$
\n
$$
a := \frac{A_{\text{sProvided}} \cdot f_{\text{y}}}{0.85 \cdot f_{\text{c}} \cdot b} =
$$

a :=
$$
\frac{A_{\text{sProvided}} t_{\text{y}}}{0.85 \cdot f_{\text{c}} \cdot b}
$$
 = 1.55·in
d_v := max $\left(d_{\text{e}} - \frac{a}{2}, 0.9 \cdot d_{\text{e}}, 0.72 \cdot t_{\text{footing}}\right)$ = 31.23·in LRFD
5.7.2.8

$$
l_{shear} := l_{toe} - d_v = 1.98 \text{ ft}
$$

$$
q_d := q_{min} + \frac{(q_{max} - q_{min})}{B_{footing}} \cdot (B_{footing} - l_{shear}) = 6.68 \cdot \text{ksf}
$$

$$
b = 12 \cdot in
$$

A_{sProvi}

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than $3d_v$.

Check if the distance l_{toe} is less than $3d_v$ Check := if $(l_{\text{toe}} < 3 \cdot d_v$, "Yes", "No" $) =$ "Yes"

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n , is calculated as follows:

 $\beta := 2$

Development Length of Reinforcement

LRFD 5.7.3.4.1

Heel Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:

The self-weight of the footing, the weight of soil, live load surcharge and the bearing pressure act on the heel. The critical load combination for the design selects the load factors to produce the minimum vertical loads and maximum eccentricities resulting in the minimum bearing pressure.

The critical location for the design of flexure is located at the back face of the wall. **LRFD 5.12.8.4** In the general case of a cantilever abutment wall, where the downward load on the heel is larger than the upward reaction of the soil under the heel, the top of the heel is in tension. Therefore, the critical section for shear is taken at the back face of the abutment wall. **LRFD C5.12.8.6.1**

Load cases I, III, and IV under the Strength I limit state are used to calculate the maximum moment and shear at the critical sections.

Load Case I

Maximum and minimum bearing pressure

$$
q_{\text{max}} := \frac{F_{\text{VFLC1StrIMin}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 4.27 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFLC1StrIMin}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 0.62 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC1StrI}} := q_{\text{min}} + \left(q_{\text{max}} - q_{\text{min}}\right) \frac{l_{\text{heel}}}{B_{\text{footing}}} = 2.61 \cdot \text{ksf}
$$

Bearing pressure at the critical section

Factored moment at the critical section

$$
M_{rLCIStrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC1StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLCIStrI} = 120.08 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{uHeelLC1StrI} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC1StrI} - q_{min}) \cdot l_{heel}
$$

$$
V_{uHeelLC1StrI} = 22.9 \cdot \frac{kip}{ft}
$$

Load Case III

Two cases need to be considered: without and with the live load.

Without the live load

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Bearing pressure at the critical section

Minimum vertical force
\nFactored moment about the longitudinal axis of
\nthe footing
\nEccentricity in the footing width direction
\nMaximum and minimum bearing pressure
\n
\n
$$
P_{\text{VFtLC3Str1Min_nOLL}} = 46.72 \cdot \frac{kip \cdot ft}{ft} = \frac{\text{Step 2.6, sliding}}{\text{FvFtLC3Str1_nOLL}} = 46.72 \cdot \frac{kip \cdot ft}{ft} = \frac{\text{Step 2.6, scientific load\nlimitation check\n
$$
e_{\text{B}} := \frac{M_{\text{uFtLC3Str1Min_nOLL}}}{F_{\text{VFtLC3Str1Min_nOLL}}} = 2.44 \cdot ft
$$
\n
$$
q_{\text{max}} := \frac{F_{\text{VFtLC3Str1Min_nOLL}}}{B_{\text{foothing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{foothing}}}\right) = 5.11 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFtLC3Str1Min_nOLL}}}{B_{\text{foothing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{foothing}}}\right) = 0.39 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC3Str1}} := q_{\text{min}} + \left(q_{\text{max}} - q_{\text{min}}\right) \frac{l_{\text{heel}}}{B_{\text{foothing}}} = 2.96 \cdot \text{ksf}
$$
$$

Factored moment at the critical section

$$
M_{rLC3StrI_nOLL} := 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC3StrI_nOLL} = 121.93 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{\text{uHeelLC3StrI_nOLL}} := 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} - q_{\text{min}} \cdot l_{\text{heel}} - \frac{1}{2} \cdot \left(q_{\text{heelLC3StrI}} - q_{\text{min}} \right) \cdot l_{\text{heel}}
$$

$$
V_{\text{uHeelLC3StrI_nOLL}} = 22.4 \cdot \frac{kip}{ft}
$$

With the live load

Minimum vertical force **Step 2.6, sliding** 2.6, sliding 2.6, slidi

Factored moment about the longitudinal axis of the footing

 $Eccentricity$ in the footing width direction ϵ

Maximum and minimum bearing pressure

$$
F_{\text{VFtLC3StrIMin}} = 56.27 \cdot \frac{\text{kip}}{\text{ft}}
$$
Step 2.6, sliding resistance check

$$
M_{\text{uFtLC3StrI}} = 143.27 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
Step 2.6,
summary table

$$
e_{\text{B}} := \frac{M_{\text{uFtLC3StrI}}}{F_{\text{VFtLC3StrIMin}}} = 2.55 \cdot \text{ft}
$$

Maximum and minimum bearing pressure
\n
$$
q_{max} := \frac{F_{VFLC3Str1Min}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 6.28 \cdot \text{ksf}
$$
\n
$$
q_{min} := \frac{F_{VFLC3Str1Min}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.34 \cdot \text{ksf}
$$
\n
$$
q_{helLC3Str1} := q_{min} + \left(q_{max} - q_{min}\right) \frac{l_{hel}}{R_{tot}} = 3.57 \cdot \text{ksf}
$$

Bfooting

Factored moment at the critical section

$$
M_{rLC3StrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC3StrI} = 114.56 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{uHeelLC3StrI} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}
$$

$$
V_{uHeelLC3StrI} = 19.78 \cdot \frac{kip}{ft}
$$
Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge

Minimum vertical force
\nFactored moment about the longitudinal axis of
\nthe footing
\nFactority in the footing width direction
\nMaximum and minimum bearing pressure
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} = 2.5 \cdot ft
$$
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} = 2.5 \cdot ft
$$
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{foothing}}\right) = 5.17 \cdot ksf
$$
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{foothing}}\right) = 0.33 \cdot ksf
$$
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{foothing}}\right) = 0.33 \cdot ksf
$$
\n
$$
q_{min} := \frac{F_{VFLC4StrIMin_nOLS}}{B_{foothing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{foothing}}\right) = 0.33 \cdot ksf
$$
\n
$$
q_{min} = 2.96 \cdot ksf
$$

Factored moment at the critical section

$$
M_{rLC4StrI_n0LS} := 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC4StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC4StrI_n0LS} = 123.54 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{\text{uHeelLC4StrI_nOLS}} := 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} - q_{\text{min}} \cdot l_{\text{heel}} - \frac{1}{2} \cdot \left(q_{\text{heelLC4StrI}} - q_{\text{min}} \right) \cdot l_{\text{heel}}
$$

$$
V_{\text{uHeelLC4StrI_n0LS}} = 22.65 \cdot \frac{\text{kip}}{\text{ft}}
$$

With the live load surcharge

Minimum vertical force $F_{V F t L C 4 S t r I M i n} = 50.61 \cdot \frac{k i p}{f t}$ Step 2.6, sliding

Factored moment about the longitudinal axis of $M_{\text{uFtLC4StrI}} = 140.34 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ **Step** table the footing

Eccentricity in the footing width direction

$$
M_{\text{uFtLC4StrI}} = 140.34 \cdot \frac{\text{kip·ft}}{\text{ft}}
$$

Step 2.6, summary

$$
e_{\text{B}} := \frac{M_{\text{uFtLC4StrI}}}{F_{\text{VFtLC4StrIMin}}} = 2.77 \cdot \text{ft}
$$

resistance check

 q_{max} FVFtLC4StrIMin B_{footing} $1 + \frac{6 \cdot e_B}{\sqrt{2}}$ **B**footing $\ddot{}$ ſ L \setminus \setminus $\overline{}$ J Maximum and minimum bearing pressure $q_{\text{max}} = \frac{q_{\text{max}}}{B_{\text{S}} + 1} \left(1 + \frac{B}{B_{\text{S}} + 1} \right) = 5.89 \text{ ksf}$ qmin FVFtLC4StrIMin B_{footing} $1 - \frac{6 \cdot e_B}{2}$ **B**footing $\Bigg(1 \setminus$ \setminus $\overline{}$ J $\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}} = 0.06 \cdot \text{ksf}$ Bearing pressure at the critical section $q_{heelLC4StrI} = q_{min} + (q_{max} - q_{min})$ l heel **B**footing $= q_{\min} + (q_{\max} - q_{\min}) \frac{\text{mod}}{\text{mod}} = 3.23 \cdot \text{ksf}$

Factored moment at the critical section

$$
M_{rLC4StrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC4StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC4StrI} = 127.15 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{\text{uHeelLC4StrI}} := 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} - q_{\text{min}} \cdot l_{\text{heel}} - \frac{1}{2} \cdot \left(q_{\text{heelLC4StrI}} - q_{\text{min}} \right) \cdot l_{\text{heel}}
$$

$$
V_{\text{uHeelLC4StrI}} = 22.6 \cdot \frac{\text{kip}}{\text{ft}}
$$

Moment demand at the critical section

$$
M_{HeelDemand} := max(M_{rLC1StrI}, M_{rLC3StrI_n0LL}, M_{rLC3StrI}, M_{rLC4StrI_n0LS}, M_{rLC4StrI}) = 127.15 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Shear demand at the critical section

$$
V_{\text{HeelDemand}} \coloneqq \max\left(V_{\text{uHeelLC1StrI}}, V_{\text{uHeelLC3StrI_n0LL}}, V_{\text{uHeelLC3StrI}}, V_{\text{uHeelLC4StrI_n0LS}}, V_{\text{uHeelLC4StrI}}\right)
$$

$$
V_{\text{HeelDemand}} = 22.9 \cdot \frac{\text{kip}}{\text{ft}}
$$

Flexural Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Distance from the extreme compression fiber to the neutral axis

Check the validity of the assumption, $f_s = f$

$$
M_{Provided} = \Psi f' \cdot A_{sProvided} \cdot I_{y'} \qquad \frac{f}{ft}
$$

\n
$$
M_{provided} = 166.45 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
c := \frac{A_{sProvided} \cdot f_y}{0.85 \cdot f_c \cdot \beta_1 \cdot b} = 2.77 \cdot in
$$

\n
$$
= f_y
$$

\nCheck_f_s := if $\left(\frac{c}{d_e} < 0.6, \text{"OK"}\right, \text{"Not OK"} = \text{"OK"}$

Limits for Reinforcement LRFD 5.6.3.3

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

$$
\gamma_1 := 1.6
$$

$$
\gamma_3 := 0.67
$$

Flexural cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental

For ASTM A615 Grade 60 reinforcement

Section modulus
\n
$$
S_c := \frac{1}{6} \cdot b \cdot t_{footing}^2 = 2.59 \times 10^3 \cdot in^3
$$
\n\nCracking moment
\n
$$
M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.25 \cdot \frac{kip \cdot ft}{ft}
$$
\n1.33 times the factored moment demand
\n
$$
1.33 \cdot M_{HeelDemand} = 169.12 \cdot \frac{kip \cdot ft}{ft}
$$
\nThe factored moment to satisfy the minimum reinforcement requirement
\nCheck the adequacy of section capacity
\nCheck := if (M_{Provided} > M_{req}, "OK", "Not OK") = "OK"

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face $s \leq \frac{700 \cdot \gamma_e}{\gamma}$ $\leq \frac{1}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$ **LRFD Eq. 5.6.7-1** Exposure factor for the Class 1 exposure condition $\gamma_e \coloneqq 1.00$ Distance from extreme tension fiber to the Distance from extreme tension floer to the

center of the closest flexural reinforcement
 d_c := Cover_{ft} = 4 in Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face $\beta_{\rm s} \coloneqq 1$ $d_{\mathbf{c}}$ $= 1 + \frac{1}{0.7 (\text{tfooting} - \text{d}_\text{c})} = 1.18$

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, f_{ss} , requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme
\ncompression fiber to the neutral axis
\nGiven
$$
\frac{1}{2} \cdot b \cdot x^2 = \frac{E_s}{E_c} \cdot A_s
$$
 Provided $(d_e - x)$
\nPosition of the neutral axis $x_{na} := Find(x) = 6.4 \cdot in$
\nMaximum and minimum bearing pressure
\nunder Service I limit state
\n(from the to design)
\nBearing pressure at the critical section
\n $q_{HeelSerI} := q_{minSerI} + \frac{(q_{maxSerI} - q_{minSerI})}{B_{footing}} \cdot l_{heel} = 3.38 \cdot ksf$

$$
M_{\text{heelSer1}} = W_{\text{c}} \cdot \text{fototing} \cdot \frac{I_{\text{heel}}}{2} + EV_{\text{earthBk}} \cdot \frac{I_{\text{heel}}}{2} \cdot ...
$$
\n
$$
+ V_{\text{LSFoting}} \cdot \frac{I_{\text{heel}}}{2} - q_{\text{minSer1}} \cdot \frac{I_{\text{heel}}}{2} - (q_{\text{HeelSer1}} - q_{\text{minSer1}}) \cdot \frac{I_{\text{heel}}}{6}
$$
\n
$$
M_{\text{heelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{heelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{heelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{heelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{beelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{beelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{beelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{beelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{beelSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{belSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{belSer1}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{belSet}} = 41.33 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
M_{\text{belSet}} = 41.33 \cdot
$$

The critical section for shear in the heel is located at the back face of the abutment wall. **LRFD C5.12.8.6.1**

Shear demand at the critical section (max. from the load cases)

Effective width of the section b = $12 \cdot in$

Depth of the equivalent rectangular stress block and the computation of the computation of the stress block and the stress and the stress and the stress and the stress stress block

Check := if
$$
(A_{sProvided} > A_{shrink,temp}, "OK", "Not OK") = "OK"
$$

$$
V_{\text{HeelDemand}} = 22.9 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
c := \frac{A_{\rm sProvided} \cdot f_{\rm y}}{0.85 \cdot f_{\rm c} \cdot b} = 2.35 \cdot in
$$

Effective shear depth

$$
d_V := max\left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{footing}\right) = 30.82 \cdot in
$$
 LRFD 5.7.2.8

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than $3d_v$.

Check if the distance $l_{\text{heel}} < 3 d_v$ (

Check := if
$$
(l_{\text{heel}} < 3 \cdot d_v, "Yes", "No") = "No"
$$

LRFD 5.7.3.4.1

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear $\beta = 2$

Nominal shear resistance of concrete, V_n , is calculated as follows:

 V_{c1} = 0.0316 β $\sqrt{f_c$ ksi b d_e = 42 kip **LRFD Eq. 5.7.3.3-3** V_{c2} = 0.25f_c·b·d_e = 288·kip **LRFD Eq. 5.7.3.3-2** $V_n := min(V_{c1}, V_{c2}) = 42.03 \text{·kip}$ Resistance factor for shear $\phi_V = 0.9$ LRFD 5.5.4.2 Factored shear resistance (capacity) $V_r := \phi_V \cdot V_n = 37.83 \cdot \text{kip}$ $V_{\mathbf{r}}$ $\frac{1}{\text{ft}}$ > V_{HeelDemand}, "OK", "Not OK" ſ L \setminus \setminus $:= \text{if} \left(\frac{1}{\text{ft}} > V_{\text{HeelDemand}} , \text{''OK''}, \text{''Not OK''} \right) = \text{''OK''}$

Check if the shear capacity $>$ the demand

Development Length of Reinforcement

Shrinkage and Temperature Reinforcement Design

The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing.

The reinforcement along the longitudinal direction of the footing at the top and bottom should satisfy the shrinkage and temperature reinforcement requirements. **LRFD 5.10.6**

The spacing of shrinkage and temperature reinforcement shall not exceed the following: 12 in. for walls and footings greater than 18 in.

Note: MDOT limits reinforcement spacing to a maximum of 18 in. **BDG 5.16.01 and 5.22.01**

Select a trial bar size bar $= 6$ Nominal diameter of a reinforcing steel bar $d_{\text{bST}} = \text{Dia}(\text{bar}) = 0.75 \cdot \text{in}$ Cross-section area of the bar A_{barST} := Area (bar) = 0.44 · in² Select a spacing for reinforcing steel bars $s_{barST} = 12 \cdot in$ Reinforcing steel area provided in the section A_{barST} 12in sbarST $= \frac{PbarST^{-12}m}{T} = 0.44 \cdot in^2$ Required minimum area of shrinkage and required minimum area of shrinkage and
temperature reinforcement in the footing $A_{\text{shrink.temp}} = 0.33 \cdot \text{in}^2$

Check if the provided steel area > the required area for shrinkage and temperature steel

Check := if
$$
(A_{sProvidedST} > A_{shrink,temp}, "OK", "Not OK") = "OK"
$$

LRFD 5.10.6

The footing design presented in this step provides the following details:

- No. 9 bars @ 10.0 in. spacing $(A_s = 1.0 \text{ in.}^2/\text{ft})$ as the transverse flexural reinforcement at the top of the footing
- No. 8 bars @ 12.0 in. spacing $(A_s = 0.79 \text{ in.}^2/\text{ft})$ as the transverse flexural reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.

Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

Appendix 2.A Braking Force and Wind Load Calculation

Description

This appendix presents the braking force and wind load calculation procedures for illustrative purposes.

Braking Force

Since the abutments have expansion bearings, the fixed bearings at the pier resist the braking force along the longitudinal direction of the bridge.

The braking force (BR) shall be taken as the greater of:

- 25% of the axle weight of the design truck / tandem
- 5% of the design truck / tandem weight plus lane load

The braking force is applied on all design lanes assuming that the bridge carries traffic in one direction.

Braking force per lane due to 25% of the axle weight of the design truck / tandem

 $BR_1 := 25\% \cdot (32kip + 32kip + 8kip) = 18$ ·kip

Braking force per lane due to 5% of the design truck / tandem weight plus plus lane load

$$
BR_2 := 5\% \cdot \left(72\text{kip} + 0.64\frac{\text{kip}}{\text{ft}} \cdot 2L_{\text{span}}\right) = 10 \cdot \text{kip}
$$

Note: The MDOT practice, as reflected in the BDS, is to take only 5% of the design truck plus lane load as the breaking force. In addition, the HL-93 modification factor is not included in the braking force calculation. This example describes the MDOT practice.

Braking force selected for the design BRK $B\text{R} = \text{BR}_2 = 10 \cdot \text{kip}$

The braking force transmitted to the bearings based on the number of lanes with the live load.

The braking force is assumed to be equally shared by the bearings at the pier.

Wind Load

Since the expansion bearings are located over the abutments, the fixed bearings at the pier resist the longitudinal component of the wind load acting on the superstructure.

Wind Load on Superstructure LRFD 3.8.1.1, 3.8.1.2

To calculate the wind load acting on the superstructure, the total depth from the top of the barrier to the bottom of the girder is required. Once the total depth is known, the wind exposure area is calculated. The wind pressure and the exposure area are used to calculate the wind load.

LRFD 3.6.4

Appendix 2.B Sliding Resistance Check for Spread Footings on Clay

Description

This appendix presents the calculation procedure for checking the sliding resistance of spread footings located on a clay layer.

Undrained shear strength (provided by the Geotechnical Service Section)

For footings that rest on clay, where footings are supported on at least 6.0 in. of compacted granular material, the sliding resistance may be taken as the lesser of

- the cohesion of the clay, or
- one-half the normal stress on the interface between the footing and soil.

Figure 10.6.3.4-1-Procedure for Estimating Nominal **Sliding Resistance for Walls on Clay**

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used.

- Live load on the bridge is excluded.
- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to the horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Resistance factor for sliding ϕ_{τ} = 0.85 LRFD Table 10.5.5.5.2-1

According to the loads in the summary tables provided at the end of Step 2.5, LC I or IV could control the design. Therefore, both load cases are checked.

Load Case I

Factored sliding force (demand)

Eccentricity in the footing width direction

Factored shear force parallel to the transverse axis of the footing
\nFactored sliding force (demand)
\nMinimum vertical load
\nEccentricity in the footing width direction
\n
$$
V_{\text{b}} = V_{\text{u}}F_{\text{t}}C_{\text{d}}F_{\text{t}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
V_{\text{sliding}} = V_{\text{u}}F_{\text{t}}C_{\text{d}}F_{\text{t}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
= 16.59 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
V_{\text{sliding}} = V_{\text{u}}F_{\text{t}}C_{\text{d}}F_{\text{t}} = 16.59 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
= 16.59 \cdot \frac{\text{kip}}{\text{ft}}
$$

LRFD 10.6.3.4

Maximum and minimum bearing pressure

$$
q_{max} := \frac{F_{VFLC1StrlMin}}{B_{foothing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{foothing}}\right) = 4.27 \cdot ksf
$$

\n
$$
q_{min} := \frac{F_{VFLC1StrlMin}}{B_{foothing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{foothing}}\right) = 0.62 \cdot ksf
$$

\n
$$
B_{Su} := B_{foothing} \cdot \frac{q_{max} - 2 \cdot S_u}{q_{max} - q_{min}} = 5.93 \text{ ft}
$$

\n
$$
V_{resistance} := \phi_{\tau} \cdot \left[B_{Su} \cdot S_u + \frac{1}{2} \cdot \left(B_{foothing} - B_{Su}\right)\left(\frac{1}{2}q_{min} + S_u\right)\right]
$$

\n
$$
V_{resistance} = 16.09 \cdot \frac{kip}{ft}
$$

\nCheck := if $(V_{resistance} > V_{sliding}, "OK", "Not OK") = "Not OK"$

Width of the footing with a normal stress greater than $2S_u$

Sliding resistance (capacity)

 $Check if V_{resistance} > V_{sliding}$

Therefore, the sliding resistance is inadequate. Since MDOT typically does not use keyways, consider widening the footing to enhance the sliding resistance. When the footing width is too excessive and uneconomical, consider using EPS as a backfill material.

Load Case IV

Factored shear force parallel to the Factored shear force parallel to the

transverse axis of the footing $V_{\text{uFtLC4StrI}} = 19.85 \cdot \frac{kip}{ft}$

Factored sliding force (demand)

Minimum vertical load

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Width of the footing with a normal stress greater than $2S_{\text{u}}$

Factored sliding force (demand)
\n
$$
V_{\text{sliding}} := V_{\text{uFtL} \text{C4Str1}} - 1.75 P_{\text{LSFooting}} = 16.73 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{Minimum vertical load}
$$
\n
$$
F_{\text{VFtL} \text{C4Str1Min_nOLS}} = 46.72 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{Ferm Step 2.6, sliding}
$$
\n
$$
\text{Eccentricity in the footing width direction}
$$
\n
$$
e_{\text{B}} := \frac{M_{\text{uFtL} \text{C4Str1Min_nOLS}}}{F_{\text{VFtL} \text{C4Str1Min_nOLS}}} = 2.5 \cdot \text{ft}
$$
\n
$$
q_{\text{max}} := \frac{F_{\text{VFtL} \text{C4Str1Min_nOLS}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}} \right) = 5.17 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFtL} \text{C4Str1Min_nOLS}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}} \right) = 0.33 \cdot \text{ksf}
$$
\n
$$
B_{\text{Su}} := B_{\text{footing}} \cdot \frac{q_{\text{max}} - 2 \cdot S_{\text{u}}}{q_{\text{max}} - q_{\text{min}}} = 7.62 \text{ ft}
$$
\n
$$
\text{Sliding resistance (capacity)}
$$
\n
$$
V_{\text{resistance}} := \phi_{\text{T}} \left[B_{\text{Su}} \cdot S_{\text{u}} + \frac{1}{2} \cdot \left(B_{\text{footing}} - B_{\text{Su}} \right) \left(\frac{1}{2} q_{\text{min}} + S_{\text{u}} \right) \right]
$$

 $V_{\text{resistance}} = 16.34 \cdot \frac{\text{kip}}{\text{ft}}$

Check if $V_{resistance} > V_{sliding}$ Check $V = \text{if } (V_{resistance} > V_{sliding}, "OK", "Not OK") = "Not OK"$

Therefore, the sliding resistance is inadequate. Since MDOT typically does not use keyways, consider widening the footing to enhance the sliding resistance. When the footing width is too excessive and uneconomical, consider using EPS as a backfill material.

Section 3 Abutment with Spread Footing and EPS Backfill

Step 3.1 Preliminary Abutment Dimensions

Description

This step presents the selected preliminary abutment dimensions.

The design criteria, bridge information, material properties, reinforcing steel cover requirements, soil types and properties, along with superstructure loads in this section are taken from Section 2.

 \blacktriangleright

This section presents the design of a full-depth reinforced concrete cantilever abutment with expanded polystyrene (EPS) blocks as the lightweight backfill material.

Geofoam made with EPS is effective at reducing lateral forces or settlement potential for bridge abutments (MDOT Geotechnical Manual 2019). The selection of a specific Geofoam grade depends on the project needs. A typical Geofoam embankment consists of the foundation soils, the Geofoam fill, and a load dissipater slab designed to transfer loads to the Geofoam.

Design guidelines for Geofoam embankments are provided in the National Cooperative Highway Research Program (NCHRP) web document 65, titled *Geofoam Applications in the Design and Construction of Highway Embankments (Stark et al., 2004).* It is cited as **NCHRP w65** in this design example.

The designer should select the preliminary dimensions based on state-specific standards and past experience. The following figure shows the abutment geometry and dimensional variables:

If the fill above the EPS blocks is greater than 8 ft, the compressive strength of the blocks needs to be checked.

According to the MDOT Geotechnical Manual (2019), EPS blocks should not be used where the water table could rise and make geoform unstable due to buoyant forces. The structural engineer and the geotechnical engineer need to work together and check EPS stability for a 100-year flood.

Step 3.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of the future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$
DC_{Sup} := \frac{2 \cdot R_{DCEx} + (N_{beams} - 2) \cdot R_{DCln}}{L_{abut}} = 5.658 \cdot \frac{kip}{ft}
$$

\n
$$
DW_{Sup} := \frac{2 \cdot R_{DWEx} + (N_{beams} - 2) \cdot R_{DWIn}}{L_{abut}} = 0.886 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{backwall} := h_{backwall} \cdot t_{backwall} \cdot W_c = 0.956 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{wall} := h_{wall} \cdot t_{wall} \cdot W_c = 8.332 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{foothing} := B_{foothing} \cdot t_{foothing} \cdot W_c = 6.075 \cdot \frac{kip}{ft}
$$

Step 3.3 Application of Live Load

Description

 \blacktriangleright

Please refer to Step 2.3. The same loads are applied following the procedures described in Step 2.3.

94

Step 3.4 Application of Other Loads

Description

This step typically includes the calculation of braking force, wind load, earth load, and temperature load.

The calculation of "Other Loads", except the earth load, is identical to Step 2.4. Since EPS blocks are used as the backfill and a different spread footing width is selected, the calculation of the earth load is different. Therefore, this step only presents the earth load calculation. Please refer to Step 2.4 for the rest of the calculations.

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the information received from the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. When possible, the hydrostatic pressure should be avoided at abutments and retaining walls using an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral pressure and the resultant force due to earth pressure are calculated.

The lateral component of the earth load on the abutment consists of seven parts as listed below and shown in the following figure:

EH 1: the lateral pressure from the soil located above the EPS blocks

EH 2: the lateral pressure due to the vertical load at the top of the EPS blocks

EH 3: the lateral pressure from the soil located behind the EPS blocks

EH 4: the lateral pressure from the soil located below the EPS blocks and above the top of the footing

EH 5: the lateral pressure due to the vertical load at the bottom of the EPS blocks

EH 6: the lateral pressure due to the vertical load at the top of the footing

EH 7: the lateral pressure from the soil located along the depth (thickness) of the footing.

Backwall

Lateral earth pressure at the base $p_{bw} := k_a \cdot \gamma_s \cdot h_{backwall} = 0.153 \cdot \text{ksf}$ **LRFD Eq. 3.11.5.1-1**

Lateral load
$$
P_{\text{EHBackwall}} := \frac{1}{2} \cdot p_{\text{bw}} \cdot h_{\text{backwall}} = 0.325 \cdot \frac{kip}{ft}
$$

Abutment Wall

The calculation of lateral loads on the abutment wall with EPS blocks as the backfill follows the procedure outlined in the NCHRP web document 65, titled *Geoform Applications in the Design and Construction of Highway Embankments* by Stark et al. (2004).

Height of backfill soil above the EPS blocks

Lateral earth pressure at the $\frac{p}{p}$ top of EPS blocks p

Lateral load from the soil located α above the EPS blocks α

EH 2 ·

Lateral earth pressure due to the vertical $\frac{1}{2}$ boad at the top of the EPS blocks p

Lateral load due to the vertical load at the top of the EPS blocks

EH 3:

Lateral earth pressure from the soil located behind the EPS blocks

Lateral load from the soil located behind the EPS blocks

EH 4:

Lateral earth pressure from the soil located below the EPS blocks and above the top of the footing

Lateral load from the soil located below the EPS blocks and above the top of the footing

EH 5:

Lateral earth pressure due to the vertical load at the bottom of the EPS blocks

Total resultant lateral load at the base of the wall

 $h_{\text{SoilAbove}} = 7.79 \text{ ft}$

EH 1: **LRFD Eq. 3.11.5.1-1**

AboveEPS
$$
= k_a \gamma_s \cdot h_{\text{SoilAboveEPS}} = 0.28 \cdot \text{ksf}
$$

$$
P_{\text{EH1}} \coloneqq \frac{1}{2} \cdot p_{\text{AboveEPS}} \cdot h_{\text{SoilAboveEPS}} = 1.092 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
PVEPS := \frac{1}{10} \gamma_{\rm s} \cdot \text{h}_{\rm SoilAboveEPS} = 0.093 \cdot \text{ksf} \qquad \text{NCHRP w65}
$$

$$
P_{EH2} := p_{VEPS} \cdot h_{EPS} = 1.122 \cdot \frac{kip}{ft}
$$

$$
P\text{SoilBehind} := k_{EPS} \gamma_{s} \cdot h_{EPS} = 0.045 \cdot \text{ksf}
$$
\n
$$
P_{EH3} := \frac{1}{2} \cdot p\text{SoilBehind} \cdot h_{EPS} = 0.268 \cdot \frac{\text{kip}}{\text{ft}}
$$

 $p_{SoilBelowEPS} := k_a \gamma_s h_{SoilBelowEPS} = 0.072$ ksf

$$
P_{EH4} := \frac{1}{2} \cdot p_{SoilBelow EPS} \cdot h_{SoilBelow EPS} = 0.072 \cdot \frac{kip}{ft}
$$

 $PWS oil BelowEPS = k_a (\gamma_s \cdot h_{SoilAboveEPS} + \gamma_{EPS} \cdot h_{EPS}) = 0.288 \cdot ksf$

\n Lateral load due to the vertical load
\n at the bottom of the EPS blocks\n
$$
P_{EH5} := \frac{P_{V}}{P_{H5}} \cdot \frac{P_{V}}{P_{H5}} \cdot \frac{P_{V}}{P_{H5}} = 0.575 \cdot \frac{kip}{ft}
$$
\n

\n\n Total resultant lateral load at
\n
$$
P_{E} = \frac{P_{H}}{P_{H5}} + \frac{P_{H}}{P_{H5}} + \frac{P_{H}}{P_{H5}} = 3.129 \cdot \frac{kip}{ft}
$$
\n

Total moment of the lateral earth load at the base of the wall

$$
M_{EHWall} := P_{EH1} \cdot \left(\frac{1}{3} h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS}\right) + P_{EH2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoilBelowEPS}\right) \cdots
$$

$$
+ P_{EH3} \cdot \left(\frac{1}{3} \cdot h_{EPS} + h_{SoilBelowEPS}\right) + P_{EH4} \cdot \frac{1}{3} \cdot h_{SoilBelowEPS} \cdots
$$

$$
+ P_{EH5} \cdot \frac{1}{2} \cdot h_{SoilBelowEPS}
$$

$$
M_{EHWall} = 29.331 \cdot \frac{kip \cdot ft}{ft}
$$

Footing

The lateral earth load on the backwall, abutment wall, and footing are defined using 7 profiles. The forces acting on the abutment wall from profiles 1 to 5 remain unchanged. Hence, the calculation of forces from the earth load profiles 6 and 7 is described below.

EH 6:

Lateral earth pressure due to the vertical load at the footing top surface elevation

Lateral earth load due to the vertical load at the footing top surface elevation

EH 7:

Lateral earth pressure from the soil located along the depth of the footing

Lateral earth load from the soil located along the depth of the footing

1 ² pSoilSideFt ^t footing 0.162 kip ft Total lateral earth load PEHFooting PEHWall PEH6 PEH7 4.37 kip ft

+ γ EPS $^{\text{th}}$ EPS + γ_s hSoilBelowEPS

 $= k_a / \gamma_s h_{\text{SoilAbove}FPS}$... $= 0.36$ ksf

 \setminus $\overline{}$ J

 $\begin{cases} \gamma_{s} \cdot h_{\text{SoilAboveEPS}} & \cdots \\ + \gamma_{\text{The other}} + \gamma \cdot h_{\text{S}} \end{cases}$

PSoilAboveFt $:= k_a / \gamma_s \cdot h_{\text{SoilAboveEPS}}$

 \setminus

 $P_{EH6} := p_{SoilAboveFt}(t_{footing}) = 1.079 \cdot \frac{kip}{ft}$ $=$ PSoilAboveFt $(t_{\text{footing}}) = 1.079$

 f_{0} , f_{0} , f_{0} f_{0} f_{0} , f_{0}

Total moment of the lateral earth load at the base of the footing

$$
M_{\text{EHFooting}} := P_{\text{EH1}} \cdot \left(\frac{1}{3} h_{\text{Soi1AboveEPS}} + h_{\text{EPS}} + h_{\text{Soi1BelowEPS}} + t_{\text{footing}} \right) \cdots
$$

+
$$
P_{\text{EH2}} \cdot \left(\frac{1}{2} \cdot h_{\text{EPS}} + h_{\text{Soi1BelowEPS}} + t_{\text{footing}} \right) + P_{\text{EH3}} \cdot \left(\frac{1}{3} \cdot h_{\text{EPS}} + h_{\text{Soi1BelowEPS}} + t_{\text{footing}} \right) \cdots
$$

+
$$
P_{\text{EH4}} \cdot \left(\frac{1}{3} \cdot h_{\text{Soi1BelowEPS}} + t_{\text{footing}} \right) + P_{\text{EH5}} \cdot \left(\frac{1}{2} \cdot h_{\text{Soi1BelowEPS}} + t_{\text{footing}} \right) \cdots
$$

+
$$
P_{\text{EH6}} \cdot \frac{1}{2} \cdot \left(t_{\text{footing}} \right) + P_{\text{EH7}} \cdot \frac{1}{3} \cdot \left(t_{\text{footing}} \right)
$$

$$
M_{\text{EHFooting}} = 40.499 \cdot \frac{kip \cdot ft}{ft}
$$

Vertical Earth Load on the Footing

Back side (heel) $EV_{earthBk} = \gamma_s \cdot l_{heel} (h_{Soi1AboveEPS} + h_{Soi1BelowEPS}) + \gamma_{EPS} \cdot l_{heel} (h_{EPS} + h_{EPS})$

$$
EV_{earthBk} = 4.795 \cdot \frac{kip}{ft}
$$

Front side (toe) E^V

$$
V_{earthFt} := \gamma_{s'} l_{\text{toe}} \left(h_{\text{toeDepth}} - t_{\text{foothing}} \right) = 3.04 \cdot \frac{\text{kip}}{\text{ft}}
$$

LRFD 3.11.6.4

Live Load Surcharge

A surcharge is applied to account for a vehicular live load acting on the backfill surface within a distance equal to one-half the wall height behind the back face of the wall.

The lateral component of the live load surcharge on the abutment wall consists of three parts, as shown in the previous figure:

LS 1: the lateral pressure across the soil located above the EPS blocks

LS 2: the lateral pressure across the EPS blocks due to the soil located above the blocks

LS 3: the lateral pressure across the soil located below the EPS blocks.

Total moment at the base of the wall due to the lateral component of the live load surcharge

$$
M_{LSWall} := P_{LSWall1} \cdot \left(\frac{1}{2}h_{SoiIAboveEPS} + h_{EPS} + h_{SoiIBelowEPS}\right) \cdots
$$

$$
+ P_{LSWall2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoiIBelowEPS}\right) + P_{LSWall3} \cdot \left(\frac{1}{2}h_{SoiIBelowEPS}\right)
$$

$$
M_{LSWall} = 12.485 \cdot \frac{kip \cdot ft}{ft}
$$

Footing

The lateral component of the live load surcharge on the footing consists of three parts. The contribution of LS 1 and LS 2 is the same as the abutment wall. The contribution of LS 3 needs to be considered up to the bottom of the footing.

\nLateral surveillance load from the profile LS 1
\nLateral surveillance load
\nfrom the profile LS 2
\nLateral surface load
\nLateral surface load from
\nthe profile LS 3
\nTotal lateral load due to live
\nload surveillance
\n

\n\n
$$
P_{LSF} = \frac{1}{10} \gamma_s \cdot h_{eq} \cdot h_{eps} = 0.288 \cdot \frac{kip}{ft}
$$
\n
$$
P_{LSF} = \frac{1}{10} \gamma_s \cdot h_{eq} \cdot h_{eps} = 0.288 \cdot \frac{kip}{ft}
$$
\n
$$
P_{LSF} = \frac{1}{10} \gamma_s \cdot h_{eq} \cdot h_{eps} = 0.288 \cdot \frac{kip}{ft}
$$
\n
$$
P_{LSF} = \frac{1}{10} \gamma_s \cdot h_{eq} \cdot h_{eps} = 0.288 \cdot \frac{kip}{ft}
$$
\n
$$
P_{LSF} = \frac{1}{10} \cdot \
$$

Total moment at the base of the footing due to the lateral component of the live load surcharge

$$
M_{LSFoting} := P_{LSFoting1} \cdot \left(\frac{1}{2}h_{SoiIAboveEPS} + h_{EPS} + h_{SoiIBelowEPS} + t_{footing}\right) ...
$$

+
$$
P_{LSFoting2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoiIBelowEPS} + t_{footing}\right) ...
$$

+
$$
P_{LSFoting3} \cdot \frac{1}{2} \cdot \left(h_{SoiIBelowEPS} + t_{footing}\right)
$$

$$
M_{LSFoting} = 15.788 \cdot \frac{kip \cdot ft}{ft}
$$

Vertical load

$$
V_{LSFoting} := \gamma_s \cdot l_{heel} \cdot h_{eq} = 0.96 \cdot \frac{kip}{ft}
$$

 $\overline{\mathbf{E}}$

Step 3.5 Combined Load Effects

Description

This step presents the procedure for combining all load effects and calculating total factored forces and moments acting at the base of the abutment wall and footing. The total factored forces and moments at the base of the backwall are similar to those ones in Step 2.5.

\blacksquare

Page Contents

102 Forces and Moments at the Base of the Abutment Wall

106 Forces and Moments at the Base of the Footing

Forces and Moments at the Base of the Abutment Wall

Load Cases I, III, and IV are considered. More specifically, superstructure dead load, superstructure live load, and uniform temperature induced loads are considered in addition to the dead load of the backwall, dead load of the abutment wall, lateral earth pressure, and lateral surcharge pressure.

Strength I

Strength I = $1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU$

Load Case I

Factored vertical force at the base of the wall FVWallLC1StrI 1.25 DCbackwall DCwall 11.61 kip ft Factored shear force parallel to the transverse axis of the abutment wall VuWallLC1StrI 1.5 PEHWall 4.693 kip ft **LRFD 3.4.1**

The backwall weight reduces the critical moment at the base of the abutment wall. This requires the use of a minimum load factor of 0.9 for DC instead of the factor 1.25 in the Strength I combination.

This is the same for the moment calculated about the longitudinal axis of the abutment wall for all the load cases and limit states.

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC1StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + 1.5 \cdot M_{EHWall} = 43.28 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force at the base of the wall

$$
F_{\text{VWallLC3StrI}} := 1.25 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} \right) + 1.5 \text{DW}_{\text{Sup}} + 1.75 \text{R}_{\text{LLWallMax}}
$$
\n
$$
F_{\text{VWallLC3StrI}} = 29.861 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
\text{Factored shear force parallel to the}
$$
\n
$$
V_{\text{uWallLC3StrI}} := 1.5 \cdot P_{\text{EHWall}} = 4.693 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{\text{uWallLC3StrI}} := 0.9 \cdot \text{DC}_{\text{backwall}} \cdot \frac{(t_{\text{backwall}} - t_{\text{wall}})}{2} \dots
$$

$$
+ \left(1.25 \cdot \text{DC}_{\text{Sup}} + 1.5 \cdot \text{DW}_{\text{Sup}} + 1.75 \cdot \text{RLLWallMax}\right) \cdot \left(t_{\text{brtowall}} - \frac{t_{\text{wall}}}{2}\right) \dots
$$

$$
+ 1.5 \cdot \text{M}_{\text{EHWall}} \times \text{M}_{\text{uWallLC3StrI}} = 56.969 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case IV

Factored vertical force at the base of the wall

$$
F_{\text{VWallLC4StrI}} \coloneqq 1.25 \cdot \left(DC_{\text{Sup}} + DC_{\text{backwall}} + DC_{\text{wall}} \right) + 1.5DW_{\text{Sup}} = 20.012 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the abutment wall

$$
V_{uWallLC4StrI} := 1.5 \cdot P_{EHWall} + 1.75 \cdot P_{LSWall} + 0.5 \text{TU} = 6.57 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC4StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + (1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup}) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) ... + 1.5 \cdot M_{EHWall} + 1.75 \cdot M_{LSWall} + 0.5 \cdot TU \cdot h_{wall}
$$

$$
M_{\text{uWallLC4StrI}} = 73.864 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Load Case I

Factored vertical force at the base of the wall

\nFactored shear force parallel to the transverse axis of the abundant wall

\n
$$
V_{\text{uWallLC1SerI}} := DC_{\text{backwall}} + DC_{\text{wall}} = 9.288 \cdot \frac{\text{kip}}{\text{ft}}
$$
\n
$$
V_{\text{uWallLC1SerI}} := P_{\text{EHWall}} = 3.129 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC1SerI} := DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + M_{EHWall}
$$

$$
M_{uWallLC1SerI} = 28.535 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force at the base of the wall

$$
F_{\text{VWallLC3SerI}} := \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} \right) + \text{DW}_{\text{Sup}} + R_{\text{LLWallMax}}
$$

$$
F_{\text{VWallLC3SerI}} = 21.46 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the abutment wall

$$
V_{\text{uWallLC3SerI}} := P_{\text{EHWall}} = 3.129 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC3SerI} := DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots
$$

$$
+ \left(DC_{Sup} + DW_{Sup} + R_{LLWallMax}\right) \cdot \left(1_{brtowall} - \frac{t_{wall}}{2}\right) \dots
$$

$$
+ M_{EHWall}
$$

$$
M_{\text{uWallLC3SerI}} = 37.664 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case IV

Factored vertical force at the base of the wall

$$
FvWallLC4SerI := (DCSup + DCbackwall + DCwall) + 1.0DWSup
$$

$$
FvWallLC4SerI = 15.832 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the
transverse axis of the abundant wall\n
$$
V_{\text{uWallLC4SerI}} := P_{\text{EHWall}} + P_{\text{LSWall}} + TU = 4.399 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the abutment wall

$$
M_{uWallLC4SerI} := DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + (1.0 \cdot DC_{Sup} + 1.0 \cdot DW_{Sup}) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2} \right) ... + 1.0 \cdot M_{EHWall} + 1.0 \cdot M_{LSWall} + 1.0 \cdot TU \cdot h_{wall}
$$

$$
M_{uWallLC4SerI} = 50.795 \cdot \frac{kip \cdot ft}{ft}
$$

Summary of the Forces and Moments at the Base of the Abutment Wall

Factored vertical force, F_{VWall} (kip/ft)

Factored moment about the longitudinal axis of the abutment wall, M_{u Wall (kip[.]ft/ft)

The forces and moments presented in the above tables are used for the structural design presented in Step 3.8. As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the abutment wall after excluding the lateral earth load within the EPS backfill zone. This summary is presented for informational purposes only.

Factored vertical force, F_{VWatt} (kip/ft)

Factored shear force parallel to the transverse axis of the abutment wall, V_{uWall} (kip/ft)

Factored moment about the longitudinal axis of the abutment wall, M_{uWall} (kip ft/ft)

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered. In addition to all the loads considered for the abutment wall, weight of soil (earth load) on the footing toe and heel along with live load surcharge on the heel are considered.

LRFD 3.6.2.1

The dynamic load allowance is excluded from the live load for foundation components located entirely below ground level.

Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU

Load Case I

Factored vertical force at the base of the footing

$$
F_{VFLC1StrI} \coloneqq 1.25 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 29.781 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the footing\n
$$
V_{\text{uFtLC1StrI}} \coloneqq 1.5 \cdot P_{\text{EHFooting}} = 6.555 \cdot \frac{\text{kip}}{\text{ft}}
$$

The vertical earth load of the backfill soil reduces the critical moment about the footing longitudinal axis. This requires the use of a minimum load factor of 1.0 for EV instead of the factor 1.35 in the Strength I combination.

LRFD 3.4.1

The same is applied for the moment calculated about the footing's longitudinal axis for all the load cases and limit states.

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLCIStrI}} := 1.25 \cdot DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot M_{\text{EHFooting}} + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.35 \cdot EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{to}}}{2} \right)
$$

$$
M_{\text{uFtLCIStrI}} = 38.136 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case III

Factored vertical force at the base of the footing

 $F_{\text{VFitLC3StrI}} \coloneqq 1.25 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{foothing}} \right) + 1.5\text{DW}_{\text{Sup}} + 1.75\text{R}_{\text{LLFoothingMax}}$ $+1.35\cdot(EV_{earthBk} + EV_{earthFt})$ $\mu = 1.25 \cdot (DC_{S11D} + DC_{\text{backwall}} + DC_{\text{wall}} + DC_{\text{foothing}}) + 1.5DW_{S1D} + 1.75R_{\text{I}}$ Footing May ...

 $:= 1.5 \cdot P_{\text{FHEooting}} = 6.555$

$$
F_{\text{VFtLC3StrI}} = 47.733 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the Factored shear force parallel to the
 $V_{\text{uFtLC3StrI}} \coloneqq 1.5 \cdot P_{\text{EHFooting}} = 6.555 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3StrI}} \coloneqq 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(1.25 \cdot DC_{\text{Sup}} + 1.5 \cdot DW_{\text{Sup}} + 1.75 \cdot R_{\text{LL}FoothingMax} \right) \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot M_{\text{EHFoothing}} + 1.0 \cdot EV_{\text{earthBk}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.35 \cdot EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right)
$$

$$
M_{\text{uFtLC3StrI}} = 30.656 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force at the base of the footing

$$
F_{VFLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing}) + 1.5DW_{Sup} ... + 1.35 \cdot (EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFooting}
$$

$$
F_{\text{VFtLC4StrI}} = 39.863 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the

Factored shear force parallel to the $V_{\text{uFtLC4StrI}} = 1.5 \cdot P_{\text{EHFooting}} + 1.75 \cdot P_{\text{LSFooting}} + 0.5 \text{TU} = 8.809 \cdot \frac{\text{kip}}{\text{ft}}$ $= 1.5 \cdot P_{\text{FHEooting}} + 1.75 \cdot P_{\text{I SEooting}} + 0.5 \text{TU} = 8.809$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC4StrI}} \coloneqq 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(1.25 \cdot DC_{\text{Sup}} + 1.5 \cdot DW_{\text{Sup}} \right) \cdot \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot M_{\text{EHFooting}} + 1.75 M_{\text{LSFooting}} + 1.75 V_{\text{LSFooting}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.0 \cdot EV_{\text{earthBk}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.35 \cdot EV_{\text{earthFt}} \cdot \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right) \dots + 0.5 \cdot TU \cdot \left(h_{\text{wall}} + t_{\text{footing}} \right)
$$
\n
$$
M_{\text{uFtLC4StrI}} = 57.133 \cdot \frac{\text{kip} \cdot ft}{\text{ft}}
$$

Service I

Service $I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU$

Load Case I

Factored vertical force at the base of the footing

$$
F_{VFLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 23.198 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the transverse axis of the footing\n
$$
V_{\text{uFtLC1SerI}} := P_{\text{EHFooting}} = 4.37 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLCISerI}} \coloneqq DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots
$$

$$
+ M_{\text{EHFooting}} + EV_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{to}}}{2} \right)
$$

$$
M_{\text{uFtLCISerI}} = 16.982 \cdot \frac{kip \cdot ft}{ft}
$$
Load Case III

Factored vertical force at the base of the footing

$$
F_{VFLC3SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFootingMax} ...
$$

+ $(EV_{earthFt} + EV_{earthBk})$

$$
F_{VFLC3SerI} = 35.199 \cdot \frac{kip}{ft}
$$

shear force parallel to the

$$
V_{VFLC3SerI} := P_{EUEooting} = 4.37 \cdot \frac{kip}{t}
$$

Factored s¹ transverse axis of the footing

$$
V_{\text{uFtLC3SerI}} := P_{\text{EHFooting}} = 4.37 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3SerI}} := DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) + DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) \dots + \left(DC_{\text{Sup}} + DW_{\text{Sup}} + R_{\text{LLFootingMax}} \right) \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + M_{\text{EHFooting}} + EV_{\text{earthBk}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right)
$$

$$
M_{\text{uFtLC3SerI}} = 11.982 \cdot \frac{\text{kip·ft}}{\text{ft}}
$$

Load Case IV

Factored vertical force at the
\nbase of the footing\n
$$
F_{VFLC4SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing} + DW_{Sup} ...
$$
\n
$$
+ (EV_{earthFt} + EV_{earthBk}) + V_{LSFoothing}
$$
\n
$$
F_{VFLC4SerI} = 30.702 \cdot \frac{kip}{ft}
$$

 $= P_{\text{FHF}ooting} + P_{\text{I SF}ooting} + TU = 5.856$

Factored shear force parallel to the transverse axis of the footing Factored shear force parallel to the
transverse axis of the footing $V_{\text{uFtLC4SerI}} := P_{\text{EHF} \text{ooting}} + P_{\text{LSF} \text{ooting}} + TU = 5.856 \cdot \frac{\text{kip}}{\text{ft}}$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC4SerI}} \coloneqq DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots
$$

$$
+ \left(DC_{\text{Sup}} + DW_{\text{Sup}} \right) \cdot \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) + M_{\text{EHFooting}} \dots
$$

$$
+ EV_{\text{earthBk}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right) \dots
$$

$$
+ V_{\text{LSFooting}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + M_{\text{LSFooting}} + TU \cdot \left(h_{\text{wall}} + t_{\text{footing}} \right)
$$

$$
M_{\text{uFtLC4SerI}} = 31.183 \cdot \frac{kip \cdot ft}{ft}
$$

Summary of Forces and Moments at the Base of the Footing

Factored shear force parallel to the transverse axis Factored vertical force, F_{VFt} (kip/ft) F_{VFt} (footing, V_{uFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

 The forces and moments presented in the tables above are used for the designs presented in Step 3.6. and 3.9. As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the abutment wall after excluding the lateral earth load within the EPS backfill zone. This summary is presented for informational purposes only.

Factored vertical force, F_{VFt} (kip/ft)

Factored shear force parallel to the transverse axis of the footing, V_{uFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/ft)

 $\,{}^+$

Step 3.6 Geotechnical Design of the Footing

Description

This step presents the geotechnical design of a spread footing considering the following strength and serviceability limit states:

1. bearing resistance – strength limit state

2. settlement – service limit state

3. sliding resistance – strength limit state

4. load eccentricity (overturning) – strength limit state.

The evaluation of structural resistance of the footing (internal stability) is presented later in Step 3.9.

Page Contents

- **112 Summary of Forces and Moments at the Base of the Footing**
- **112 Bearing Resistance Check**
- **116 Settlement Check**
- **116 Sliding Resistance Check**
- **118 Eccentric Load Limitation (Overturning) Check**

LRFD 10.6.1.1

Summary of Forces and Moments at the Base of the Footing

As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the footing after including the lateral earth load within the EPS backfill zone. The forces and moments presented in these tables are used for the designs presented in Step 3.6. and 3.9.

Factored shear force parallel to the transverse axis Factored vertical force, F_{VFt} (kip/ft) F_{VFt} (kip/ft) of the footing, V_{VFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Bearing Resistance Check

For eccentrically loaded footings, the use of a reduced effective area is allowed for bearing resistance or settlement calculation. The point of load application shall be at the centroid of the reduced area.

Note: As a practice, the average pressure and the values at the toe and heel under different load cases and limit states are provided to the MDOT Geotechnical Services Section for verification.

This example presents the LRFD and MDOT methods.

Load Case I, Strength I

LRFD method

A reduced effective footing width is used for bearing resistance and settlement design. **LRFD 10.6.1.3**

LRFD 10.6.1.3

112

Footing bearing pressure qbearing_LC1

MDOT method

Average bearing pressure quality of the contract of the contra

Toe bearing pressure quality of α

Heel bearing pressure quality of quality quality of quality qu

Load Case III, Strength I

Factored vertical force

Eccentricity in the footing width direction

LRFD method

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case IV, Strength I

Factored vertical force

Factored moment about footing
 $M_{\text{uFtLC4StrI}} = 57.133 \cdot \frac{\text{kip·ft}}{\text{ft}}$

Eccentricity in the footing width direction

$$
bearing_LC1 := \frac{F_V F t LC1StrI}{B_{eff}} = 2.722 \cdot ksf
$$

$$
q_{avgLC1} := \frac{F_{VFLC1StrI}}{B_{footing}} = 2.206 \cdot \text{ksf}
$$
\n
$$
q_{toeLC1} := \frac{F_{VFLC1StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.461 \cdot \text{ksf}
$$

$$
heelLC1 := \frac{F_V FtLC1StrI}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.95 \cdot ksf
$$

Factored vertical force
\nFactored moment about footing
\nlongitudinal axis
\nEccentricity in the footing width direction
\n
$$
\text{E}_{\text{B}} = \frac{M_{\text{uFtLC3StrI}}}{F_{\text{vFtLC3StrI}}} = 0.642 \text{ ft}
$$

Effective footing width B_{eff} = $B_{foothing} - 2 \cdot e_B = 12.216 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure $q_{\text{bearing_LC3}} :=$ FVFtLC3StrI B_{eff} $\frac{3.908 \cdot \text{ksf}}{2} = 3.908 \cdot \text{ksf}$

$$
q_{avgLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} = 3.536 \cdot \text{ksf}
$$
\n
$$
q_{toeLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.545 \cdot \text{ksf}
$$
\n
$$
q_{heelLC3} := \frac{F_{VFLC3StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 2.527 \cdot \text{ksf}
$$

$$
F_{\text{VFtLC4StrI}} = 39.863 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
M_{\text{uFtLC4StrI}} = 57.133 \cdot \frac{\text{kip·ft}}{\text{ft}}
$$

$$
e_B := \frac{M_u F t L C 4 S t r I}{F_{V F t L C 4 S t r I}} = 1.433 ft
$$

LRFD method

MDOT method

Average bearing pressure q_a

Toe bearing pressure quality of α

Heel bearing pressure quality of the leading of the leadi

Load Case I, Service I

Factored vertical force

Eccentricity in the footing width direction

LRFD method

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case III, Service I

Factored vertical force

Eccentricity in the footing width direction

Effective footing width B_{eff} = $B_{foothing} - 2 \cdot e_B = 10.634 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Bearing pressure qbearing LC4 F_{VFtLC4StrI} B_{eff} $\frac{3.749 \text{ kfs}}{2}$ = 3.749 ksf

$$
avgLC4 \stackrel{\text{?}}{=} \frac{\text{F}_{VFLC4StrI}}{\text{B}_{\text{footing}}} = 2.953 \cdot \text{ksf}
$$

$$
H_{\text{toeLC4}} := \frac{F_{\text{VFtLC4StrI}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 4.834 \cdot \text{ksf}
$$
\n
$$
H_{\text{heelLC4}} := \frac{F_{\text{VFtLC4StrI}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 1.072 \cdot \text{ksf}
$$

Factored vertical force
\nFactored moment about footing
\nlongitudinal axis
\nEccentricity in the footing width direction
\n
$$
\epsilon_{\text{B}} := \frac{M_{\text{uFtLC1SerI}}}{F_{\text{vFtLC1SerI}}} = 0.732 \text{ ft}
$$

Effective footing width B_{eff} = $B_{footing} - 2 \cdot e_B = 12.036 \text{ ft}$ **LRFD Eq. 10.6.1.3-1** Footing bearing pressure qbearing LC1SerI FVFtLC1SerI B_{eff} $:= \frac{1.927 \cdot \text{ksf}}{2} = 1.927 \cdot \text{ksf}$

$$
q_{avgLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}}
$$

\n
$$
q_{toeLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 2.277 \cdot \text{ksf}
$$

\n
$$
q_{heelLC1SerI} := \frac{F_{VFLC1SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.159 \cdot \text{ksf}
$$

Factored vertical force
\n
$$
F_{VFLLC3SerI} = 35.199 \cdot \frac{kip}{ft}
$$
\nFactored moment about footing
\nlongitudinal axis
\nEccentricity in the footing width direction
\n
$$
e_B := \frac{M_{uFtLC3SerI}}{F_{VFLC3SerI}} = 0.34 \text{ ft}
$$

LRFD method

-
- Bearing pressure

MDOT method

Average bearing pressure q_{av}

Toe bearing pressure

Heel bearing pressure

Load Case IV, Service I

Factored vertical force

Eccentricity in the footing width direction

LRFD method

Bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Effective footing width

\n
$$
B_{eff} := B_{footing} - 2 \cdot e_B = 12.819 \text{ ft} \qquad \text{LRFD Eq. 10.6.1.3-1}
$$
\nBearing pressure

\n
$$
q_{\text{bearing}_\text{LC3SerI}} := \frac{F_{\text{VFit}_\text{C3SerI}}}{B_{\text{eff}}} = 2.746 \cdot \text{ksf}
$$

$$
VgLC3SerI := \frac{FVFLC3SerI}{B_{footing}} = 2.607 \text{ ksf}
$$

$$
FVFLC3SerI \begin{pmatrix} 6 \text{ e} \\ 9 \text{ e} \end{pmatrix} = 2.07
$$

$$
q_{\text{toeLC3SerI}} := \frac{4 \text{VFLC3SerI}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \text{°C}}{B_{\text{footing}}}\right) = 3.002 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC3SerI}} := \frac{F_{\text{VFLC3SerI}}}{B_{\text{footing}}}
$$
\n
$$
\left(1 - \frac{6 \cdot \text{°B}}{B_{\text{footing}}}\right) = 2.213 \cdot \text{ksf}
$$

Factored vertical force
\nFactored moment about footing
\nlongitudinal axis
\nEccentricity in the footing width direction
\n
$$
e_B := \frac{M_{\text{uFtLC4SerI}}}{F_{\text{vFtLC4SerI}}} = 1.016 \text{ ft}
$$

Effective footing width B_{eff} = $B_{foothing} - 2 \cdot e_B = 11.469 \text{ ft}$ **LRFD Eq. 10.6.1.3-1**

$$
q_{\text{bearing_LC4SerI}} := \frac{F_{\text{VFtLC4SerI}}}{B_{\text{eff}}} = 2.677 \cdot \text{ksf}
$$

$$
q_{avgLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} = 2.274 \cdot \text{ksf}
$$
\n
$$
q_{toeLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.301 \cdot \text{ksf}
$$
\n
$$
q_{heelLC4SerI} := \frac{F_{VFLC4SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.248 \cdot \text{ksf}
$$

Summary

LRFD method

The controlling bearing pressure under strength limit states

 $q_b := max (q_{\text{bearing LC1}} , q_{\text{bearing LC3}} , q_{\text{bearing LC4}}) = 3.908$ ksf

The controlling bearing pressure needs to be checked with the factored bearing resistance of the soil provided by the Geotechnical Services Section.

MDOT method

A summary of bearing pressure values (in psf) is shown in the following table:

The Geotechnical Services Section uses these values for the verification of bearing resistance and settlement limits. If the bearing pressure exceeds the bearing strength of the soil, the size of the footing needs to be increased. See BDM 7.03.02.G for more information.

Settlement Check

The Geotechnical Services Section uses the controlling bearing pressure from the service limit state to check if the total settlement of foundation is less than 1.5 in., the allowable limit.

BDM 7.03.02G 2b

For LRFD method, the controlling bearing pressure for settlement analysis is

 q_b settlement = max q_b qbearing LC1SerI q_b qbearing LC3SerI q_b q_b q_b q_b q_b q_b q_b q_c q_b q_b q_c q_b q_c

The Geotechnical Services Section uses this controlling bearing pressure to calculate the foundation's total settlement.

For the MDOT method, the bearing pressures under service limit state are provided to the Geotechnical Services Section to calculate the settlement.

Note: Besides the total settlement, considerations should be given to prevent the differential settlement between the abutments and pier from exceeding the tolerable differential settlement limit. Differential settlement limits are given in the *Steel Plate Girder Design Example.*

Sliding Resistance Check

Spread footings must be designed to resist lateral loads without sliding. The sliding resistance of a footing on cohesionless soil is a function of the normal force and the interface friction between the foundation and the soil.

The Geotechnical Services Section should provide a coefficient of sliding resistance (μ) for a design. MDOT typically uses a sliding resistance coefficient of 0.5 for cast-in-place concrete footings. Consult the Geotechnical Services Section to identify the most suitable coefficient for a specific design.

Coefficient of sliding resistance $\mu = 0.5$

LRFD 10.6.3.4

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used:

- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Load Case I

Factored shear force parallel to the Factored shear force parallel to the
 $V_{\text{uFtLC1StrI}} = 6.555 \cdot \frac{kip}{\theta}$

Factored sliding force $V_{\text{sliding}} = V_{\text{uFtLC1StrI}} = 6.555 \cdot \frac{\text{kip}}{\text{ft}}$

Minimum vertical load

$$
F_{VFLC1StrIMin} = 0.9 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 21.662 \cdot \frac{kip}{ft}
$$

 $V_{\text{uFtI}} = V_{\text{uFtI}} - 6.555$

 V_{uFtI} $C3\text{StrI} = 6.555$

Resistance factor for sliding ϕ_{τ} = 0.8 **BDM 7.03.02.F, LRFD Table 10.5.5.5.2-1**

Sliding resistance V_{resistance} $= \phi_{\tau} \cdot \mu \cdot F_{VFLC1StrIMin} = 8.665 \cdot \frac{kip}{ft}$

Check if $V_{\text{resistance}} > V_{\text{sliding}}$ Check $V = \text{if}(V_{\text{resistance}} > V_{\text{sliding}}$, "OK", "Not OK" $) = \text{``OK''}$

Load Case III

Factored shear force parallel to the transverse axis of the footing

Factored sliding force $V_{\text{sliding}} = V_{\text{uFtLC3StrI}} = 6.555 \cdot \frac{\text{kip}}{\text{ft}}$

When calculating the minimum vertical force for sliding and eccentric load limitation checks, the live load on the superstructure is excluded to develop a conservative design.

Minimum vertical load without the live load $F_{\text{VFtLC3StrIMin_{n}}}\ = 0.9 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{foothing}} \right) ...$ + $1.\dot{0}$ (EV_{earthBk} + EV_{earthFt})

 $V_{\text{uFtLC3StrI}} = 6.555 \cdot \frac{\text{kip}}{\text{ft}}$

Stiding resistance

\n
$$
F_{VFLC3StrIMin_nOLL} = 26.754 \cdot \frac{kip}{ft}
$$
\nStiding resistance

\n
$$
V_{resistance} := \phi_{\tau} \cdot \mu \cdot F_{VFLC3StrIMin_nOLL} = 10.702 \cdot \frac{kip}{ft}
$$
\nCheck if $V_{resistance} > V_{\text{sliding}}$

\n
$$
V_{VFLC3StrIMin} = \frac{10.702 \cdot \frac{kip}{ft}}{10.702 \cdot \frac{1000 \cdot \text{K}}{ft}}
$$
\nCheck:

\n
$$
V_{VFLC3StrIMin} = \frac{10.702 \cdot \frac{kip}{ft}}{10.702 \cdot \frac{1000 \cdot \text{K}}{ft}}
$$

 ϕ_{τ} : μ · F_{VFtI} $C1$ StrIMin = 8.665·

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without live load surcharge:

 $Check if $V_{resistance} > V_{sliding}$$

Factored shear force parallel to the

transverse axis of the footing $V_{\text{uFtLC4StrI}} = 8.809 \cdot \frac{kip}{ft}$

Factored sliding force without the live load surcharge

$$
V_{\text{uFtLC4StrI}} = 8.809 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
V_{\text{sliding}} \coloneqq V_{\text{uFtLC4StrI}} - 1.75 P_{\text{LSFooting}} = 6.693 \cdot \frac{\text{kip}}{\text{ft}}
$$

Minimum vertical load without the live load surcharge

Minimum vertical load without
\nthe live load surveillance
\nthe live load surveillance
\n
$$
F_VFtLC4StrIMin_nnOLS := 0.9 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing}) ...
$$
\n
$$
F_VFtLC4StrIMin_nnOLS = 26.754 \cdot \frac{kip}{ft}
$$
\n
$$
F_VFtLC4StrIMin_nnOLS = 26.754 \cdot \frac{kip}{ft}
$$
\n
$$
V_{resistance} := \phi_T \cdot \mu \cdot F_VFtLC4StrIMin_nnOLS = 10.702 \cdot \frac{kip}{ft}
$$
\n
$$
Check if V_{resistance} > V_{sliding}
$$

With live load surcharge:

Check if $V_{resistance} > V_{sliding}$

Factored sliding force

Minimum vertical load with the live load surcharge

With live load surveillance:

\nFactored shear force parallel to the transverse axis of the footing

\nFactored sliding force

\n
$$
V_{\text{uFtL}C4\text{StrI}} = 8.809 \cdot \frac{kip}{ft}
$$
\nMinimum vertical load with the live load surveillance

\n
$$
F_{\text{vFtL}C4\text{StrIMin}} := 0.9 \cdot \left(DC_{\text{Sup}} + DC_{\text{backwall}} + DC_{\text{wall}} + DC_{\text{foting}} \right) \dots
$$
\ndivel bad surface

\n
$$
+ 1.0 \cdot \left(EV_{\text{earthBk}} + EV_{\text{earthFt}} \right) + 1.75 \cdot \text{USFooting}
$$

 $F_{VFLC4StrIMin}$ = 28.434. $\frac{kip}{ft}$

Check if $V_{resistance} > V_{sliding}$

Sliding resistance $V_{\text{resistance}} = \phi_{\tau} \cdot \mu \cdot F_{\text{VFitLCAStrIMin}} = 11.374 \cdot \frac{\text{kip}}{\text{ft}}$ $= \phi_{\tau} \cdot \mu \cdot F_{\text{VFit C4StrIMin}} = 11.374$

Check := if
$$
(V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"
$$

Eccentric Load Limitation (Overturning) Check

The eccentricity of loading at the strength limit state, evaluated based on factored loads, shall not exceed one-sixth of the corresponding dimension measured from the centerline of the footing for stability. **LRFD 10.6.3.3**

The eccentricity in the abutment length direction is not a concern. The following calculations present the evaluation of the eccentricity in the abutment width direction for the Strength I limit state:

Load Case I

 $\frac{\text{Total Case 1}}{\text{ft}}$
Minimum vertical load FVFtLC1StrIMin = 21.662. $\frac{\text{kip}}{\text{ft}}$ Maximum moment about the Maximum moment about the $M_{\text{uFtLC1StrI}} = 38.136 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ Eccentricity in the footing width direction measured from the centerline eB $\rm M_{\rm uFtLCl\,StrI}$ FVFtLC1StrIMin $\frac{1}{2}$ = 1.761 ft 1/6 of footing width B_{footing} $\frac{6 \text{ cm/s}}{6}$ = 2.25 ft Check if the eccentric load limitation is satisfied Check $:=$ if e_B B_{footing} 6 $\lt \frac{1000 \text{mJg}}{2}$, "OK", "Not OK" ſ L \setminus \setminus $\mathcal{C} = \text{if} \left(e_\mathbf{B} < \frac{\text{round}}{6}, \text{``OK''}, \text{``Not OK''} \right) = \text{``OK''}$

Load Case III

Two cases need to be considered: without and with live load.

Without live load:

Moment about the longitudinal axis of the footing (with live load)

Minimum vertical force without the live load

\n
$$
F_{VFLC3StrIMin_nOLL} = 26.754 \cdot \frac{\text{kip}}{\text{ft}}
$$
\nMoment about the longitudinal axis

\n
$$
M_{uFtLC3StrI} = 30.656 \cdot \frac{\text{kip}}{\text{ft}}
$$

 $M_{\text{uFtLC3StrI}}$ noLL FVFtLC3StrIMin_noLL 1.295 ft

> ſ L \setminus

B_{footing} 6

Moment about the longitudinal axis of the footing (without the live load)

$$
M_{uFtLC3StrI_noLL} := M_{uFtLC3StrI} - (1.75 \cdot R_{LLFootingMax}) \cdot \left(I_{heel} + I_{brtowall} - \frac{B_{footing}}{2} \right) = 34.635 \cdot \frac{kip \cdot ft}{ft}
$$

eB

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied Check $:=$ if e_B

With live load:

Minimum vertical force with the live load

Moment about the longitudinal axis of the footing (with the live load)

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation Example 2 if $\cos \theta$ is satisfied
is satisfied

Load Case IV

Two cases need to be considered: without and with live load surcharge.

Without live load surcharge:

Minimum vertical force without the live load surcharge

Moment about the longitudinal axis of the footing (with the live load surcharge)

$$
F_{VFLC4StrIMin_noLS} = 26.754 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
M_{\text{uFtLC4StrI}} = 57.133 \cdot \frac{\text{kip·ft}}{\text{ft}}
$$

Moment about the longitudinal axis of the footing (without the live load surcharge)

$$
M_{\text{uFtLC4StrI_nOLS}} := M_{\text{uFtLC4StrI}} - 1.75 V_{\text{LSFooting}} \cdot \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2}\right) \dots
$$

$$
+ (-1.75) \cdot P_{\text{LSFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}}\right)}{2}
$$

$$
M_{\text{uFtLC4StrI_nOLS}} = 38.891 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

$$
F_{VFLC3StrIMin} := F_{VFLC3StrIMin_n0LL} + 1.75 R_{LLFoothingMax}
$$

 \setminus

 \setminus $\overline{}$

 $\lt \frac{1000 \text{mJg}}{2}$, "OK", "Not OK"

 $\mathcal{C} = \text{if} \left(e_\mathbf{B} < \frac{\text{round}}{6}, \text{``OK''}, \text{``Not OK''} \right) = \text{``OK''}$

$$
F_{VFLLC3StrIMin} = 36.304 \cdot \frac{kip}{ft}
$$

\n
$$
M_{uFtLC3StrI} = 30.656 \cdot \frac{kip \cdot ft}{ft}
$$

\n
$$
e_B := \frac{M_{uFtLC3StrI}}{F_{VFtLC3StrIMin}} = 0.844 \text{ ft}
$$

\nCheck := if $\left(e_B < \frac{B_{footing}}{6}, \text{"OK"}\right), \text{"Not OK"} \right) = \text{"OK"}$

119

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

With live load surcharge:

Minimum vertical force with the live load surcharge

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$
e_{B} := \frac{M_{uFtLC4StrI_n0LS}}{F_{VFtLC4StrIMin_n0LS}} = 1.454 \text{ ft}
$$

Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK"\right) = "OK"$

Minimum vertical force with the live load
\nsurcharge
\nMoment about the longitudinal
\naxis of the footing
\nEccentricity in the footing width direction
\nmeasured from the centerline
\n
$$
\mathbf{e}_{\text{B}} := \frac{M_{\text{uFtLC4StrI}}}{F_{\text{vFtLC4StrIMin}}} = 2.009 \text{ ft}
$$

Check $:=$ if e_B B_{footing} 6 $\lt \frac{1000 \text{mJg}}{2}$, "OK", "Not OK" L \setminus $\mathcal{C} = \text{if} \left(e_\mathbf{B} < \frac{\text{round}}{6}, \text{``OK''}, \text{``Not OK''} \right) = \text{``OK''}$

Step 3.7 Backwall Design

Description

Please refer to the design calculations and details presented in Step 2.7. The backwall forces and moments used in Step 2.7. are not impacted by the use of EPS blocks as the backfill material since EPS blocks are located below the backwall.

Step 3.8 Abutment Wall Design

Description

This step presents the design of the abutment wall.

Page Contents 123 Forces and Moments at the Base of the Abutment Wall

- **123 Design for Flexure**
- **126 Design for Shear**
- **128 Development Length of Reinforcement**
- **129 Shrinkage and Temperature Reinforcement**

Forces and Moments at the Base of the Abutment Wall

Step 3.5 presents the load effects at the base of the abutment wall under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VWH} (kip/ft)

Factored moment about the longitudinal axis of the abutment wall, M_{u Wall (kip[.]ft/ft)

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

Moment demand at the base of the wall

Select a trial bar size bar $= 8$

$$
M_{\text{DemandWall}} := M_{\text{uWallLC4StrI}} = 73.864 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Flexure Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

1-It we see
\nEffective deepth
\nBflective depth
\nResistance factor for flexure
\nby i = 0.9
\nWe then member
\nthe member
\nStress block factor
\n
$$
\beta_1 := \min \left[\max \left[0.85 - 0.05 \cdot \left(\frac{f_c - 4ksi}{ksi} \right), 0.65 \right], 0.85 \right] = 0.85
$$
\nLRFD 5.5.4.2
\nSolve the following equation of A_s to calculate the required area of steel to satisfy the moment demand. Use an
\nassumed initial, value to solve the equation.
\nInitial assumption
\n
$$
A_s := 1 \text{ in}^2
$$
\nGiven $M_{\text{Dermand}}[W \text{ all} : \text{ft} = \varphi_{\text{F}} A_s : f_y \left[d_c - \frac{1}{2} \left(\frac{A_s : f_y}{0.85 \cdot f_c : b} \right) \right]$ \nLRFD
\nGiven $M_{\text{Dermand}}[W \text{ all} : \text{ft} = \varphi_{\text{F}} A_s : f_y \left[d_c - \frac{1}{2} \left(\frac{A_s : f_y}{0.85 \cdot f_c : b} \right) \right]$ \nLRFD
\nGiven $M_{\text{Dermand}}[W \text{ all} : \text{ft} = \varphi_{\text{F}} A_s : f_y \left[d_c - \frac{1}{2} \left(\frac{A_s : f_y}{0.85 \cdot f_c : b} \right) \right]$ \n
$$
= \text{Cf} \left(\frac{A_s}{0.85 \cdot f_c : b} \right)
$$
\n
$$
= \text{Cf} \left(\frac{A_s}{0.85 \cdot f_c : b} \right)
$$
\nH
\nMomentum capacity of the section
\nwith the provided steel area
\nwith the provided steel area
\n
$$
M_{\text{Capacity}}[W \text{ all} = 121.672 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\n
$$
= \frac{A_s \text{Provided} \cdot f_y}{0.85 \cdot f_c : \beta_1 : b} = 1.82 \cdot \text{in}
$$
\nCheck the validity of assumption $f_s = f_y$
\n
$$
= \frac{A_s \text{Provided} \cdot f_y}{0.85 \cdot f_c : \beta_1 : b} =
$$

 A_{bar} . 12in

 $= \frac{A_{\text{bar}} \cdot 12 \text{m}}{2} = 0.79 \cdot \text{in}^2$

Area of reinforcing steel provided in a
1-ft wide section

 1 -ft wide section $A_{\rm sProtided}$

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Flexural cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental

 γ_3 = 0.67 For ASTM A615 Grade 60 reinforcement

Section modulus
\nSection modulus
\n
$$
S_{c} := \frac{1}{6} \cdot b \cdot t_{wall}^{2} = 2.888 \times 10^{3} \cdot in^{3}
$$
\n\nCracking moment
\n
$$
M_{cr} := \frac{\gamma_{3} \cdot \gamma_{1} \cdot f_{r} \cdot S_{c}}{ft} = 107.246 \cdot \frac{kip \cdot ft}{ft}
$$
\n1.33 times the factored moment demand
\n
$$
1.33 \cdot M_{\text{DemandWall}} = 98.239 \cdot \frac{kip \cdot ft}{ft}
$$
\n\nRequired moment to satisfy the minimum reinforcement requirement
\nCheck the adequacy of the section capacity
\n
$$
M_{req} := \min(1.33 M_{\text{DemandWall}}, M_{cr}) = 98.239 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{req} := \min(1.33 M_{\text{DemandWall}}, M_{cr}) = 98.239 \cdot \frac{kip \cdot ft}{ft}
$$

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

 $s \leq \frac{700 \cdot \gamma_e}{\gamma}$

 d_c := Cover_{wall} = $3 \cdot in$

 $d_{\mathbf{c}}$ $= 1 + \frac{1}{0.7 (t_{\text{wall}} - d_{\text{c}})} = 1.122$

The spacing requirements for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition $\gamma_e := 1.00$

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

 $\beta_{\rm s} \coloneqq 1$

 \cdot b \cdot x² = $\frac{E_s}{E}$

Assumed distance from the extreme Example distance from the externe
compression fiber to the neutral axis $x := 6 \cdot in$

Given $\frac{1}{2}$

Position of the neutral axis

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to service limit state moment

 f_{ss} (not to exceed $0.6f_v$) f

2
\n
$$
E_c
$$

\n $x_{na} := \text{Find}(x) = 5.568 \cdot \text{in}$
\n $T_s := \frac{M_u \text{WallLC4SerI}}{d_e - \frac{x_{na}}{3}} \cdot \text{ft} = 18.4 \cdot \text{kip}$
\n $f_{ss1} := \frac{T_s}{A_s \text{Provided}} = 23.279 \cdot \text{ksi}$

 $=$ $\frac{1}{F}$ A_sProvided $\left(d_e - x\right)$

 $\leq \frac{1}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$ **LRFD Eq. 5.6.7-1**

$$
f_{\text{SS}} := \min(f_{\text{SS}1}, 0.6f_{\text{y}}) = 23.279 \text{ k} \sin \theta
$$

Required reinforcement spacing
\n
$$
s_{barRequired} := \frac{700 \cdot \gamma_e \cdot \frac{kip}{in}}{\beta_s \cdot f_{ss}} - 2 \cdot d_c = 20.789 \cdot in
$$
\nCheck if the spacing provided
\nthe required spacing
\n
$$
c_{bark} := if (s_{bar} < s_{barRequired}, "OK", "Not OK") = "OK"
$$

Shrinkage and Temperature Reinforcement Requirement

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the abutment wall.

For bars, the area of reinforcement per foot (As), on each face and in each direction, shall satisfy AS 1.3bh 2b h ()f y **LRFD 5.10.6** and 0.11in² AS 0.6in² Minimum area of shrinkage and temperature reinforcement Ashrink.temp min 0.60 in2 ft max 0.11 in2 ft 1.3 hwall t wall kip in ft 2 hwall t wall fy ft 0.349 in² Check if the provided area of steel > the required area of shrinkage and temperature steel Check if AsProvided Ashrink.temp "OK" "Not OK" "OK"

Design for Shear

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

The maximum factored shear force
\nat the base of the albument wall
\nEffective width of the section
\nDepth of equivalent rectangular
\nstress block
\nEffective shear depth
\n
$$
a := \frac{A_{\text{SProvided}} f_y}{0.85 \cdot f_c \cdot b} = 1.549 \cdot \text{in}
$$
\n
$$
d_v := \max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{\text{wall}} \right) = 34.225 \cdot \text{in} \quad \text{LRFD 5.7.2.8}
$$
\nNote: Since there is no transverse reinforcement in the well and the overall depth of the well is greater than 16.

Note: Since there is no transverse reinforcement in the wall and the overall depth of the wall is greater than 16 in., the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used..

The factored N_u , V_u , and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the abutment wall. The critical section is located in the wall segment with EPS backfill.

Factored axial force at the critical section (use negative if compression)

$$
N_{uWallShear} := \left[1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} - d_{v} \cdot t_{wall} \cdot W_{c}\right) \cdots\right]
$$

+ 1.5DW_{Sup}

$$
N_{uWallShear} = -18.318 \cdot \frac{kip}{ft}
$$

The lateral earth load component at the critical section for shear consists of three parts. Part 1 is the lateral load from the soil located above the EPS blocks, which is the same as that calculated in Step 3.4. Part 2 is the lateral load from the EPS due to the vertical load at the top of the EPS blocks. Part 3 is the lateral load from the soil located behind the EPS blocks above the critical section for shear.

EH 1: the lateral load from the soil located above the EPS blocks

EH 2: the lateral load from the EPS due to the vertical load at the top of the EPS blocks

EH 3: the lateral load from the soil located behind the EPS blocks and above the critical section for shear.

PEHWall2Shear := PVEPS:
$$
(h_{EPS} + h_{SoilBelowEPS} - d_v) = 1.042 \cdot \frac{kip}{ft}
$$

\nPEHWall3Shear := $\frac{1}{2}k_{EPS}$: γ_s : $(h_{EPS} + h_{SoilBelowEPS} - d_v)^2 = 0.231 \cdot \frac{kip}{ft}$
\nPEHWallShear := P_{EHI} + P_{EH2} + P_{EHWall3Shear} = 2.445 $\cdot \frac{kip}{ft}$

The lateral live load surcharge at the critical section consists of two parts.

LS 1: the lateral load from the soil located above the EPS blocks due to the live load surcharge

LS 2: the lateral load from the EPS blocks located above the critical section due the the live load surcharge

$$
P_{LSWall2Shear} := \frac{1}{10} \gamma_s \cdot h_{eq} \cdot (h_{EPS} + h_{SoilBelowEPS} - d_v) = 0.268 \cdot \frac{kip}{ft}
$$

$$
P_{LSWallShear} := P_{LSWall1} + P_{LSWall2Shear} = 0.828 \cdot \frac{kip}{ft}
$$

Factored shear force at the critical section for shear (demand)

$$
V_{uWallShear} := 1.5 \cdot P_{EHWallShear} + 1.75 \cdot P_{LSWallShear} + 0.5 \text{TU} = 5.256 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment at the critical section for shear

$$
M_{uWallShear} := 0.9 \cdot DC_{backwall} \cdot \frac{(t_{backwall} - t_{wall})}{2} + (1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup}) \cdot (t_{brtowall} - \frac{t_{wall}}{2}) ... + 1.5 P_{EH1} \cdot (\frac{1}{3} h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} - d_v) ... + 1.5 P_{EH2} \cdot \frac{1}{2} (h_{EPS} + h_{SoilBelowEPS} - d_v) ... + 1.75 P_{LSWall1} \cdot (\frac{1}{2} h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} - d_v) ... + 1.75 \cdot P_{LSWall2Shear} \cdot \frac{(h_{EPS} + h_{SoilBelowEPS} - d_v)}{2} + 0.5 \cdot TU \cdot (h_{wall} - d_v) M_{uWallShear} = 56.896 \cdot \frac{kip \cdot ft}{ft}
$$

Note: MDOT limits reinforcement spacing to a maximum of 18 in. **BDG 5.16.01**

The required minimum shrinkage and temperature reinforcement area at the abutment wall was previously calculated during the design of flexural reinforcement.

The abutment wall design presented in this step provides the following details:

- No. 8 bars @ 12.0 in. spacing $(A_s = 0.79 \text{ in.}^2/\text{ft})$ as the back face flexural reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front and back face horizontal shrinkage and temperature reinforcement.

Step 3.9 Structural Design of the Footing

Description

This step presents the structural design process for the abutment footing.

Forces and Moments at the Base of the Footing

Step 3.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VFt} (kip/ft) F_{VFt} (kip/ft) of the footing, V_{TFt} (kip/ft)

Factored shear force parallel to the transverse axis

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Note: The length of the footing and the abutment wall is 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Toe Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:

For structural design of an eccentrically loaded foundation, a triangular or trapezoidal bearing pressure distribution is used.

LRFD 10.6.5

According to the loads in the summary tables, Load Case IV under the Strength I limit state is identified as the governing load case for the design of flexure and shear at the toe.

$$
F_{VFLC4StrI} = 39.863 \cdot \frac{kip}{ft} \qquad M_{uFtLC4StrI} = 57.133 \cdot \frac{kip \cdot ft}{ft}
$$

132

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

FVFtLC4StrI F_{VFtLC4StrI} B_{footing} $1 + \frac{6 \cdot e_B}{\sqrt{2}}$ B_{footing} $\ddot{}$ ſ L \setminus \setminus $\overline{}$ J $=$ $\frac{1}{2}$ + $\frac{1}{2}$ + $\frac{1}{2}$ = 4.834·ksf qmin FVFtLC4StrI B_{footing} $1 - \frac{6 \cdot e_B}{2}$ B_{footing} $\Bigg(1 \setminus$ \setminus $\overline{}$ J $:=$ $\frac{1}{2}$ $\frac{1}{2$

> $(q_{\text{max}} - q_{\text{min}})$ B_{footing}

 $t = q_{\text{min}} + \frac{q_{\text{max}}}{R_{\text{max}}} \cdot (B_{\text{footing}} - l_{\text{toe}}) = 3.069 \cdot \text{ksf}$

 $\rm M_{\rm uFtLC4StrI}$

 $:=$ $\frac{44 \text{ m} - 6 \text{ m/s}}{1.433 \cdot \text{ft}}$

The critical section for flexural design is at the front face of the wall.

Bearing pressure at the critical section

A simplified analysis method is used in this example to determine the maximum moments at the front face of the wall by selecting load factors to produce the maximum bearing pressure and minimum resisting loads. This method is conservative and eliminates the need for using multiple combinations.

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum moment at the front face of the wall.

The moment demand at the critical section

$$
M_{rDemand} := q_{toe} \cdot \frac{l_{toe}^{2}}{2} + (q_{max} - q_{toe}) \cdot \frac{l_{toe}^{2}}{3} - 0.9 \cdot W_{c} \cdot t_{footing} \cdot \frac{l_{toe}^{2}}{2} - 1.0 \gamma_{s} \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{l_{toe}^{2}}{2}
$$

$$
M_{rDemand} = 67.396 \cdot \frac{kip \cdot ft}{ft}
$$

Flexure Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

The tensile reinforcement provided must develop a factored flexural resistance equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

moment or 1.33 times the factored moment from the applicable strength limit state load combinations.
\nFlexural cracking variability factor\n

$\gamma_1 := 1.6$	For concrete structures that are not precast segmental	
Ratio of specified minimum yield	$\gamma_3 := 0.67$	For ASTM A615 Grade 60 reinforcement
the nonpersressed reinforcement	$S_c := \frac{1}{6} \cdot b \cdot t_{footing}^2 = 2.592 \times 10^3 \cdot in^3$	
Cracking moment	$M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.254 \cdot \frac{kip \cdot ft}{ft}$	
1.33 times the factored moment demand	1.33·M _r Demand	= 89.637· $\frac{kip \cdot ft}{ft}$

Required moment to satisfy the minimum reinforcement requirement

$$
M_{req} := min(1.33 M_{rDemand}, M_{cr}) = 89.637 \cdot \frac{kip \cdot ft}{ft}
$$

 $\leq \frac{1}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$ **LRFD Eq. 5.6.7-1**

d_{bar} 2 $=$ Cover_{ft} + $\frac{64}{1}$ = 4.5 in

 $d_{\mathbf{c}}$ $= 1 + \frac{1}{0.7 (\text{tfooting} - \text{d}_\text{c})} = 1.204$

Check the adequacy of section capacity Check $:=$ if $(M_{Provided} > M_{req}, "OK", "Not OK") = "OK"$

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

 $s \leq \frac{700 \cdot \gamma_e}{\gamma}$

 $\gamma_e := 1.00$

 $\beta_{\rm s} \coloneqq 1$

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition

Distance from extreme tension fiber to the Example from externe whiston flock which d_c := Cover_{ft}

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer nearest the tension face

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, $f_{\rm ss}$, requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme compression fiber to the neutral axis

$$
x := 5 \cdot in
$$

Given
$$
\frac{1}{2} \cdot b \cdot x^2 = \frac{E_s}{E_c} \cdot A_s \text{Provided} \cdot (d_e - x)
$$

$$
x_{na} := \text{Find}(x) = 5.303 \cdot in
$$

Position of the neutral axis

The vertical force and moment at the base of the footing from Load Case IV under the Service I limit state are:

$$
F_{\text{VFtLC4SerI}} = 30.702 \cdot \frac{\text{kip}}{\text{ft}} \qquad M_{\text{uFtLC4SerI}} = 31.183 \cdot \frac{\text{kip·ft}}{\text{ft}}
$$

Eccentricity in the footing width direction under Service I limit state

Maximum and minimum bearing pressure under Service I limit state

$$
e_{BSerI} := \frac{M_{uFtLC4SerI}}{F_{VFtLC4SerI}} = 1.016 \cdot ft
$$

$$
F_{VFtLC4SerI} \left(6 \cdot e_{BSerI} \right)
$$

$$
q_{\text{maxSerI}} := \frac{V_{\text{F}}(E + S_{\text{C}})}{B_{\text{foothing}}}\cdot \left(1 + \frac{B_{\text{S}}(E)}{B_{\text{foothing}}}\right) = 3.301 \cdot \text{ksf}
$$

$$
q_{\text{minSerI}} := \frac{F_{\text{VF}tL}C4\text{SerI}}{B_{\text{foothing}}}\cdot \left(1 - \frac{6 \cdot \text{e}_{\text{BSerI}}}{B_{\text{foothing}}}\right) = 1.248 \cdot \text{ksf}
$$

Bearing pressure at the critical
section under Service I limit state section under Service I limit state $q_{toSerI} = q_{minSerI}$

The moment at the critical section under the Service I limit state:

$$
M_{r\text{SerI}} := q_{\text{toe} \text{SerI}} \cdot \frac{l_{\text{toe}}^2}{2} + \left(q_{\text{max} \text{SerI}} - q_{\text{toe} \text{SerI}} \right) \cdot \frac{l_{\text{toe}}^2}{3} - W_c \cdot t_{\text{foothing}} \cdot \frac{l_{\text{toe}}^2}{2} - \gamma_s \cdot \left(h_{\text{toe} \text{Depth}} - t_{\text{foothing}} \right) \cdot \frac{l_{\text{toe}}^2}{2}
$$
\n
$$
M_{r\text{SerI}} = 41.109 \cdot \frac{kip \cdot ft}{ft}
$$
\nTensile force in the reinforcement

\nto the service limit state moment

\nto the service limit state moment

\nStress in the reinforcement

\nStress in the reinforcement

\nStress in the reinforcement

\nfor the second of the service limit state moment

\nf_{ss} := \frac{T_s}{A_{s\text{Provided}}}\n
$$
f_{\text{ss}} := \frac{T_s}{A_{s\text{Provided}}}
$$
\n
$$
f_{\text{ss}} := \min \left(f_{\text{ss}1}, 0.6 f_y \right) = 20.655 \cdot \text{ksi}
$$
\nRequired reinforcement spacing

\nSo

\n

 $q_{toeSerI} = 2.338$ ksf

Shrinkage and Temperature Reinforcement Requirement LRFD 5.10.6

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the toe:

Minimum area of shrinkage and
\ntemperature reinforcement
\n
$$
A_{shrink.temp} := min \begin{bmatrix} 0.60 \frac{in^2}{ft} \end{bmatrix}
$$

\n $A_{shrink.temp} = min \begin{bmatrix} 0.11 \frac{in^2}{ft} \end{bmatrix}$
\n $A_{shrink.temp} = max \begin{bmatrix} 0.11 \frac{in^2}{ft} \end{bmatrix}$

 $(q_{\text{maxSerI}} - q_{\text{minSerI}})$ B_{footing} $t = q_{\text{minSerI}} + \frac{($ masser minister (B_{footing} – l_{toe})

Design for Shear

Effective width of the section $b = 12 \cdot in$

Depth of equivalent rectangular stress block a

$$
0.85 \cdot f_c \cdot b
$$

Effective shear depth
$$
d_v := max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{footing} \right) = 31.225 \cdot in \qquad 5.7.2.8
$$

The critical section for shear at the toe is located at a distance d_v from the front face of the wall.

Distance from the toe to the critical section

$$
l_{shear} := l_{toe} - d_v = 3.731 \text{ ft}
$$

$$
q_d := q_{min} + \frac{(q_{max} - q_{min})}{B_{footing}} \cdot (B_{footing} - l_{shear}) = 3.794 \cdot \text{ksf}
$$

Bearing pressure at the shear critical section

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum shear at the shear critical section.

Factored shear force (demand) at the shear critical section

$$
V_{\text{uFtToe}} := \frac{(q_{\text{max}} + q_{\text{d}})}{2} \cdot l_{\text{shear}} - 0.9 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{shear}} - 1.0 \cdot \gamma_{\text{s}} \cdot (h_{\text{toeDepth}} - t_{\text{footing}}) \cdot l_{\text{shear}}
$$

$$
V_{\text{uFtToe}} = 12.794 \cdot \frac{\text{kip}}{\text{ft}}
$$

 A _SProvided f_y

 $\frac{1}{1} = \frac{1.549 \cdot in}{1.549 \cdot in}$

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than $3d_{v}$. **LRFD 5.7.3.4.1**

 $\beta \coloneqq 2$

Check if the distance l_{toe} is less than $3d_v$ Check := if $(l_{\text{toe}} < 3 \cdot d_v$, "Yes", "No" $) =$ "Yes"

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n , is calculated as follows:

Heel Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:

The self-weight of the footing, the weight of soil, live load surcharge and the bearing pressure act on the heel. The critical load combination for the design selects the load factors to produce the minimum vertical loads and maximum eccentricities resulting in the minimum bearing pressure.

The critical location for the design of flexure is located at the back face of the wall. **LRFD 5.12.8.4**

LRFD C5.12.8.6.1

In the general case of a cantilever abutment wall, where the downward load on the heel is larger than the upward reaction of the soil under the heel, the top of the heel is in tension. Therefore, the critical section for shear is taken at the back face of the abutment wall.

Load cases I, III, and IV under the Strength I limit state are used to calculate the maximum moment and shear at the critical sections.

Load Case I

Eccentricity in the footing width direction $e_B :=$

Maximum and minimum bearing pressure

$$
q_{max} := \frac{F_{VFLC1StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 2.86 \cdot \text{ksf}
$$
\n
$$
q_{min} := \frac{F_{VFLC1StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.349 \cdot \text{ksf}
$$

 \setminus

J

 $= q_{\min} + (q_{\max} - q_{\min}) \frac{\text{net}}{2} = 1.093 \text{ ksf}$

l heel **B**footing

Bearing pressure at the critical section $q_{heelLC1StrI} = q_{min} + (q_{max} - q_{min})$

Factored moment at the critical section

$$
M_{rLCIStrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{hel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC1StrI} - q_{min}) l_{hel}^2
$$

$$
M_{rLCIStrI} = 12.671 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{\text{uHeelLC1StrI}} = 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} - q_{\text{min}} \cdot l_{\text{heel}} - \frac{1}{2} \cdot \left(q_{\text{heelLC1StrI}} - q_{\text{min}} \right) \cdot l_{\text{heel}}
$$

$$
V_{\text{uHeelLC1StrI}} = 5.839 \cdot \frac{\text{kip}}{\text{ft}}
$$

Load Case III

Two cases need to be considered: without and with the live load.

Without the live load:

Minimum vertical force
$$
F_{V F t L C 3 S tr I Min_n o L L} = 26.754 \cdot \frac{kip}{ft}
$$
Step 3.6, sliding resistance check

Factored moment about the longitudinal axis of the footing

Maximum and minimum bearing pressure

Eccentricity in the footing width direction

$$
M_{uFtLC3Str1_nOLL} = 34.635 \text{ ft} \cdot \frac{\text{kip}}{\text{ft}}
$$
**Step 3.6, eccentric
load limitation check**

$$
e_B := \frac{M_{uFtLC3Str1_nOLL}}{F_{VFtLC3Str1Min_nOLL}} = 1.295 \cdot \text{ft}
$$

$$
q_{max} := \frac{F_{VFtLC3Str1Min_nOLL}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.122 \cdot \text{ksf}
$$

$$
q_{min} := \frac{F_{VFtLC3Str1Min_nOLL}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.842 \cdot \text{ksf}
$$

Bearing stress at the critical section

$$
q_{heelLC3StrI} \coloneqq q_{min} + (q_{max} - q_{min}) \frac{l_{heel}}{B_{footing}}
$$

Factored moment at the critical section

$$
M_{rLC3StrI_noLL} := 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC3StrI_noLL} = 8.913 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{uHeelLC3StrI_nOLL} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}
$$

$$
V_{uHeelLC3StrI_nOLL} = 4.006 \cdot \frac{kip}{ft}
$$

With the live load:

Factored moment about the longitudinal Factored moment about the longitudinal $M_{\text{uFtLC3StrI}} = 30.656 \cdot \frac{kip \cdot ft}{ft}$ Step 3.6,

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Bearing pressure at the critical section

Minimum vertical force
$$
F_{VFLC3StrIMin} = 36.304 \cdot \frac{kip}{ft}
$$
Step 3.6, sliding resistance check

summary table

 1.517 ksf

$$
e_B := \frac{M_{\text{uFtLC3StrI}}}{F_{\text{VFtLC3StrIMin}}} = 0.844 \cdot \text{ft}
$$

$$
q_{\text{max}} := \frac{F_{\text{VFtLC3StrIMin}}}{B_{\text{footing}}}\cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 3.698 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFtLC3StrIMin}}}{B_{\text{footing}}}\cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 1.68 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelLC3StrI}} := q_{\text{min}} + \left(q_{\text{max}} - q_{\text{min}}\right) \frac{I_{\text{heel}}}{B_{\text{footing}}} = 2.278 \cdot \text{ksf}
$$

Factored moment at the critical section

$$
M_{rLC3StrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^2
$$

$$
M_{rLC3StrI} = 2.413 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{uHeelLC3StrI} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}
$$

$$
V_{uHeelLC3StrI} = 0.808 \cdot \frac{kip}{ft}
$$

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Minimum vertical force
\nFactored moment about the longitudinal
\naxis of the footing
\n
$$
M_{\text{uFtL} \text{C4Str1}_{\text{noLS}} = 38.891 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{\text{uFtL} \text{C4Str1}_{\text{noLS}} = 38.891 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{\text{uFtL} \text{C4Str1}_{\text{noLS}} = 38.891 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{\text{uFtL} \text{C4Str1}_{\text{noLS}} = 38.891 \cdot \frac{kip \cdot ft}{ft}
$$
\n
$$
M_{\text{vFtL} \text{C4Str1}_{\text{noLS}}} = 1.368 \cdot ft
$$
\n
$$
M_{\text{maximum and minimum bearing pressures}}
$$
\n
$$
q_{\text{max}} := \frac{F_{\text{VFtL} \text{C4Str1}_{\text{Min}} \text{noLS}}}{B_{\text{foothing}}}\cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{foothing}}}\right) = 3.186 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFtL} \text{C4Str1}_{\text{Min}} \text{noLS}}}{B_{\text{foothing}}}\cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{foothing}}}\right) = 0.777 \cdot \text{ksf}
$$
\n
$$
q_{\text{heelL} \text{C4Str1}_{\text{noLS}}} = 1.491 \cdot \text{ksf}
$$
\n
$$
M_{\text{rL} \text{C4Str1}_{\text{noLS}}} = 1.25 \cdot W_{\text{c}} \cdot t_{\text{foothing}} \cdot \frac{l_{\text{heel}}}{2} + 1.35 \text{EV}_{\text{earthB}} \cdot \frac{l_{\text{heel}}}{2} - q_{\text{min}} \cdot l_{\text{heel}} \cdot \frac{l_{\text{heel}}}{2} - \frac{l}{6} (q_{\text{heel} \text{L} \text{C4Str1}_{\text{o}} - q_{\text{min}}) l_{\text{heel}} \cdot \frac{l_{\text{heel}}}{2} - \frac{l_{\text{h
$$

Factored shear force at the critical section

 $V_{\text{uHeelLC4StrI_nOLS}} = 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} - q_{\text{min}} \cdot l_{\text{heel}} - \frac{1}{2} \cdot (q_{\text{heelLC4StrI}} - q_{\text{min}}) \cdot l_{\text{heel}}$ $V_{\text{uHeelLC4StrI_n0LS}} = 4.187 \cdot \frac{\text{kip}}{\text{ft}}$

2

With the live load surcharge:

Minimum vertical force $F_{VFtLC4StrIMin} = 28.434 \cdot \frac{kip}{ft}$ Step 3.6, sliding

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

$$
e_{\text{B}} := \frac{E_{\text{VFLC4StrIMin}}}{F_{\text{VFLC4StrIMin}}} = 2.009 \cdot \text{ft}
$$
\n
$$
q_{\text{max}} := \frac{F_{\text{VFLC4StrIMin}}}{B_{\text{footing}}}\cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 3.987 \cdot \text{ksf}
$$
\n
$$
q_{\text{min}} := \frac{F_{\text{VFLC4StrIMin}}}{B_{\text{footing}}}\cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 0.225 \cdot \text{ksf}
$$

 $\rm M_{\rm uFtLC4StrI}$

 $M_{\text{uFtLC4StrI}} = 57.133 \cdot \frac{\text{kip·ft}}{\text{ft}}$ **Step 3.6, summary table**

resistance check

$$
q_{\text{heelLC4StrI}} := q_{\text{min}} + \left(q_{\text{max}} - q_{\text{min}} \right) \frac{\text{1heel}}{B_{\text{footing}}} = 1.34 \cdot \text{ksf}
$$

Factored moment at the critical section

Bearing stress at the critical section

$$
M_{rLC4StrI} \coloneqq 1.25 \cdot W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 \text{EV}_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} \left(q_{heelLC4StrI} - q_{min} \right) l_{heel}^2
$$

$$
M_{rLC4StrI} = 12.672 \cdot \frac{kip \cdot ft}{ft}
$$

Factored shear force at the critical section

$$
V_{uHeelLC4StrI} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC4StrI} - q_{min}) \cdot l_{heel}
$$

$$
V_{uHeelLC4StrI} = 5.593 \cdot \frac{kip}{ft}
$$

Moment demand at the critical section

 $M_{\text{HeelDemand}} \coloneqq \max(M_{\text{rLC1StrI}}, M_{\text{rLC3StrI_noLL}}, M_{\text{rLC3StrI}}, M_{\text{rLC4StrI_noLS}}, M_{\text{rLC4StrI}}) = 12.672 \cdot \frac{\text{kip·ft}}{\text{ft}}$ $\mathcal{L} = \max(M_{rI} C_1 S_{trI}, M_{rI} C_3 S_{trI} \text{ not } I, M_{rI} C_3 S_{trI}, M_{rI} C_4 S_{trI} \text{ not } S, M_{rI} C_4 S_{trI}) = 12.672 \cdot$ Shear demand at the critical section

$$
V_{\text{HeelDemand}} := \max\left(V_{\text{uHeelLC1StrI}}, V_{\text{uHeelLC3StrI}} \text{ to } V_{\text{HeelLC3StrI}}, V_{\text{uHeelLC4StrI_n0LS}}, V_{\text{uHeelLC4StrI}}\right)
$$
\n
$$
V_{\text{HeelDemand}} = 5.839 \cdot \frac{\text{kip}}{\text{ft}}
$$

Flexure Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

 \mathcal{L}

141

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Cracking moment

1.33 times the factored moment demand

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

s

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition $\gamma_e := 1.00$

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, $f_{\rm ss}$, requires establishing

the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Given $\frac{1}{2}$

 $x := 5 \cdot in$

 \cdot b \cdot x² = $\frac{E_s}{E}$

 $E_{\rm c}$

2

Assumed distance from the extreme compression fiber to the neutral axis

Position of the neutral axis x_{na} := Find $(x) = 4.049$ in

Maximum and minimum bearing pressure under Service I limit state (from the toe design)

Bearing pressure at the critical section $q_{HeelSerI} = q_{minSerI}$

$$
\gamma_1\coloneqq 1.6
$$

Flexural cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental

$$
\gamma_3 := 0.67
$$
 For ASTM A615 Grade 60 reinforcement

Section modulus
\n
$$
S_c := \frac{1}{6} \cdot b \cdot t_{footing}^2 = 2.592 \times 10^3 \cdot in^3
$$
\n
$$
M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.254 \cdot \frac{kip \cdot ft}{ft}
$$

$$
1.33 \cdot M_{\text{HeelDemand}} = 16.854 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Required factored moment to satisfy the minimum reinforcement requirement Mreq min 1.33MHeelDemand Mcr 16.854 kip ft ft

Check the adequacy of the section capacity
$$
Check := if(M_{Provided} > M_{req}, "OK", "Not OK") = "OK"
$$

$$
d_{\mathbf{C}} := \text{Cover}_{\hat{\mathbf{H}}} = 4 \cdot \text{in}
$$

$$
\beta_{\rm S} := 1 + \frac{d_{\rm c}}{0.7(t_{\rm footing} - d_{\rm c})} = 1.179
$$

 $=$ $\frac{1}{F}$ A_sProvided $\left(d_e - x\right)$

$$
b_{\rm s} := 1 + \frac{d_{\rm c}}{0.7(t_{\rm s} - t_{\rm s})} = 1.1
$$

the service limit state:

$$
\leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c
$$

LRFD Eq. 5.6.7-1

 $q_{maxSerI} = 3.301$ ksf $q_{minSerI} = 1.248$ ksf

 $(q_{\text{maxSerI}} - q_{\text{minSerI}})$ B_{footing} $l = q_{\text{minSerI}} + \frac{\langle \text{masses} \rangle}{R_{\text{max}}}\cdot l_{\text{heel}} = 1.856 \cdot \text{ksf}$

144

The moment at the critical section under the Service I limit state

$$
M_{\text{heelSerI}} := W_{\text{c}} \cdot t_{\text{footing}} \cdot \frac{I_{\text{heel}}}{2} + EV_{\text{earthBk}} \cdot \frac{I_{\text{heel}}}{2} \dots
$$

+ $V_{\text{LSFooting}} \cdot \frac{I_{\text{heel}}}{2} - q_{\text{minSerI}} \cdot \frac{I_{\text{heel}}}{2} - (q_{\text{HeelSerI}} - q_{\text{minSerI}}) \cdot \frac{I_{\text{heel}}}{6}$

$$
M_{\text{heelSerI}} = 3.507 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

teel due

$$
T_{\text{s}} := \frac{M_{\text{heelSerI}}}{d_{\text{e}} - \frac{x_{\text{na}}}{3}}
$$

: to the

$$
f_{\text{ss1}} := \frac{T_{\text{s}}}{A_{\text{sProvided}}} = 3.12 \cdot \text{ksi}
$$

$$
f_{\text{ss1}} := \frac{700 \cdot \gamma_{\text{c}} \cdot \frac{\text{kip}}{\text{in}}}{\frac{N_{\text{p}}}{\beta_{\text{s}} \cdot f_{\text{ss}}}} - 2 \cdot d_{\text{c}} = 182.337 \cdot \text{in}
$$

the

$$
\frac{\text{Check} := \text{if} (\text{s}_{\text{bar}} < \text{s}_{\text{barRequired}}, \text{''OK''}, \text{''Not OK''}) = \text{''OK''}}{\text{for}} = \frac{N_{\text{bar}}}{N_{\text{barRequired}}}
$$

Tensile force in the reinforcing ste to the service limit state moment

Stress in the reinforcing steel due service limit state moment

 f_{ss} (not to exceed 0.6 f_v)

Required reinforcement spacing

Check if the spacing provided $\leq t$ required spacing

Shrinkage and Temperature Reinforcement LRFD 5.10.6

The required minimum shrinkage and temperature reinforcement area was calculated previously for the toe.

Required shrinkage and temperature steel area $A_{\text{shrink}.\text{temp}} = 0.319 \cdot \text{in}^2$

Design for Shear

The critical section for shear in the heel is located at the back face of the abutment wall. **LRFD C5.12.8.6.1**

Shear demand at the critical section (max. from the load cases)

Effective width of the section

Depth of the equivalent rectangular $s =$ stress block and $s =$

$$
\Delta
$$
shrink $t_{\text{emm}} = 0.319 \cdot \text{in}^2$

Check := if
$$
(A_{sProvided} > A_{shrink,temp}, "OK", "Not OK") = "OK"
$$

$$
V_{\text{HeelDemand}} = 5.839 \cdot \frac{\text{kip}}{\text{ft}}
$$

$$
= 12 \cdot \text{in}
$$

 \setminus

Depth of the equivalent rectangular
\nstress block\n
$$
a := \frac{A_{sProvided} \cdot f_y}{0.85 \cdot f_c \cdot b} = 0.863 \cdot in
$$
\nLRFD
\nd_V := max $\left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{footing}\right) = 31.569 \cdot in$ \nLRFD
\n5.7.2.8

$$
f_{\rm{max}}
$$
The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than $3d_{v}$.

Check := if
$$
(l_{\text{heel}} < 3 \cdot d_v, \text{``Yes''}, \text{``No''}) = \text{``Yes''}
$$

LRFD 5.7.3.4.1

Check if the distance $l_{\text{heel}} < 3 d_v$

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally ractor indicating the ability of diagonally
cracked concrete to transmit tension and shear $β = 2$

Nominal shear resistance of concrete, V_n , is calculated as follows:

Development Length of Reinforcement

The flexural reinforcing steel must be developed on each side of the critical section for its full development length. **LRFD 5.10.8.1.2** Available length for rebar development d.available $=$ l_{heel} – Cover_{ft} = 44 in Basic development length $db \coloneqq 2.4 \cdot d_{bar}$ f y f_c ·ksi $t = 2.4 \cdot d_{\text{bar}} \cdot \frac{y}{\sqrt{2}} = 5.196 \text{ ft}$ **LRFD Eq. 5.10.8.2.1a-2** Reinforcement location factor λ_{r1} = 1.3 More than 12 in. concrete below Coating factor $\lambda_{\text{cf}} = 1.5$ Epoxy coated bars with less than 3d_b cover Reinforcement confinement factor $\lambda_{\text{rc}} = 0.4$ For $c_b > 2.5$ in. and No. 8 bars or smaller $\lambda_{\rm er}$ A_{sRequired} Excess reinforcement factor $\lambda_{\text{er}} = \frac{1}{A_{\text{sProvided}}} = 0.201$ **LRFD Eq. 5.10.8.2.1c-4** Factor for normal weight concrete $\lambda = 1$ $1_{\text{d,required}} := 1_{\text{db}} \cdot \frac{(\lambda_{\text{r1}} \cdot \lambda_{\text{c} \text{f}} \cdot \lambda_{\text{rc}} \cdot \lambda_{\text{er}})}{\lambda} = 9.754 \cdot \text{in}$ **LRFD Eq.**
5.10.8.2.1a-1 $(\lambda_{\rm rl}\!\cdot\!\lambda_{\rm cf}\!\cdot\!\lambda_{\rm rc}\!\cdot\!\lambda_{\rm er})$ Required development length $l_{\text{d},\text{required}} := l_{\text{db}} \cdot \frac{l_{\text{d},\text{required}}}{\lambda} = 9.754 \cdot \text{in}$ Check if $l_{d.available} > l_{d.required}$ $\qquad \qquad$ Check := if $(l_{d.available} > l_{d.required}, "OK", "Not OK") = "OK"$

145

Shrinkage and Temperature Reinforcement Design

The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing. The reinforcement along the longitudinal direction of the footing at the top and bottom should satisfy the shrinkage and temperature reinforcement requirements. **LRFD 5.10.6** The spacing of shrinkage and temperature reinforcement shall not exceed the following: **LRFD 5.10.6**

12 in. for walls and footings greater than 18 in.

Note: MDOT limits reinforcement spacing to a maximum of 18 in. **BDG 5.16.01 and 5.22.01**

Select a trial bar size bar $= 6$

Nominal diameter of a reinforcing steel bar $d_{\text{bST}} = \text{Dia}(\text{bar}) = 0.75 \cdot \text{in}$

Select a spacing for reinforcing steel bars $s_{\text{barST}} = 12$ in

Reinforcing steel area provided in the section

Required minimum area of shrinkage and temperature reinforcement in the footing

Check if the provided steel area > the required area for shrinkage and temperature steel

Cross-section area of the bar A_{barST} : = Area (bar) = 0.44 · in² A_{barST} 12in sbarST $= \frac{PbarST^{-12}m}{T} = 0.44 \cdot in^2$

$$
A_{\text{shrink.temp}} = 0.319 \cdot \text{in}^2
$$

Check := if $(A_{sProvidedST} > A_{shrink.temp}$, "OK", "Not OK" $) =$ "OK"

The footing design presented in this step provides the following details:

- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the transverse flexural reinforcement at the top of the footing
- No. 8 bars @ 12.0 in. spacing $(A_s = 0.79 \text{ in.}^2/\text{ft})$ as the transverse flexural reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.

Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

References

MDOT Geotechnical Manual (2019).

https://www.michigan.gov/-/media/Project/Websites/MDOT/Programs/Bridges-and-Structures/Geotechnical-Services /Geotechnical-Manual.pdf?rev=00901c15702e4493963ee866d0ed4c01 (Last accessed: 09/30/2022)

Stark, T. D., Arellano, D., Horvath, J. S., and Leshchinsky, D. (2004). "Geofoam Applications in the Design and Construction of Highway Embankments," the National Cooperative Highway Research Program, the Transportation Research Board, Washington, D.C. 20001

https://trb.org/publications/nchrp/nchrp_w65.pdf (Last accessed: 09/30/2022)

Section 4 Abutment with Piles

Step 4.1 Preliminary Abutment Dimensions

Description

 \blacktriangleright

This step presents the selected preliminary abutment dimensions.

The design criteria, bridge information, material properties, reinforcing steel cover requirements, soil types and properties, along with superstructure loads are taken from Section 2.

148

This section presents the design of a full-depth reinforced concrete cantilever abutment with pile supports.

The structural design of the backwall and abutment wall is presented in Section 2. The pile design presented in this example covers structural design aspects assuming that the geotechnical design is performed by the Geotechnical Services Section.

The designers select the preliminary dimensions based on state-specific standards and past experience. The following figure shows the abutment geometry and dimensional variables:

Step 4.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of the future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$
DC_{Sup} := \frac{2 \cdot R_{DCEx} + (N_{beams} - 2) \cdot R_{DCIn}}{L_{abut}} = 5.658 \cdot \frac{kip}{ft}
$$

\n
$$
DW_{Sup} := \frac{2 \cdot R_{DWEx} + (N_{beams} - 2) \cdot R_{DWIn}}{L_{abut}} = 0.886 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{backwall} := h_{backwall} \cdot t_{backwall} \cdot W_{c} = 0.956 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{wall} := h_{wall} \cdot t_{wall} \cdot W_{c} = 8.332 \cdot \frac{kip}{ft}
$$

\n
$$
DC_{foothing} := B_{foothing} \cdot t_{foothing} \cdot W_{c} = 4.95 \cdot \frac{kip}{ft}
$$

Step 4.3 Application of Live Load

Description

 \blacktriangleright

Please refer to Step 2.3 for the application of live load on the structure.

Step 4.4 Application of Other Loads

Description

 \blacktriangleright

This step typically includes the calculation of braking force, wind load, earth load, and temperature load.

Since piles and a pile cap are selected to replace the spread footing in Section 2, all other dimensions of the abutment remain consistent. Only the calculation of the earth load is different from Step 2.4. Therefore, please refer to Step 2.4 for the rest of the calculations.

154

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. The hydrostatic pressure should be avoided, if possible, at abutments and retaining walls through the design of an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral loads due to earth pressure are calculated.

Backwall

Live Load Surcharge

Live load surcharge is applied to account for a vehicular live load acting on the backfill surface within a distance equal to one-half the wall height behind the back face of the wall.

Height of the abutment $h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} = 24.79 \text{ ft}$ Equivalent height of soil for vehicular load $h_{eq} = 2ft$ **LRFD Table 3.11.6.4-1** Lateral surcharge pressure $\sigma_p := k_a \gamma_s \cdot h_{eq} = 0.072 \cdot \text{ksf}$ **LRFD Eq. 3.11.6.4-1** Backwall Lateral load $P_{LSBackwall} := \sigma_p \cdot h_{backwall} = 0.306 \cdot \frac{kip}{ft}$ $:= \sigma_{\mathbf{n}} \cdot h_{\text{backwall}} = 0.306$ Abutment Wall Lateral load
Lateral load
 $P_{LSWall} = \sigma_p \cdot (h_{backwall} + h_{wall}) = 1.569 \cdot \frac{kip}{ft}$ Footing Lateral load $P_{LSFoothing} := \sigma_p \cdot (h_{backwall} + h_{wall} + t_{footing}) = 1.785 \cdot \frac{kip}{ft}$ $\tau = \sigma_{\mathbf{n}} \cdot (h_{\mathbf{backwall}} + h_{\mathbf{wall}} + t_{\mathbf{footino}}) = 1.785$ Vertical load $V_{LSFoothing} = \gamma_s \cdot l_{heel} \cdot h_{eq} = 1.58 \cdot \frac{kip}{ft}$ $:= \gamma_{s} \cdot l_{\text{heel}} \cdot h_{\text{eq}} = 1.58$

LRFD 3.11.6.4

Step 4.5 Combined Load Effects

Description

 \blacktriangleright

This step describes the procedure for combining all load effects and calculating the total factored forces and moments acting at the base of the backwall, abutment wall, and footing.

The total factored forces and moments at the base of the backwall and abutment wall are similar to the ones in Step 2.5. Therefore, this step only shows the calculation of the total factored forces and moments at the base of the footing.

156

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered. In addition to all the loads considered for the abutment wall, weight of soil (earth load) on the toe and heel, along with live load surcharge on the heel, are considered.

LRFD 3.6.2.1

The dynamic load allowance is excluded from the live load for foundation components that are located entirely below the ground level.

Strength I

Strength I = $1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU$

Load Case I

Factored vertical force at the base of the footing

$$
F_{VFLC1StrI} := 1.25 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 41.846 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the

Factored shear force parallel to the
 $V_{\text{uFtLClStrI}} \coloneqq 1.5 \cdot P_{\text{EHFooting}} = 16.593 \cdot \frac{\text{kip}}{\text{ft}}$ $= 1.5 \cdot P_{\text{FHfooting}} = 16.593$

LRFD 3.4.1

The vertical earth load of the backfill soil reduces the critical moment about the footing longitudinal axis. This requires using the minimum load factor of 1.0 for EV instead of the factor 1.35 in the Strength I combination.

This is the same for the moment calculated about the longitudinal axis of the footing for all the load cases and limit states.

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLCIStrI}} := 1.25 \cdot \text{DC}_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 \text{DC}_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backward}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} + 1.35 \text{EV}_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{toe}}}{2} \right) \dots + 1.0 \cdot \text{EV}_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right)
$$

$$
M_{\text{uFtLCIStrI}} = 133.008 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Load Case III

Factored vertical force at the base of the footing

 $F_{\text{VFitLC3StrI}} \coloneqq 1.25 \cdot \left(\text{DC}_{\text{Sup}} + \text{DC}_{\text{backwall}} + \text{DC}_{\text{wall}} + \text{DC}_{\text{foothing}} \right) + 1.5\text{DW}_{\text{Sup}} + 1.75\text{R}_{\text{LLFoothingMax}}$ $+1.35\cdot(EV_{earthBk} + EV_{earthFt})$ $\mu = 1.25 \cdot (DC_{S11D} + DC_{\text{backwall}} + DC_{\text{wall}} + DC_{\text{foothing}}) + 1.5DW_{S1D} + 1.75R_{\text{I}}$ Footing May ...

$$
F_{\text{VFtLC3StrI}} = 59.798 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the footing
$$
V_{\text{uFtLC3StrI}} \approx 1.5 \cdot P_{\text{EHFooting}} = 16.593 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3StrI}} := 1.25 \cdot DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(1.25 \cdot DC_{\text{Sup}} + 1.5 \cdot DW_{\text{Supp}} + 1.75 \cdot R_{\text{LLFootingMax}} \right) \cdot \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} \dots + 1.0 \cdot EV_{\text{earthBk}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.35 \cdot EV_{\text{earthFt}} \cdot \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{tot}}}{2} \right)
$$

$$
M_{\text{uFtLC3StrI}} = 194.344 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force at the base of the footing

$$
F_{VFLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing}) + 1.5DW_{Sup} ...
$$

+ 1.35 \cdot $(EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFoding}$

$$
F_{\text{VFtLC4StrI}} = 53.013 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the
transverse axis of the footing
$$
V_{\text{uFtLC4StrI}} := 1.5 \cdot P_{\text{EHFooting}} + 1.75 P_{\text{LSFooting}} + 0.5 \text{TU} = 19.855 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC4StrI}} \coloneqq 1.25 \cdot \text{DC}_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + 1.25 \text{DC}_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + (1.25 \cdot \text{DC}_{\text{Sup}} + 1.5 \cdot \text{DW}_{\text{Sup}}) \cdot \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.5 \cdot P_{\text{EHFooting}} \cdot \frac{\left(I_{\text{hackwall}} + I_{\text{wall}} + t_{\text{footing}} \right)}{3} + 1.75 \cdot \text{V}_{\text{LSFooting}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.75 \cdot P_{\text{LSFooting}} \cdot \frac{\left(I_{\text{hackwall}} + I_{\text{wall}} + t_{\text{footing}} \right)}{2} + 1.0 \cdot \text{EV}_{\text{earthBk}} \cdot \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + 1.35 \cdot \text{EV}_{\text{earthFt}} \cdot \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{top}}}{2} \right) + 0.5 \cdot \text{TU} \cdot \left(I_{\text{wall}} + t_{\text{footing}} \right) + 0.5 \cdot \text{TU} \cdot \left(I_{\text{wall}} + t_{\text{footing}} \right) + 0.5 \cdot \text{TU} \cdot \left(I_{\text{wall}} + t_{\text{footing}} \right)
$$
\n
$$
M_{\text{uFtLC4StrI}} = 197.175 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$

Service I

Service $I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU$

Load Case I

Factored vertical force at the base of the footing

$$
F_{VFLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 32.052 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the Factored shear force parallel to the
transverse axis of the footing $V_{\text{uFtLClSerI}} = P_{\text{EHFooting}} = 11.062 \cdot \frac{\text{kip}}{\text{ft}}$ $:= P_{\text{FHEooting}} = 11.062$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLCISerI}} \coloneqq DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) + DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) \dots
$$

$$
+ P_{\text{EHFooting}} \left(\frac{l_{\text{hackwall}} + h_{\text{wall}} + t_{\text{foothing}}}{3} \right) \dots
$$

$$
+ EV_{\text{earthBk}} \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{to}}}{2} \right)
$$

$$
M_{\text{uFtLCISerI}} = 80.288 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case III

Factored vertical force at the base of the footing

$$
F_{VFLC3SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFoothingMax} ... + (EV_{earthFt} + EV_{earthBk})
$$

$$
F_{\text{VFtLC3SerI}} = 44.053 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored shear force parallel to the transverse axis of the footing
$$
V_{\text{uFtLC3SerI}} := P_{\text{EHFooting}} = 11.062 \cdot \frac{\text{kip}}{\text{ft}}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC3SerI}} \coloneqq DC_{\text{backwall}} \left(l_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) + DC_{\text{wall}} \left(l_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{foothing}}}{2} \right) \dots
$$

$$
+ \left(DC_{\text{Sup}} + DW_{\text{Sup}} + R_{\text{LLFootingMax}} \right) \left(l_{\text{heel}} + l_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) \dots
$$

$$
+ P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} \dots
$$

$$
+ EV_{\text{earthBk}} \cdot \left(\frac{l_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \cdot \left(\frac{B_{\text{footing}}}{2} - \frac{l_{\text{toe}}}{2} \right)
$$

$$
M_{\text{uFtLC3SerI}} = 121.293 \cdot \frac{kip \cdot ft}{ft}
$$

Load Case IV

Factored vertical force at the base of the footing

$$
F_{VFLC4SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{foothing} + DW_{Sup} ...
$$

+
$$
EV_{earthFt} + EV_{earthBk} + V_{LSFoothing}
$$

$$
F_{VFLC4SerI} = 40.176 \cdot \frac{kip}{ft}
$$

Factored shear force parallel to the
transverse axis of the footing

$$
V_{uFtLC4SerI} := P_{EHFoothing} + P_{LSFoothing} + TU = 13.124 \cdot \frac{kip}{ft}
$$

Factored moment about the longitudinal axis of the footing

$$
M_{\text{uFtLC4SerI}} \coloneqq DC_{\text{backwall}} \left(I_{\text{heel}} + \frac{t_{\text{backwall}}}{2} - \frac{B_{\text{footing}}}{2} \right) + DC_{\text{wall}} \left(I_{\text{heel}} + \frac{t_{\text{wall}}}{2} - \frac{B_{\text{footing}}}{2} \right) \dots + \left(DC_{\text{Sup}} + DW_{\text{Sup}} \right) \left(I_{\text{heel}} + I_{\text{brtowall}} - \frac{B_{\text{footing}}}{2} \right) + P_{\text{EHFooting}} \cdot \frac{\left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} \right)}{3} \dots + EV_{\text{earthBk}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + EV_{\text{earthFt}} \left(\frac{B_{\text{footing}}}{2} - \frac{I_{\text{toe}}}{2} \right) \dots + V_{\text{LSFooting}} \left(\frac{I_{\text{heel}}}{2} - \frac{B_{\text{footing}}}{2} \right) + P_{\text{LSFooting}} \cdot \frac{\left(h_{\text{backward1}} + h_{\text{wall}} + t_{\text{footing}} \right)}{2} \dots + TU \cdot \left(h_{\text{wall}} + t_{\text{footing}} \right)
$$
\n
$$
M_{\text{uFtLC4SerI}} = 126.982 \cdot \frac{\text{kip} \cdot ft}{ft}
$$

Summary of Forces and Moments at the Base of the Footing

Factored vertical force, F_{VFt} (kip/ft)

Factored shear force parallel to the transverse axis
of the footing, $V_{\text{uFt}}(\text{kip/ft})$

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/t)

Step 4.6 Pile Size and Layout Design

Description

This step presents the pile type, size, and preliminary layout.

This example uses steel H piles since it is the most commonly used pile type in Michigan. Typically, the pile type is selected after evaluating other possibilities, such as ground improvement techniques, other foundation types, and constructability. Pile embedment into the footing Pile embd $:= 6$ in **BDM 7.03.09.A5** Note: A tremie seal is not used for this footing. If a tremie seal is used, the pile embedment into the footing is 1 ft. A tremie seal design is given in Appendix 4.A. The following parameters are considered to determine the pile layout: 1. Pile spacing: The depth of commonly used H-piles ranges from 10 to 14 inches. **LRFD 10.7.1.2** The minimum pile spacing is controlled by the greater of 30 inches or 2.5 times the pile diameter. As a practice, MDOT uses 3 times the pile diameter as the spacing. Selected pile section HP 12X53 $b_f = 12.0$ in $d_{\text{pile}} = 11.8$ in Minimum spacing (3d_{pile}) Spacing_{min} := $3 \cdot d_{\text{pile}} = 2.95 \text{ ft}$ 2. Edge distance: The usual minimum edge distance for piles is 18 inches. **BDM 7.03.09.A7** Pile edge distance PileEdgeDist := 18in Use two rows of piles. $L_{\text{footing}} - 2$ PileEdgeDist Maximum number of piles in each row N_{MaxPiles} $\frac{21.271}{2}$ = 21.271 Spacing_{min} the footing can accommodate Spacing between two rows $S_B := B_{footing} - 2 \cdot \text{PileEdgeDist} = 8 \text{ ft}$ The loads acting on the two rows of piles are determined as follows: Load Case III under the Strength I limit state is identified as the governing load case by examining the summary tables presented at the end of Step 4.5. Therefore: Total vertical force $P_{\text{vert}} = F_{\text{VFtLC3StrI}} \cdot L_{\text{footing}} = 3.932 \times 10^3 \cdot \text{kip}$ Total moment about the Total moment about the

longitudinal axis of the footing M_{long} := $M_{uFtLC3StrI}$ L footing = 1.278 × 10⁴·kip·ft P_{vert} B S_B R_B Total vertical loads on each row of piles are calculated based on static equilibrium. $\bigg\{M_{\text{long}} + P_{\text{vert}}\bigg\}$ $S_{\bf B}$ \setminus $\overline{}$ $M_{long} + P_{vert}$ \setminus J 2 $R_{\rm B} = \frac{(8.56 \times 10^{3} \text{ kg})}{S_{\rm B}} = 3.563 \times 10^{3} \text{ kip}$ $R_{\rm B} = P_{\rm vert} - R_{\rm rv} = 368.598 \text{ kip}$ R_{rv} $S_{\bf B}$

Check if the spacing of the piles is greater than $3d_{\text{pile}}$

Piles in the Back Row

Number of pile selected for the back row $N_{\text{back}} =$

Selected pile spacing $BackPileSpacing := 10ft + 5.5in = 125.5 \cdot in$

Select 7 back row piles spaced at 10 ft 5.5 in.

Note: As per the AASHTO LRFD Article 10.7.5, the effects of corrosion and deterioration from environmental conditions shall be considered in the selection of the pile type and cross-section. The soil conditions should be examined to ensure that there is no indication of contamination that would cause piles to corrode. Consult the Geotechnical Services Section to determine a suitable pile type and cross-section for the selected site.

The preliminary pile layout is shown in the following figure.

Step 4.7 Pile Capacity Check

Description

This step presents the pile axial and lateral load calculations along with pile capacity checks.

Strength I Limit State

Load Case I

Total vertical load $P_{\text{vert}} = F_{\text{VFtLC1Str1}} L_{\text{footing}} = 2.751 \times 10^3$ kip Total shear force parallel to the Total shear force parallel to the
transverse axis of the footing $P_{\text{lat}} = V_{\text{uFtLC1Str1}} L_{\text{footing}} = 1.091 \times 10^3$ kip Total moment about the longitudinal axis of the footing $M_{long} := M_{uFtLC1StrI}L_{footing} = 8.745 × 10³ kip·ft$

The total vertical loads on the front and back row of piles are calculated based on the static equilibrium of the footing.

$$
R_{rv} := \frac{\left(M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_B} = 2.469 \times 10^3 \cdot \text{kip} \qquad R_B := P_{vert} - R_{rv} = 282.533 \cdot \text{kip}
$$

R_{rv} SingleLC1StrI

Vertical component of the axial force on a front row battered pile

Axial force on a front row battered pile

Pile section selected in Step 4.6 HP 14X73

Factored nominal pile resistance $R_{\rm D} = 250$ kip

Check if R_R > Axial force

Horizontal component of the axial force on a front row battered pile

Total lateral force resisted by the battered piles (i.e. the horizontal component of the axial force)

The required lateral load resistance

of a pile

$$
R_R = 250^{\circ} \text{Kip}
$$

\nCheck := if $(R_R > R_r_SingleLC1StrI, "OK", "Not OK") = "OK"$
\n
$$
R_{rh_SingleLC1StrI} := \frac{R_r_SingleLC1StrI}{\sqrt{Pi_0} \sqrt{Pi_0^2 + 1^2}} = 51.435 \cdot \text{kip}
$$

 R_{rv} n_{front}

 $R_{r_SingleLC1StrI} \coloneqq R_{rv_SingleLC1StrI}$

 $\frac{1}{15} = \frac{154.304 \cdot \text{kip}}{154.304 \cdot \text{kip}}$

PHBatteredPiles $=$ R_{rh} SingleLC1StrI nfront $=$ 822.952 kip

Check if the lateral load capacity of the battered piles is greater than the lateral load demand **BDM 7.03.09.A.11**

Pile_{batter}² + 1²

Pile_{batter}

 $=$ R_{rv} SingleI $C1$ StrI $\frac{V}{R}$ = 162.65 kip

Check := if $(P_{HBatteredPiles} > P_{lat}$, "Yes", "No, check if the vertical piles can resist the remaining later load"

 $Check = "No, check if the vertical piles can resist the remaining later load"$

Note: Per MDOT practice, the typical lateral resistance of a vertical pile is 12 kips. A pile bending (p-y) analysis may be performed by incorporating soil-pile interaction to determine the more accurate lateral load resistance of the piles. Consult the Geotechnical Services Section for more information.

$$
P_{latRegd_LC1StrI} := \frac{(P_{lat} - P_{HBatteredPiles})}{(N_{front} + N_{back})} = 11.653 \cdot kip
$$

Lateral load resistance of a pile (from Eateral bad resistance of a plie (hold P at Provided $= 12$ kip the Geotechnical Services Section)

Check if the lateral load resistance > Check is used at resistance \ge Check if $(P_{latProvided} > P_{latRegd_LC1StrI}$, "OK", "Not OK" $) = "OK"$ the required lateral load resistance

Vertical force on a back row pile

Check if R_R > Axial force

Load Case III

Total shear force parallel to the transverse axis of the footing

Total moment about the longitudinal axis of the footing

The total vertical loads on the front and back row of piles are calculated based on static equilibrium of the footing.

$$
R_{rv} := \frac{\left(M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_B} = 3.563 \times 10^3 \cdot \text{kip} \qquad R_B := P_{vert} - R_{rv} = 368.598 \cdot \text{kip}
$$

Vertical component of the axial force on a front row battered pile
$$
R_{\text{rv}_\text{SingleLC3StrI}}
$$

Axial force on a front row

Check if R_R > Axial force

Horizontal component of the axial force on a front row battered pile

Total lateral force resisted

Rrv nfront 222.695 kip battered pile Rr_SingleLC3StrI Rrv_SingleLC3StrI Pilebatter ² ¹ 2 Pilebatter 234.741 kip Rr_SingleLC3StrI Pilebatter ² ¹ 2 74.232 kip

Total lateral force resisted
by the battered piles

$$
P_{HBatteredPiles} := R_{rh_SingleLC3StrI} \cdot n_{front} = 1.188 \times 10^3 \cdot kip
$$

Check if the lateral load capacity of the battered piles is greater than the lateral load demand\nCheck := if (P_{HB}atteredPiles > P_{lat}, "Yes", "No, check if the vertical piles can resist the remaining later load") = "Yes"\nThe required lateral load resistance\n
$$
P_{latRegd_LC3StrI} := 0
$$
\nof a pile\nVert\n\nVert
$$
R_B_{SingleLC3StrI} := \frac{R_B}{N_{back}} = 52.657 \cdot kip
$$
\nCheck if R_R > Axial force\nCheck if R_R > Axial force\nCheck if R_R is in the image.

Vertical force on a back row pile
\n
$$
R_{B_SingleLC1StrI} := \frac{R_B}{N_{back}} = 40.362 \cdot kip
$$

\nCheck if $R_R > Axial$ force
\n $ext{C$ back $=$ if $(R_R > R_{B_SingleLC1StrI}, "OK", "Not OK") = "OK"\n $P_{vert} := F_{VFLC3StrI} \cdot L_{foothing} = 3.932 \times 10^3 \cdot kip$
\nTotal shear force parallel to the
\ntransverse axis of the footing
\n $P_{lat} := V_{uFtLC3StrI} \cdot L_{foothing} = 1.091 \times 10^3 \cdot kip$$

$$
M_{long} := M_{\text{uFtLC3StrI}} L_{\text{footing}} = 1.278 \times 10^4 \cdot \text{kip·ft}
$$

$$
R_B := P_{vert} - R_{rv} = 368.598 \cdot kip
$$

Load Case IV

The total vertical loads on the front and back row of piles are calculated based the static equilibrium of the footing.

$$
R_{rv} := \frac{\left(M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_B} = 3.363 \times 10^3 \cdot \text{kip} \qquad R_B := P_{vert} - R_{rv} = 122.275 \cdot \text{kip}
$$

Vertical component of the axial force on a front row battered pile

Axial force on a front row

Check if R_R > Axial force

Horizontal component of the axial force on a front row battered pile

battered pile

$$
R_{\text{rv_SingleLC4StrI}} := \frac{R_{\text{rv}}}{n_{\text{front}}} = 210.209 \text{ kip}
$$

$$
R_{r_SingleLC4StrI} := R_{rv_SingleLC4StrI} \cdot \frac{\sqrt{Pile_{batter}^2 + 1^2}}{Pile_{batter}} = 221.58 \cdot kip
$$

Check := if
$$
(R_R > R_r \cdot SingleLC4StrI, "OK", "Not OK") = "OK"
$$

$$
R_{rh_SingleLC4StrI} := \frac{R_{r_SingleLC4StrI}}{\sqrt{\text{Pile}_{batter}^2 + 1^2}} = 70.07 \cdot \text{kip}
$$

Total lateral force resisted by
the battered piles
$$
P_{HBatteredPiles} := R_{rh_SingleLC4StrI} \cdot n_{front} = 1.121 \times 10^3 \cdot kip
$$

Check if the lateral load capacity of the battered piles is greater than the lateral load demand **BDM 7.03.09.A.11**

Check := if $(P_{HBatteredPiles} > P_{lat}$, "Yes", "No, check if the vertical piles can resist the remaining later load"

 $Check = "No, check if the vertical piles can resist the remaining later load"$

The required lateral load resistance of a pile

Lateral load resistance of a pile (from Eateral load resistance of a plie (from
 P latProvided = 12 kip
 P latProvided = 12 kip

Check if the lateral load resistance > the required lateral load resistance

Vertical force on a back row pile

$$
P_{latRegd_LC4StrI} := \frac{(P_{lat} - P_{HBatteredPiles})}{(N_{front} + N_{back})} = 8.015 \cdot kip
$$

Check := if
$$
(P_{latProvided} > P_{latRegd LC1StrI}, "OK", "Not OK") = "OK"
$$

$$
R_{B_SingleLC4StrI} := \frac{R_B}{N_{back}} = 17.468 \cdot kip
$$

Check if R_R > Axial force Check := if $(R_R > R_B \text{SingleLC4StrI}$, "OK" , "Not OK" $) =$ "OK"

Summary of Forces Acting on a Single Pile

A summary of forces acting on a single pile under different Strength I limit state load cases is listed in the following tables. The pile penetration depth design, driveability analysis, and settlement analysis are performed by the Geotechnical Services Section to evaluate the adequacy of the selected design.

Axial force on a battered pile in the Axial force on a pile in diversion a back row (kip) front row (kip) front row (kip)

 $\overline{\Gamma}$

Required lateral force resistance of a pile (kip)

Step 4.8 Backwall Design

Description

Since the backwall forces and moments used in Step 2.7 are not impacted by the use of piles, please refer to the design calculations and details presented in Step 2.7.

Step 4.9 Abutment Wall Design

Description

Since the abutment wall forces and moments used in Step 2.8 are not impacted by the use of piles, please refer to the design calculations and details presented in Step 2.8.

Step 4.10 Structural Design of the Footing

Description

This step presents the structural design of the abutment footing.

Note: In this example, the length of the footing and the abutment wall are 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Design for Flexure

In a typical spread footing, the critical section for flexure, due to the loads acting on the toe, is at the front face of the wall. As shown below, since the front row piles are located behind the critical section, the flexural capacity of the pile cap is not evaluated.

For the heel of the footing, the critical section is located at the back face of the wall. The footing is designed considering the flexural demand at this section since the back row of piles is located closer to the edge of the heel.

As per the summary tables presented at the end of Step 4.7, the maximum and minimum Strength I limit state axial forces at the back row piles are from LC III and LC IV, respectively.

Bottom of the footing stresses at the critical section

The tension at the bottom of the footing is developed due to the axial forces at the back row piles. The self-weight of the footing and the vertical earth load on the heel develop the resisting moment. For a safe design, the maximum axial load at the back row piles is used with the minimum load factors for the resisting forces.

The minimum load factors for dead load and earth load are 0.9 and 1.0, respectively. **LRFD Table 3.4.1-2**

The maximum moment at the critical section to develop tension at the bottom of the footing

$$
M_{rb} := \frac{R_{backMax} \cdot d_{arm}}{L_{footing}} - 0.9 W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} - EV_{earthBk} \cdot \frac{l_{heel}}{2} = -36.942 \cdot \frac{kip \cdot ft}{ft}
$$

The negative moment does not require a design for the flexural reinforcement at the bottom of the footing.

Top of the footing stresses at the critical section

Load case IV under the Strength I limit state develops the minimum axial force at the back row piles. The same load case develops the maximum vertical downward loads on the heel due to self weight of the footing, vertical earth load, and live load surcharge.

The maximum moment at the critical section to develop tension at the top of the footing

$$
M_{rt} \coloneqq 1.25 W_c \cdot t_{footing} \cdot \frac{l_{heel}^2}{2} + 1.35 EV_{earthBk} \cdot \frac{l_{heel}}{2} + 1.75 V_{LSFooting} \cdot \frac{l_{heel}}{2} - \frac{R_{backMin} \cdot d_{arm}}{L_{footing}} = 88.333 \cdot \frac{kip \cdot ft}{ft}
$$

Flexure Resistance LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

assumed initial A_s value to solve the equation.

The initial assumption for A_s $A_s := 1in^2$

176

Required steel area

\nRequired steel area

\n
$$
A_{sRequired} = \text{Find}(A_{s}) = 0.625 \cdot \text{in}^{2}
$$
\nCheck if A_{sProduct} > A_{sRequired}

\n
$$
A_{sRequired} = \text{Find}(A_{s}) = 0.625 \cdot \text{in}^{2}
$$
\nCheck: = if (A_{sProduct} > A_{sRequired}, "OK", "Not OK") = "OK" and (A_{sProduct} > A_{sRequired})

\n
$$
M_{provided} = \text{if}(A_{sProduct} > A_{sProduct} > A_{sRequired}, "OK", "Not OK") = "OK" and (A_{sProduct} > A_{sProduct} > A_{sRequired} > A
$$

Limits for Reinforcement LRFD 5.6.3.3

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Control of Cracking by Distribution of Reinforcement LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to see the tension face

Exposure factor for the Class 1 exposure

condition $\gamma_e := 1.00$

Distance from extreme tension fiber to the Distance from extreme tension inter to the dc d_c := Coverft = 4 in center of the closest bar

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

700 $\cdot \gamma_e$ $\leq \frac{1}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$ **LRFD Eq. 5.6.7-1**

 $\beta_{\rm s} \coloneqq 1$ $d_{\mathbf{c}}$ $= 1 + \frac{1}{0.7 (\text{tfooting} - \text{d}_\text{c})} = 1.179$

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, f_{ss} , requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme Assumed distance from the extreme
compression fiber to the neutral axis $x := 5 \cdot in$

Given
$$
\frac{1}{2} \cdot b \cdot x^2 = \frac{E_s}{E_c} \cdot A_{sProvided} \cdot (d_e - x)
$$

 $x_{na} := \text{Find}(x) = 5.303 \cdot \text{in}$

Position of the neutral axis x_{na}

The axial force in the back row piles (R_B) from Load Case IV under the Service I limit state is calculated as shown below.

The total vertical loads on the front and back row of piles are calculated based on static equilibrium of the footing.

$$
R_{rv} := \frac{\left(M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_B} = 2.364 \times 10^3 \cdot kip
$$
 $R_B := P_{vert} - R_{rv} = 277.156 \cdot kip$

The moment at the critical section under Service I limit state that generates tension at the top of the footing is:

$$
M_{\text{heelTopSerI}} := W_{\text{c}} \cdot t_{\text{footing}} \cdot \frac{I_{\text{heel}}^2}{2} + EV_{\text{earthBk}} \cdot \frac{I_{\text{heel}}}{2} + V_{\text{LSFooting}} \cdot \frac{I_{\text{heel}}}{2} - \frac{R_{\text{B}} \cdot d_{\text{arm}}}{L_{\text{footing}}} = 50.188 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}
$$
\nTensile force in the reinforcement to the Service I limit state moment

\n
$$
T_{\text{s}} := \frac{M_{\text{heelTopSerI}}}{\frac{X_{\text{na}}}{3}} \cdot \text{ft} = 19.9 \cdot \text{kip}
$$

Stress in the reinforcing steel due to the Service I limit state moment f_s

 f_{ss} (not to exceed 0.6f_y)

$$
F_{\text{ss1}} := \frac{T_{\text{s}}}{A_{\text{sProvided}}} = 25.216 \text{ k} \cdot \text{ksi}
$$

$$
f_{ss}
$$
 := min $(f_{ss1}, 0.6f_v)$ = 25.216 ksi

 $700 \cdot \gamma_e \cdot \frac{kip}{in}$ $\ddot{}$

 $=$ $\frac{m}{\beta_s f_{ss}} - 2 \cdot d_c = 15.554 \cdot in$

Check := if $(s_{bar} < bar_{spaReq}$, "OK" , "Not OK" $)$ = "OK"

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement LRFD 5.10.6

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the heel:

Design for Shear

Shear design in abutment footings supported by piles provides adequate resistance against one-way action (beam action shear) and two-way action (punching shear). For both one-way and two-way actions, the design shear is taken at the critical section. For abutment footings, one-way action is checked at the toe and heel. The factored shear force at the critical section is computed by cutting the footing at the critical section and taking the summation of the pile loads or portions of pile loads that are outside the critical section. Two-way action in abutment footings supported by piles is generally checked by taking a critical perimeter around individual piles or around a group of piles when the critical perimeter of individual piles overlap.

One-way Shear

For one-way shear on the toe side, a shear check at the critical section or towards the toe is not required since the front row of piles is inside the critical section.

On the heel side, the downward load is larger than the upward axial force at the back row pile. Therefore, the top of the heel is in tension. As a result, the critical section for shear is taken at the back face of the abutment wall.

LRFD C5.12.8.6.1

Effective shear depth $d_v := max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{\text{foothing}} \right) = 31.225 \cdot in$ **LRFD**

The factored shear demand at the critical section for shear:

$$
V_{\text{uFtHeel}} = 1.25 \cdot W_{\text{c}} \cdot t_{\text{footing}} \cdot l_{\text{heel}} + 1.35 \text{EV}_{\text{earthBk}} + 1.75 \text{V}_{\text{LSFooting}} - \frac{R_{\text{backMin}}}{L_{\text{footing}}} = 27.847 \cdot \frac{\text{kip}}{\text{ft}}
$$

sete footing in which the distance from point of zero shear to the face of the

 A _SProvided f_y $0.85 \cdot f_c \cdot b$

 \setminus

 $\frac{1}{1} = \frac{1.549 \cdot in}{1.549 \cdot in}$

For a concrete footing in which the distance from point of zero shear to the face of the wall is less than $3d_v$, the simplified procedure for nonprestressed sections can be used.

Check if $l_{\text{heel}} < 3 d_v$

footing,

$$
Check := if(l_{heel} < 3 \cdot d_v, "Yes", "No"] = "Yes"
$$

 $= max (d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{footing}) = 31.225 \cdot in$

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear $\beta := 2$

Nominal shear resistance of concrete, V_n , is calculated as follows:

The loads on the front piles are assumed to be identical. The critical case fora two-way shear is the piles at the end of the front row since the critical perimeter of these piles may be off the footing in both directions.

 \setminus $\overline{}$

According to the summary tables of the pile axial forces, LC III under the Strength I limit state developed the maximum pile axial force at the front row piles.

Check if the critical perimeter is off the Check if the critical perimeter is off the OffF offFooting $1 := \text{if}$

Check if the critical perimeter is off the footing in the footing length direction

Length of the critical perimeter side parallel to the footing width direction

Length of the critical perimeter side parallel to the footing length direction

Critical perimeter

Ratio of long side to short side of the rectangle through which the concentrated load is transmitted

Nominal shear resistance

Length of the critical perimeter side
\nparallel to the footing width direction
\nparallel to the footing width direction
\n
$$
b_{01} := if \left(\text{OffFooting1 = "Yes", } \frac{d_{\text{pile}}}{2} + \frac{d_{\text{v}}}{2} + \text{PileEdgeDist}, d_{\text{pile}} + d_{\text{v}} \right)
$$
\nLength of the critical perimeter side
\nparallel to the footing length direction
\n
$$
b_{02} := if \left(\text{OffFooting2 = "Yes", } \frac{b_{\text{f}}}{2} + \frac{d_{\text{v}}}{2} + \text{PileEdgeDist}, b_{\text{f}} + d_{\text{v}} \right)
$$
\n
$$
b_{02} = 3.409 \text{ ft}
$$
\nCritical perimeter
\n
$$
b_{0} := (b_{01} + b_{02}) = 6.777 \text{ ft}
$$
\nRatio of long side to short side of the
\nrectangle through which the
\nconcentated load is transmitted
\nNominal shear resistance
\n
$$
V_{n1_2way} := \left(0.063 + \frac{0.126}{\beta_{\text{c}}} \right) \cdot \sqrt{f_{\text{c}} \cdot \text{ksi}} \cdot b_{0} \cdot d_{\text{v}} = 794.229 \cdot \text{kip}
$$
\nLRED Eq.
\n
$$
V_{n2_2way} := 0.126 \cdot \left(\sqrt{f_{\text{c}} \cdot \text{ksi}} \cdot b_{0} \cdot d_{\text{v}} \right) = 554.184 \cdot \text{kip}
$$
\nLRED Eq.
\nFactored shear resistance
\n
$$
V_{\text{r}} \text{2way} := \min \left(V_{n1} \text{2way}, V_{n2_2way} \right) = 554.184 \cdot \text{kip}
$$

 $d_v/2$ HP14X73 \mathbf{N} 5ft 1.5_{ft}

> d_{pile} 2 d_V 2 $+ -$ > PileEdgeDist, "Yes", "No" ſ L $:= \text{if} \left(\frac{P}{2} + \frac{1}{2} > \text{PileEdgeDist}, \text{``Yes''}, \text{``No''} \right)$ \setminus $\overline{}$

OffFooting $1 = "Yes"$

OffFooting2 := if
$$
\left(\frac{b_f}{2} + \frac{d_v}{2} > \text{PileEdgeDist}, \text{``Yes''}, \text{``No''}\right)
$$

OffFooting $2 = "Yes"$
Maximum two-way shear demand R_r SingleLC3StrI = 234.741 kip Check if the factored shear resistance > Check if the factored shear resistance \ge
the maximum pile axial force Check := if $(V_{r_2way} > R_{r_5mgleLC3Str1}$, "OK", "Not OK" $) =$ "OK" **Development Length of Reinforcement** The flexural reinforcing steel must be developed on each side of the critical section for its full development length. **LRFD 5.10.8.1.2** Available development length d.available $=$ l_{heel} – Cover_{ft} = 6.25 ft Basic development length $db \coloneqq 2.4 \cdot d_{bar}$ fy f_c ·ksi $t = 2.4 \cdot d_{\text{bar}} \cdot \frac{y}{\sqrt{2}} = 6.928 \text{ ft}$ **LRFD Eq. 5.10.8.2.1a-2** Reinforcement location factor $\lambda_{r1} = 1.3$ More than 12 in. concrete below Coating factor $\lambda_{\text{cf}} = 1.5$ Epoxy coated bars with less than 3d_b cover Reinforcement confinement factor $\lambda_{\text{rc}} = 0.4$ For $C_b > 2.5$ in. and No. 8 bars or smaller Excess reinforcement factor A_{sRequired} A_sProvided **LRFD Eq. 5.10.8.2.1c-4** Factor for normal weight concrete $\lambda = 1$ Required development length $l_{d.\text{required}} := l_{db} \cdot \frac{(\lambda_{r1} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er})}{\lambda} = 4.278 \text{ ft}$ **LRFD Eq.**
5.10.8.2.1a-1 $(\lambda_{\rm rl}\!\cdot\!\lambda_{\rm cf}\!\cdot\!\lambda_{\rm rc}\!\cdot\!\lambda_{\rm er})$ λ $= 1_{\text{db}} \cdot \frac{(1.1 \times 10^{14} \text{ J s})}{\text{m} \cdot \text{m}} = 4.278 \text{ ft}$ Check if $l_{\text{d.available}} > l_{\text{d.required}}$ Check := if $(l_{\text{d.available}} > l_{\text{d.required}}$, "OK", "Not OK" $) =$ "OK"

Shrinkage and Temperature Reinforcement

The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing.

Select a spacing for reinforcing steel bars

Provided horizontal reinforcement area

Required minimum area of shrinkage and temperature reinforcement in the the footing

Check if the area of steel provided > the required area of shrinkage and temperature steel

$$
s_{barST} := 12 \cdot in
$$

\n
$$
A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{s_{barST}} = 0.44 \cdot in^2
$$

\n
$$
A_{shrink.temp} = 0.306 \cdot in^2
$$

\nCheck := if $(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"$

The footing design presented in this step provides the following details:

- No. 8 bars @ 12.0 in. spacing $(A_s = 0.79 \text{ in.}^2/\text{ft})$ as the transverse flexural reinforcement at the top of the footing
- No. 6 bars ω 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the transverse shrinkage and temperature reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.

Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

Appendix 4.A Tremie Seal Design

Description

This appendix presents the design of a tremie seal.

Generally, tremie seals should be used on all structures when the pumping of water down below the bottom of footing is expected to be challenging. **BDM 7.03.06** A tremie seal shall be designed to resist the hydrostatic pressure at the bottom of the tremie by a combination of its weight and the bond between the cofferdam and piles. The allowable bond strength between the tremie and piles is 10 psi. The allowable bond strength between the tremie and the cofferdam is 5 psi. The allowable tension from the bending of the tremie seal is 30 psi. **BDM 7.03.06A** The design of a tremie seal consists of determining a concrete thickness that will be sufficient, in conjunction with other sources of resistance, to resist the buoyant force at the bottom of the seal. Hydrostatic pressure head is defined from the bottom of a tremie seal up to the ordinary water surface elevation. **BDM 7.03.06B** Consult the Geotechnical Services Section for the hydrostatic pressure head and the related information. Hydrostatic pressure head to the bottom of the footing (from the Geotechnical Services Section) Hwater 10ft γwater 62.4 lb ft3 Unit weight of water Unit weight of tremie concrete γtremie 140 lb ft3 Consider a 1-ft wide strip of the tremie seal. As per the BDM, the cofferdam sheet piling is typically located at 18 in. outside the footing outline. **BDM 7.03.04** Note: It is recommended to evaluate the possibility of battered piles hitting the cofferdam sheet piles during the pile driving operation. Based on the pile layout design, evaluate the space requirements and increase the distance between the footing outline and the cofferdam sheet piles. Use the revised dimensions to calculate the length of the tremie seal. This example uses the following dimensions: Expected sheet pile embedment depth from the top of the tremie seal (an estimate from the Geotechnical Services Section) SPembd 15ft Minimum clearance between the edge of the heel and sheet pile SPclrns_heel 1.5ft Minimum clearance between the edge of the toe and sheet pile SPclrns_toe SPembd Pile_embd Pilebatter 5.167 ft Selected clearance between the edge of the toe and sheet pile SPclrns_select_toe Ceil SPclrns_toe 1ft 6 ft l tremie Bfooting SPclrns_heel SPclrns_select_toe 18.5 ft Length of tremie seal Tremie seal thickness (assumed) htremie 4.25ft Weight of the tremie seal Wtremie γtremie l tremie 1ft htremie 11.008 kip

Bending Stress Check

While checking the flexural stress in the tremie seal, assume that the 1-ft wide tremie seal strip is simply supported at both ends by the cofferdam.

Section modulus of the 1-ft wide strip

$$
S_{\text{tremie}} \coloneqq \frac{1}{6} \cdot h_{\text{tremie}}^2 = 3.01 \cdot \text{ft}^2
$$

 $\frac{20 \text{ cm}}{2}$ = 29.034 · psi

M_{tremie} S_{tremie}

Max. bending moment in the tremie seal

M_{tremie} := $\frac{1}{8}$ [γ _{water} (H_{water} + h_{tremie}) – γ _{tremie} h_{tremie}] · l_{tremie}² = 12.586 · $\frac{kip \cdot ft}{ft}$ ft $\tau = -\frac{1}{2} \gamma_{\text{water}} (H_{\text{water}} + h_{\text{tremie}}) - \gamma_{\text{tremie}} h_{\text{tremie}} |_{\text{tremie}}^2 = 12.586$

Max. tensile stress in the tremie seal

Check if the max. tensile stress is less than 30 psi Check := if $(F_c < 30 \text{psi}, "OK", "Not OK") = "OK"$

Friction Check

Bond strength between tremie and cofferdam pcoffBond = 5psi **BDM 7.03.06A** Bond force between tremie and cofferdam $P_{\text{CoffBond}} := P_{\text{CoffBond}}^2 \cdot 1 \text{ ft} \cdot h_{\text{tremie}} = 6.12 \cdot \text{kip}$

From Step 4.6, the selected pile section HP14x73

Note: For H piles, surface area of a pile is defined using a rectangular shape for a conservative design (i.e. 2 times the sum of the flange width and the section depth).

Bond force between tremie and piles when a 1-ft wide strip is considered

$$
P_{\text{PileBond}} := \text{PpileBond} \cdot \left(\frac{N_{\text{front}}}{L_{\text{footing}}} + \frac{N_{\text{back}}}{L_{\text{footing}}} \right) \cdot 2 \cdot 1 \text{ ft} \cdot \left(b_f + d_{\text{pile}} \right) \cdot h_{\text{tremie}} = 10.06 \cdot \text{kip}
$$
\n
$$
P_{\text{resist}} := W_{\text{tremie}} + P_{\text{CoffBond}} + P_{\text{PileBond}}
$$

Total uplift resistance (ca

Check if the total resistance force >

Buoyant force (demand) $P_{\text{buoy}} = \gamma_{\text{water}} \cdot 1 \text{ft } l_{\text{tremie}} \cdot (H_{\text{water}} + h_{\text{tremie}}) = 16.45 \cdot \text{kip}$

Check if the total resistance force \ge
the buoyant force Check if $(P_{\text{resist}} > P_{\text{buoy}}$, "OK" , "Not OK" $) = "OK"$

 $P_{resist} = 27.188 \cdot kip$ **BDM 7.03.06A**

Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.