DESIGN OF HIGHWAY BRIDGE ABUTMENTS AND FOUNDATIONS

Project Manager: Juan Alcantar, P.E.



Submitted By:

Upul Attanayake, Ph.D., P.E. Presidential Innovation Professor Western Michigan University (269) 276-3217 upul.attanayake@wmich.edu Yufeng Hu, Ph.D., P.E. Master Faculty Specialist Western Michigan University (269) 276-3310 <u>yufeng.hu@wmich.edu</u>



Western Michigan University

Department of Civil & Construction Engineering College of Engineering and Applied Sciences Kalamazoo, MI 49008-5316

May 10, 2023

DISCLAIMER

This publication is disseminated in the interest of information exchange. The Michigan Department of Transportation (hereinafter referred to as MDOT) expressly disclaims any liability, of any kind, or for any reason, that might otherwise arise out of any use of this publication or the information or data provided in the publication. MDOT further disclaims any responsibility for typographical errors or accuracy of the information provided or contained within this information. MDOT makes no warranties or representations whatsoever regarding the quality, content, completeness, suitability, adequacy, sequence, accuracy, or timeliness of the information and data provided, or that the contents represent standards, specifications, or regulations.

ACKNOWLEDGEMENTS

This project is funded by the Michigan Department of Transportation. It is carried out by the Michigan Department of Transportation Center of Excellence for Structural Durability at Western Michigan University. We, the authors, would like to acknowledge Mr. Juan Alcantar as the project manager and the advisory panel members for their assistance in finding relevant information, reviewing the drafts, and responding to our questions in a timely manner to successfully complete this example. We appreciate the contribution of Ms. Kanchani Basnayake and Mr. Harsha Amunugama for the development of this example.

Table of Contents

Section 1 Design Criteria

Section 2 Abutment with Spread Footing

Step 2.1 Preliminary Abutment Dimensions

Step 2.2 Application of Dead Load

Step 2.3 Application of Live Load

Step 2.4 Application of Other Loads

Step 2.5 Combined Load Effects

Step 2.6 Geotechnical Design of the Footing

Step 2.7 Backwall Design

Step 2.8 Abutment Wall Design

Step 2.9 Structural Design of the Footing

Appendix 2.A Braking Force and Wind Load Calculation

Appendix 2.B Sliding Resistance Check for Spread Footings on Clay

Section 3 Abutment with Spread Footing and EPS Backfill

Step 3.1 Preliminary Abutment Dimensions

Step 3.2 Application of Dead Load

Step 3.3 Application of Live Load

Step 3.4 Application of Other Loads

Step 3.5 Combined Load Effects

Step 3.6 Geotechnical Design of the Footing

Step 3.7 Backwall Design

Step 3.8 Abutment Wall Design

Step 3.9 Structural Design of the Footing

Section 4 Abutment with Piles

Step 4.1 Preliminary Abutment Dimensions

Step 4.2 Application of Dead Load

Step 4.3 Application of Live Load

Step 4.4 Application of Other Loads

Step 4.5 Combined Load Effects

Step 4.6 Pile Size and Layout Design

Step 4.7 Pile Capacity Check

Step 4.8 Backwall Design

Step 4.9 Abutment Wall Design

Step 4.10 Structural Design of the Footing

Appendix 4.A Tremie Seal Design

Section 1 Design Criteria



Description

This example illustrates the design of an abutment with shallow and deep (pile) foundations for an interstate freeway bridge. The design is implemented in accordance with the Michigan Department of Transportation

(MDOT) policies published as of 09/30/2022. The requirements of the 9th Edition of the AASHTO LRFD Bridge Design Specification; as modified and supplemented by the Bridge Design Manual (BDM), Bridge Design Guides (BDG), and 2020 Standard Specifications for Construction (SSFC); are followed. Certain material and design parameters are selected to be in compliance with MDOT practice reflected in the Bridge Design System (BDS), the MDOT legacy software.

This step provides the design criteria, the bridge information, material properties, soil types and properties, along with loads from the superstructure analysis.

Page	Content
06	Bridge Information
07	Material Properties
08	Reinforcing Steel Concrete Cover Requirements
08	Soil Types and Properties
08	Loads from Superstructure

Bridge Information

This is a zero-skew, 200-ft long, two-span continuous, interstate freeway bridge. Each span consists of seven steel plate girders spaced at 9 ft - 8 $\frac{5}{8}$ in. on center. The vertical profile and typical cross-section of the bridge are shown below. The girders are designed for composite behavior with a 9-in. thick cast-in-place reinforced concrete deck to resist superimposed dead, live, and impact loads. The superstructure design is presented in the *Two-Span Continuous Bridge Steel Plate Girder Design Example* developed by Attanayake et al. (2021), which is cited in this example as the *Steel Plate Girder Design Example*.

Vertical Profile



Typical Cross-Section



Bridge design span length $L_{span} := 100 \cdot ft$ Number of beams $N_{beams} := 7$ Beam spacing BeamSpacing := 9ft + 8.625in = 9.72 ft $W_{deck} := 63.75$ ft Out-to-out deck width $Rdwy_{width} := 60.5 \cdot ft$ Roadway clear width $N_{lanes} := floor\left(\frac{Rdwy_{width}}{12 \cdot ft}\right) = 5$ Number of design traffic lanes LRFD 3.6.1.1.1 per roadway $t_{\text{Deck}} := 9 \text{in}$ **BDM 7.02.08** Deck slab thickness

Note: The type of barrier used in this example is for illustrative purposes only. It is the section used in the *Steel Plate Girder Design Example* to provide superstructure loads for this design. The BDG provides standard barrier section details.

Height of bridge railing	$h_{\text{Railing}} := 3 \text{ft} + 4 \text{in} = 3.33 \text{ ft}$	
Haunch thickness	t _{Haunch} := 1in	BDM 7.02.19-C
Overall depth of the girder at the abutment support	$d_{Girder} := 35in$	Steel Plate Girder Design Example
Material Properties		
Reinforced concrete unit weight	$W_c := 150 \frac{lb}{ft^3}$	
Concrete 28-day compressive strength	$f_c := 3ksi$	
Concrete density modification factor for normal weight concrete	$\lambda := 1$	LRFD 5.4.2.8
Concrete modulus of rupture	$f_r := 0.24 \cdot \lambda \sqrt{(f_c \cdot ksi)} = 0.42 \cdot ksi$	LRFD 5.4.2.6
Yield strength of reinforcing steel	f _y := 60ksi	
Concrete unit weight	$W_{con} := 145 \frac{lb}{ft^3}$	LRFD Table 3.5.1-1
Correction factor for the source of aggregate	K ₁ := 1	
Concrete modulus of elasticity	$E_{c} \coloneqq 120000 \cdot K_{1} \cdot \left(\frac{W_{con}}{1000 \frac{lb}{ft^{3}}}\right)^{2} \cdot \left(\frac{f}{k}\right)^{3}$	$ \frac{f_c}{s_i} = \frac{0.33}{s_i} \cdot \frac{c_i}{s_i} \frac{c_i}{s_i} + \frac{c_i}{s_i} + \frac{c_i}{s_i} \frac{c_i}{s_i} $
Steel modulus of elasticity	$E_{c} = 3.63 \times 10^{3} \cdot \text{ksi}$ $E_{c} = 29000 \text{ksi}$	
Nominal diameter and cross-section area of reinforcing steel bars	0.5in if bar = 4 Area(bar) 0.625in if bar = 5 0.75in if bar = 5 0.75in if bar = 6 0.875in if bar = 7 1in if bar = 8 1.128in if bar = 9 1.27in if bar = 10 1.41in if bar = 11	$:= 0.2in^{2} \text{ if } bar = 4$ $0.31in^{2} \text{ if } bar = 5$ $0.44in^{2} \text{ if } bar = 6$ $0.6in^{2} \text{ if } bar = 7$ $0.79in^{2} \text{ if } bar = 8$ $1in^{2} \text{ if } bar = 9$ $1.27in^{2} \text{ if } bar = 10$ $1.56in^{2} \text{ if } bar = 11$

Reinforcing Steel Concrete Cover Requirements

The minimum concrete cover

4 in. for the top and bottom of footing 3 in. for walls against soil

Backwall back cover	Cover _{bw} := 3in
Abutment wall cover	Cover _{wall} := 3in
Footing top and bottom cover	$Cover_{ft} := 4in$

Soil Types and Properties

Bridge designers must interact closely with the Geotechnical Services Section since site conditions may make each substructure design unique.

Soil boring results showed the following soil profile. The Geotechnical Services Section uses this information to determine applicable bearing capacity, settlement, sliding resistance, etc.

Depth (ft)	Soil type	Total unit weight, γs (pcf)	φ', degree
0-25	Fine to coarse sands	120	30
25-75	Gravelly sands	125	36
75-90	Fine to coarse sands	120	30
90-130	Gravels	125	38

The groundwater table is not located within the vicinity of the foundation.

Unit weight of backfill soil

The active lateral earth pressure coefficient



Compacted Sand, LRFD Table 3.5.1-1

BDG 5.16.01, 5.18.01, 5.22.01

Loads from Superstructure

Dead Load

The superstructure dead load reactions at each girder end are taken from the Steel Plate Girder Design Example.

Dead load reactions at the exterior girder end supports	Table 12 of the Steel Plate Girder Design Example
Weight of structural components and non-structural attachments (DC)	$R_{DCEx} := 44.6 kip$
Weight of future wearing surface (DW)	$R_{DWEx} := 8.0 kip$
Dead load reactions at the interior girder end supports	Table 13 of the Steel Plate Girder Design Example
Weight of structural components and non-structural attachments (DC)	$R_{DCIn} := 54.3 kip$
Weight of future wearing surface (DW)	$R_{DWIn} := 8.1 kip$

Live Load

MDOT uses a modified version of the HL-93 loading specified in the LRFD Specifications. A single design truck load, a single 60-kip load (axle load), a two design truck load for continuous spans, and a design lane load are multiplied by a factor of 1.2 to designate the design loading as HL-93 Mod.

Factor for HL-93 Mod	$f_{HL93Mod} := 1.2$	BDM 7.01.04-A
Dynamic load allowance	IM := 0.33	LRFD Table 3.6.2.1-1

According to the calculation presented in the *Steel Plate Girder Design Example*, the truck + lane load combination resulted in the maximum and minimum girder end reactions over the abutment. The unfactored girder support reactions for a single lane loaded case are listed below.

Maximum and minimum girder reactions due to truck load:

 $V_{TruckMax} \coloneqq 63.9 kip \quad V_{TruckMin} \coloneqq -5.9 kip$

Maximum and minimum girder reactions due to lane load:

 $V_{LaneMax} := 28.1 kip$ $V_{LaneMin} := -3.5 kip$

Table A-4 of the Steel Plate Girder Design Example

Table A-4 of the Steel Plate Girder Design Example

Section 2 Design of Abutment with a Spread Footing

Step 2.1 Preliminary Abutment Dimensions

Description

This step presents the selected preliminary abutment dimensions.

The selection of an optimal abutment type depends on the site conditions, cost considerations, superstructure geometry, and aesthetics. The common types include cantilever, counterfort, curtain wall, integral or semi-integral, and spill-through abutments.	BDM 7.03.01
A concrete cantilever abutment is considered optimal for the selected site and the structure.	
 MDOT Bridge Design Manual lists the following minimum requirements: The minimum wall thickness for abutments is 2 ft 	BDM 7.03.01C
 The minimum thickness of footings is normally 2 ft - 6 in. When the wall thickness at its 	DDM 7.02.024
base becomes 3 ft or greater, the footing thickness is to be increased to 3 ft. Footing	BDNI 7.03.02A
thickness is defined in 6 in. increments.	BDM 7.03.01B

• The minimum footing width for cantilever abutments is 6 ft.

The designers select the preliminary dimensions based on state-specific standards and past experience. The preliminary footing dimensions are selected such that the resultant of the vertical loads falls within the middle one-third. As needed, the guidelines shown in the following figure can be used to establish the initial dimensions that correlate with the minimum requirements in the BDM.





The following figure shows the selected abutment geometry and dimensional variables:



The preliminary dimensions selected for this example are given below.

Abutment length



This abutment includes an independent cantilevered backwall, similar to the one shown in BDG 6.20.03A.

Backwall height	$h_{backwall} := 4.25 ft$
Backwall thickness	$t_{backwall} := 1.5 ft$
Abutment wall design height	$h_{wall} := 17.54 ft$

The thickness of an abutment wall is controlled by several factors including the space required to fit bearings and anchor bolts with an adequate edge distance. Since the bearing pad design is not included in this example, a 3ft-2in. thick abutment wall is selected by referring to a similar bridge to provide an adequate space to accommodate bearings and edge distances.

Abutment wall thickness	$t_{wall} := 3ft + 2in = 3.17 ft$
Distance from the toe to the front face of the abutment wall	$l_{toe} := 4ft + 7in = 4.58 ft$

Distance from the heel to the back face of the abutment wall	$l_{heel} \coloneqq 9ft + 3in = 9.25 ft$	
Distance from center of the bearing pad to the back face of the abutment wall	$l_{brtowall} := 2ft + 4in = 2.33 ft$	
Footing width	$B_{footing} := l_{toe} + l_{heel} + t_{wall} = 17 ft$	
Footing length	$L_{footing} := 65.75 ft$	
Footing thickness	$t_{footing} := 3ft$	
Toe fill depth to the bottom of the footing	$h_{toeDepth} := 7 ft$	
Note: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.		

. Passive earth pressure is excluded from the footing design.

BDM 7.03.02 F

Step 2.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$\begin{aligned} DC_{Sup} &\coloneqq \frac{2 \cdot R_{DCEx} + \left(N_{beams} - 2\right) \cdot R_{DCIn}}{L_{abut}} = 5.66 \cdot \frac{kip}{ft} \\ DW_{Sup} &\coloneqq \frac{2 \cdot R_{DWEx} + \left(N_{beams} - 2\right) \cdot R_{DWIn}}{L_{abut}} = 0.89 \cdot \frac{kip}{ft} \\ DC_{backwall} &\coloneqq h_{backwall} \cdot t_{backwall} \cdot W_{c} = 0.96 \cdot \frac{kip}{ft} \\ DC_{wall} &\coloneqq h_{wall} \cdot t_{wall} \cdot W_{c} = 8.33 \cdot \frac{kip}{ft} \\ DC_{footing} &\coloneqq B_{footing} \cdot t_{footing} \cdot W_{c} = 7.65 \cdot \frac{kip}{ft} \end{aligned}$$

Step 2.3 Application of Live Load

Description

This step describes the application of live load on the abutment.

Page Content

- 17 Live Load on the Backwall
- 17 Live Load on the Abutment Wall
- 18 Live Load on the Footing

Live Load on the Backwall

The live load on the bridge has no impact on the backwall.

The live load on the approach slab is represented by a live load surcharge. The live load surcharge results in a lateral load on the backwall. Please refer to Step 2.4 for further details.

Live Load on the Abutment Wall

Depending on the number of design lanes, a multiple presence factor is applied to the HL-93 truck and lane loads.

```
MPF(lanes) := 1.2 if lanes = 1
                    1.0 if lanes = 2
0.85 if lanes = 3
0.65 otherwise
                                                 LRFD Table 3.6.1.1.2-1
```

Live Load on Bridge Superstructure

.

The total of live load girder end reactions is divided by the abutment length to calculate the load on a per-foot basis.

Note: Even though the LRFD specifications recommend including the dynamic impact in the design of substructures that are not completely buried, the MDOT practice is to exclude them from the design of bridge abutments.

$$\begin{aligned} \text{lanes} &:= 1 \qquad \text{R}_{\text{LLWall1}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{abut}}} &= 2.08 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} &:= 2 \qquad \text{R}_{\text{LLWall2}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{abut}}} &= 3.46 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} &:= 3 \qquad \text{R}_{\text{LLWall3}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{abut}}} &= 4.42 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} &:= 4 \qquad \text{R}_{\text{LLWall3}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{abut}}} &= 4.5 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} &:= 5 \qquad \text{R}_{\text{LLWall4}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{abut}}} &= 5.63 \cdot \frac{\text{kip}}{\text{ft}} \\ \end{array}$$

The controlling live load on the abutment wall is

$$R_{LLWallMax} := \max(R_{LLWall1}, R_{LLWall2}, R_{LLWall3}, R_{LLWall4}, R_{LLWall5}) = 5.63 \cdot \frac{k_{1}p}{ft}$$

Live Load on Bridge Approach

The live load on the approach is represented by a surcharge load. This surcharge results in a lateral load on the abutment wall. Please refer to Step 2.4 for further details.

Live Load on the Footing

Live Load on Bridge Superstructure

The total of live load girder reactions is divided by the footing length to calculate the load on a per-foot basis. The dynamic impact is not included in the design of foundations.

LRFD 3.6.2.1

$$\begin{aligned} \text{lanes} &:= 1 \qquad \text{R}_{\text{LLFooting1}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{footing}}} &= 2.01 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} \coloneqq 2 \qquad \text{R}_{\text{LLFooting2}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{footing}}} &= 3.36 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} \coloneqq 3 \qquad \text{R}_{\text{LLFooting3}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{footing}}} &= 4.28 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} \coloneqq 4 \qquad \text{R}_{\text{LLFooting4}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{footing}}} &= 4.37 \cdot \frac{\text{kip}}{\text{ft}} \\ \text{lanes} \coloneqq 5 \qquad \text{R}_{\text{LLFooting5}} \coloneqq \frac{\text{lanes} \cdot \left(\text{V}_{\text{TruckMax}} + \text{V}_{\text{LaneMax}} \right) \cdot \text{f}_{\text{HL93Mod}} \cdot \text{MPF(lanes)}}{\text{L}_{\text{footing}}} &= 5.46 \cdot \frac{\text{kip}}{\text{ft}} \end{aligned}$$

The controlling live load on the footing is

$$R_{LLFootingMax} := \max(R_{LLFooting1}, R_{LLFooting2}, R_{LLFooting3}, R_{LLFooting4}, R_{LLFooting5}) = 5.46 \cdot \frac{kip}{ft}$$

Live Load on Bridge Approach

Live load on the approach is represented by a surcharge load. Please refer to Step 2.4 for further details.

Step 2.4 Application of Other Loads

Description

This step describes the application of braking force, wind load, earth load, and temperature load.

Co	ontent
Bral	king Force
Wine	d Load
Eart	h Load

21 Temperature Load

Braking Force

Since the abutment in this example has expansion bearings, the fixed bearings located at the pier resist the horizontal component of the braking force. Therefore, a horizontal braking force is not applied at the abutment. The braking force calculation is presented in Appendix 2.A and the pier design example.

Note: Although there is a possibility to develop a vertical force component at the bearings due to the braking force applied at 6 ft above the bridge deck, MDOT practice is to exclude this load from substructure design.

Wind Load

Since the abutment has expansion bearings, the fixed bearings located at the pier resist the longitudinal component of the wind load on the superstructure. The relevant calculations are presented in the pier design example.

Note: Although the transverse component of the wind load acts on the abutment, it is often small and does not impact the design. The MDOT practice is to exclude this load from the abutment design.

The wind load calculation is described in the pier design example.

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. Hydrostatic pressure should be avoided if possible in all abutment and retaining wall design cases through the design of an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral pressure and the resultant load are calculated. This load acts at a distance of one third the height from the base of the components being investigated.

Backwall

Lateral load

Abutment Wall

Lateral earth pressure at the base

Lateral load

Footing

Lateral earth pressure at the base

Lateral load

Vertical Earth Load on the Footing

Back side (heel)

Front side (toe)

$$p_{bw} := k_{a} \cdot \gamma_{s} \cdot h_{backwall} = 0.15 \cdot ksf$$

$$LRFD Eq. 3.11.5.1-1$$

$$P_{EHBackwall} := \frac{1}{2} \cdot p_{bw} \cdot h_{backwall} = 0.33 \cdot \frac{kip}{ft}$$

$$p_{wall} := k_{a} \cdot \gamma_{s} \cdot \left(h_{backwall} + h_{wall} \right) = 0.78 \cdot ksf$$

$$P_{EHWall} := \frac{1}{2} \cdot p_{wall} \cdot \left(h_{backwall} + h_{wall} \right) = 8.55 \cdot \frac{kip}{ft}$$

$$p_{ft} := k_a \cdot \gamma_s \cdot \left(h_{backwall} + h_{wall} + t_{footing} \right) = 0.89 \cdot ksf$$

$$P_{EHFooting} := \frac{1}{2} \cdot p_{ft} \cdot \left(h_{backwall} + h_{wall} + t_{footing} \right) = 11.06 \cdot \frac{kip}{ft}$$

$$EV_{earthBk} := \gamma_{s} \cdot l_{heel} \cdot \left(h_{backwall} + h_{wall}\right) = 24.19 \cdot \frac{kip}{ft}$$
$$EV_{earthFt} := \gamma_{s} \cdot l_{toe} \cdot \left(h_{toeDepth} - t_{footing}\right) = 2.2 \cdot \frac{kip}{ft}$$

Live Load Surcharge

Live load surcharge is applied to account for a vehicular load acting on the backfill **LRFD 3.11.6.4** surface within a distance equal to one-half the wall height behind the back face of the wall.

Height of the abutment

 $h_{backwall} + h_{wall} + t_{footing} = 24.79 \text{ ft}$

Note: The equivalent height of soil for the surcharge load is defined as a function of the abutment height.

Equivalent height of soil for the surcharge load	$h_{eq} := 2ft$	LRFD Table 3.11.6.4-1
Lateral surcharge pressure	$\sigma_p := k_a \cdot \gamma_s \cdot h_{eq} = 0.07 \cdot ksf$	LRFD Eq. 3.11.6.4-1
Backwall		
Lateral load	$P_{LSBackwall} \coloneqq \sigma_p \cdot h_{backwall} = 0.3$	$1 \cdot \frac{\text{kip}}{\text{ft}}$
Abutment Wall		
Lateral load	$P_{LSWall} := \sigma_{p} \cdot \left(h_{backwall} + h_{wall} \right)$	$= 1.57 \cdot \frac{\text{kip}}{\text{ft}}$
Footing		tin
Lateral load	$P_{LSFooting} := \sigma_p \cdot (h_{backwall} + h_{wall})$	$1 + t_{\text{footing}} = 1.78 \cdot \frac{\text{klp}}{\text{ft}}$
Vertical load	$V_{LSFooting} \coloneqq \gamma_s \cdot l_{heel} \cdot h_{eq} = 2.22 \cdot \frac{1}{2}$	<u>kip</u> ft

Temperature Load

The forces transferred from the superstructure to the substructure due to temperature are influenced by the shear stiffness of the bearing pads.

Thermal expansion coefficient of steel (/°F)

 $\alpha := 6.5 \cdot 10^{-6}$

Note: MDOT uses a 45° F drop and 35° F rise from the temperature at the time of construction.

BDM 7.01.07 cold climate temperature range

Contraction and expansion temperatures	$T_{contraction} := 45$ $T_{expansion} := 35$	
Bridge superstructure contraction	$\Delta_{\text{TContr}} := \alpha \cdot L_{\text{span}} \cdot T_{\text{contraction}} = 0.35 \cdot p$	in
Bridge superstructure expansion	$\Delta_{\text{TExp}} \coloneqq \alpha \cdot L_{\text{span}} \cdot T_{\text{expansion}} = 0.27 \cdot \text{in}$	
Shear modulus of the elastomer	$G_{\text{bearing}} \coloneqq 100 \frac{\text{lb}}{\text{in}^2}$	BDM 7.02.05C
Plan view area of the bearing pad	$A_{\text{bearing}} := 22 \text{in} \cdot 9 \text{in} = 198 \cdot \text{in}^2$	
Total elastomer thickness	$h_{rt} \coloneqq 2.75 in$	

Since the pier bearings are fixed, the total superstructure deformation is imposed on the abutment bearings.

The force acting on a bearing due to superstructure contraction

$$H_{buContr} := \frac{G_{bearing} \cdot A_{bearing} \cdot \Delta_{TContr}}{h_{rt}} = 2.53 \cdot kip \qquad \frac{LRFD Eq.}{14.6.3.1-2}$$

Total force acting on the abutment due to superstructure contraction

The force acting on a bearing due to superstructure expansion

Total force acting on the abutment due to superstructure expansion

$$TU_{Contr} := \frac{N_{beams} \cdot H_{buContr}}{L_{abut}} = 0.28 \cdot \frac{kip}{ft}$$

$$H_{buExp} := \frac{G_{bearing} \cdot A_{bearing} \cdot \Delta_{TExp}}{h_{rt}} = 1.97 \cdot kip$$
LRFD Eq. 14.6.3.1-2

$$TU_{Exp} := \frac{N_{beams} \cdot H_{buExp}}{L_{abut}} = 0.22 \cdot \frac{kip}{ft}$$

Step 2.5 Combined Load Effects

Description

This step presents the procedure for combining all load effects and calculates total factored forces and moments acting at the base of the backwall, abutment wall, and footing.

Page Contents

- 25 Forces and Moments at the Base of the Backwall
- 27 Forces and Moments at the Base of the Abutment Wall
- 31 Forces and Moments at the Base of the Footing

Strength I, Strength III, Strength V, and Service I limit states are considered for the analysis and design of an abutment.

LRFD 3.4.1

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU

Strength III = 1.25DC + 1.5DW + 1.5EH + 1.35EV + 1.0WS + 0.5TU

Strength V = 1.25DC + 1.5DW + 1.35LL + 1.35BR + 1.0WS + 1.0WL + 1.5EH + 1.35EV + 1.35LS + 0.5TU

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

- BR = vehicular braking force
- DC = dead load of structural components and nonstructural attachments
- DW = dead load of future wearing surface and utilities
- EH = horizontal earth pressure load
- EV = vertical pressure from the earth fill
- LL = vehicular live load
- LS = live load surcharge
- WL = wind on live load
- WS = wind load on structure
- TU = force effect due to uniform temperature

Limit states that are not shown either do not control or are not applicable. Generally, Strength III or Strength V may control the design of abutments with fixed bearings when the wind load is considered.

Note: These load combinations should include the maximum and minimum load factors; only the maximum factors are shown for clarity.

Since the MDOT practice is to exclude wind load from the abutments design, only Strength I and Service I limit states are included in this section.

Four load cases are considered in the design of an abutment:

BDM 7.03.01

Case II Bridge open to traffic with traffic loading on the approach only.

Case III Bridge with traffic on it and no load on the approach.

Case I Construction state: abutment built and backfilled to grade.

Case IV Contraction: Loading forces of Case II plus the effects of temperature contraction in the deck transmitted to the abutment.

Since Case IV always governs over Case II for the bridge abutment selected for this example (independent cantilever abutment), only Cases I, III, and IV are considered.

The temperature force in Load Case IV is due to contraction; therefore

$$TU := TU_{Contr} = 0.28 \cdot \frac{kip}{ft}$$

The base of the backwall, the base of the abutment wall, and the base of the footing are the three critical locations where the force effects need to be combined and analyzed for the design of an abutment. Horizontal loads parallel to the longitudinal axis of the abutment are not considered for backwall and abutment wall design because of the high moment of inertia about the longitudinal axis of the bridge. However, such loads, even though relatively small, are considered at the base of the footing.



Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU

Load Case I

Factored vertical force

Factored shear force parallel to the transverse axis of the backwall

Factored moment about the longitudinal axis of the backwall

Load Case III

Factored vertical force

Factored shear force parallel to the transverse axis of the backwall

Factored moment about the longitudinal axis of the backwall

Load Case IV

Factored vertical force

Factored shear force parallel to the transverse axis of the backwall

Factored moment about the longitudinal axis of the backwall

$$M_{uBwLC4StrI} \coloneqq 1.5 \cdot P_{EHBackwall} \cdot \frac{h_{backwall}}{3} + 1.75 \cdot P_{LSBackwall} \cdot \frac{h_{backwall}}{2} = 1.83 \cdot \frac{kip \cdot ft}{ft}$$

 $F_{VBwLC1StrI} := 1.25 \cdot DC_{backwall} = 1.2 \cdot \frac{kip}{ft}$

 $V_{uBwLC1StrI} := 1.5 \cdot P_{EHBackwall} = 0.49 \cdot \frac{kip}{ft}$

 $F_{VBwLC3StrI} := 1.25 \cdot DC_{backwall} = 1.2 \cdot \frac{kip}{4}$

 $V_{uBwLC3StrI} := 1.5 \cdot P_{EHBackwall} = 0.49 \cdot \frac{kip}{fr}$

 $F_{VBwLC4StrI} := 1.25 \cdot DC_{backwall} = 1.2 \cdot \frac{kip}{4}$

 $M_{uBwLC1StrI} := 1.5 \cdot P_{EHBackwall} \cdot \frac{h_{backwall}}{3} = 0.69 \cdot \frac{kip \cdot ft}{ft}$

 $M_{uBwLC3StrI} := 1.5 \cdot P_{EHBackwall} \cdot \frac{h_{backwall}}{3} = 0.69 \cdot \frac{kip \cdot ft}{ft}$

 $V_{uBwLC4StrI} := 1.5 \cdot P_{EHBackwall} + 1.75 \cdot P_{LSBackwall} = 1.02 \cdot \frac{kip}{ft}$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Since Load Case IV controls the Service I limit state, related calculations are shown below.

Factored vertical force

 $F_{\text{VBackwallSerI}} \coloneqq DC_{\text{backwall}} = 0.96 \cdot \frac{\text{kip}}{\text{ft}}$

Factored shear force parallel to the transverse axis of the backwall

$$V_{uBackwallSerI} := P_{EHBackwall} + P_{LSBackwall} = 0.63 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the backwall

$$M_{uBackwallSerI} \coloneqq P_{EHBackwall} \cdot \frac{h_{backwall}}{3} + P_{LSBackwall} \cdot \frac{h_{backwall}}{2}$$
$$M_{uBackwallSerI} = 1.11 \cdot \frac{kip \cdot ft}{ft}$$

Summary of Forces and Moments at the Base of the Backwall

Factored vertical force, F_{VBw} (kip/ft)

Factored shear force parallel to the transverse axis of the backwall, $V_{uBw}(\mbox{kip/ft})$

	Strength I	Service I
LC I	1.20	-
LC III	1.20	-
LC IV	1.20	0.96

	Strength I	Service I
LC I	0.49	-
LC III	0.49	-
LC IV	1.02	0.63

Factored moment about the longitudinal axis of the backwall, MuBw (kip ft/ft)

	Strength I	Service I
LC I	0.69	-
LC III	0.69	-
LC IV	1.83	1.11

Forces and Moments at the Base of the Abutment Wall

Load Cases I, III, and IV are considered below. The superstructure dead and live loads and the uniform temperature induced loads are considered in addition to the backwall and abutment wall dead loads, lateral earth pressure, and lateral surcharge pressure.



Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU

Load Case I

Factored vertical force $F_{VWallLC1StrI} := 1.25 \cdot \left(DC_{backwall} + DC_{wall}\right) = 11.61 \cdot \frac{kip}{ft}$ Factored shear force parallel to the
transverse axis of the abutment wall $V_{uWallLC1StrI} := 1.5 \cdot P_{EHWall} = 12.82 \cdot \frac{kip}{ft}$ The backwall weight reduces the critical moment at the base of the abutment wall. ThisLRFD 3.4.1

requires using the minimum load factor of 0.9 for the dead load (DC) instead of the factor 1.25 in the Strength I combination.

LRFD 3.4.1 LFRD Table 3.4.1-2

Similar conditions are applied for the moments calculated about the longitudinal axis of the abutment wall for all the load cases and all the limit states.

Factored moment about the longitudinal axis of the abutment wall

$$M_{uWallLC1StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + 1.5 \cdot P_{EHWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{3} = 92.4 \cdot \frac{kip \cdot ft}{ft}$$

Load Case III

Factored vertical force

$$F_{VWallLC3StrI} \coloneqq 1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall}\right) + 1.5DW_{Sup} + 1.75R_{LLWallMax}$$
$$F_{VWallLC3StrI} = 29.86 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall

$$V_{uWallLC3StrI} := 1.5 \cdot P_{EHWall} = 12.82 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC3StrI} &\coloneqq 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLWallMax}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ 1.5 \cdot P_{EHWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{3} \\ &M_{uWallLC3StrI} = 106.09 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force
$$F_{VWallLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall}) + 1.5DW_{Sup} = 20.01 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall $V_{uWallLC4StrI} := 1.5 \cdot P_{EHWall} + 1.75 \cdot P_{LSWall} + 0.5TU = 15.7 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC4StrI} &\coloneqq 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ 1.5 \cdot P_{EHWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{3} + 1.75 \cdot P_{LSWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{2} + 0.5 \cdot TU \cdot h_{wall} \\ M_{uWallLC4StrI} &= 131.04 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Load Case I

Factored vertical force $F_{VWallLC1SerI} := DC_{backwall} + DC_{wall} = 9.29 \cdot \frac{kip}{ft}$ Factored shear force parallel to the
transverse axis of the abutment wall $V_{uWallLC1SerI} := P_{EHWall} = 8.55 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the abutment wall

$$M_{uWallLC1SerI} := DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + P_{EHWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{3}$$
$$M_{uWallLC1SerI} = 61.28 \cdot \frac{kip \cdot ft}{ft}$$

Load Case III

Factored vertical force

$$F_{VWallLC3SerI} := \left(DC_{Sup} + DC_{backwall} + DC_{wall}\right) + DW_{Sup} + R_{LLWallMax} = 21.46 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall

$$V_{uWallLC3SerI} := P_{EHWall} = 8.55 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC3SerI} &\coloneqq DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots \\ &+ \left(DC_{Sup} + DW_{Sup} + R_{LLWallMax}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ P_{EHWall} \cdot \frac{\left(h_{backwall} + h_{wall}\right)}{3} \\ & M_{uWallLC3SerI} = 70.41 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force

 $F_{VWallLC4SerI} := (DC_{Sup} + DC_{backwall} + DC_{wall}) + DW_{Sup}$ $F_{VWallLC4SerI} = 15.83 \cdot \frac{kip}{ft}$ e $V_{uWallLC4SerI} := P_{EHWall} + P_{LSWall} + TU = 10.39 \cdot \frac{kip}{ft}$

Factored shear force parallel to the transverse axis of the abutment wall

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC4SerI} &\coloneqq DC_{backwall} \cdot \frac{\left(^{t}backwall - t_{wall}\right)}{2} \dots \\ &+ \left(DC_{Sup} + DW_{Sup}\right) \cdot \left(^{l}b_{trowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ P_{EHWall} \cdot \frac{\left(^{h}backwall + h_{wall}\right)}{3} + P_{LSWall} \cdot \frac{\left(^{h}backwall + h_{wall}\right)}{2} + TU \cdot h_{wall} \\ M_{uWallLC4SerI} &= 88.15 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Summary of Forces and Moments at the Base of the Abutment Wall

Factored vertical force, F_{VWall} (kip/ft)

of the abutment wall, V_{uWall} (kip/ft)			
	Strongth I	Sorvice I	

Factored shear force parallel to the transverse axis

	Strength I	Service I
LC I	11.61	9.29
LC III	29.86	21.46
LC IV	20.01	15.83

	Strength I	Service I
LC I	12.82	8.55
LC III	12.82	8.55
LC IV	15.70	10.39

Factored moment about the longitudinal axis of the abutment wall, M_{uWall} (kip ft/ft)

	Strength I	Service I
LC I	92.40	61.28
LC III	106.09	70.41
LC IV	131.04	88.15

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered below. In addition to all the loads considered for the abutment wall, weight of soil (i.e. the earth load on the footing toe and heel) and live load on the backwall are considered.

The dynamic load allowance is excluded from the live load for foundation components that are entirely below ground level.

LRFD 3.6.2.1



ΣM at footing centerline

LC IV

DC_{footing}

Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU

Load Case I

Factored vertical force

 $F_{VFtLC1StrI} := 1.25 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 56.79 \cdot \frac{kip}{ft}$

 $V_{uFtLC1StrI} := 1.5 \cdot P_{EHFooting} = 16.59 \cdot \frac{kip}{ft}$

Factored shear force parallel to the transverse axis of the footing

The backfill soil weight reduces the critical moment at the base of the footing. This requires using the minimum load factor of 1.0 for the vertical earth load (EV) instead of the factor 1.35 in the Strength I combination. Similar conditions are applied for the moments calculated about the longitudinal axis of the footing for all the load cases.

LRFD 3.4.1 LFRD Table 3.4.1-2

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC1StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{footing} \right)}{3} + 1.35EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \\ &M_{uFtLC1StrI} = 87.92 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case III

Factored vertical force $F_{VFtLC3StrI} := 1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.5DW_{Sup} \dots + 1.75R_{LLFootingMax} + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right)$

$$F_{VFtLC3StrI} = 74.75 \cdot \frac{kip}{ft}$$
$$V_{uFtLC3StrI} \coloneqq 1.5 \cdot P_{EHFooting} = 16.59 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots \\ &+ 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force

$$F_{VFtLC4StrI} \coloneqq 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) + 1.5DW_{Sup} \dots + 1.35 \cdot (EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFooting}$$

$$F_{VFtLC4StrI} = 69.08 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC4StrI} := 1.5 \cdot P_{EHFooting} + 1.75 P_{LSFooting} + 0.5TU = 19.85 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} \mathsf{M}_{uFtLC4StrI} &\coloneqq 1.25 \cdot \mathsf{DC}_{backwall} \cdot \left(\mathsf{l}_{heel} + \frac{\mathsf{t}_{backwall}}{2} - \frac{\mathsf{B}_{footing}}{2} \right) + 1.25\mathsf{DC}_{wall} \cdot \left(\mathsf{l}_{heel} + \frac{\mathsf{t}_{wall}}{2} - \frac{\mathsf{B}_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot \mathsf{DC}_{Sup} + 1.5 \cdot \mathsf{DW}_{Sup} \right) \cdot \left(\mathsf{l}_{heel} + \mathsf{l}_{brtowall} - \frac{\mathsf{B}_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot \mathsf{P}_{EHFooting} \cdot \frac{\left(\mathsf{h}_{backwall} + \mathsf{h}_{wall} + \mathsf{t}_{footing} \right)}{3} + 1.75 \mathsf{V}_{LSFooting} \cdot \left(\frac{\mathsf{l}_{heel}}{2} - \frac{\mathsf{B}_{footing}}{2} \right) \dots \\ &+ 1.75 \cdot \mathsf{P}_{LSFooting} \cdot \frac{\left(\mathsf{h}_{backwall} + \mathsf{h}_{wall} + \mathsf{t}_{footing} \right)}{2} + 1.0 \cdot \mathsf{EV}_{earthBk} \cdot \left(\frac{\mathsf{l}_{heel}}{2} - \frac{\mathsf{B}_{footing}}{2} \right) \dots \\ &+ 1.35 \cdot \mathsf{EV}_{earthFt} \cdot \left(\frac{\mathsf{B}_{footing}}{2} - \frac{\mathsf{l}_{toe}}{2} \right) + 0.5 \cdot \mathsf{TU} \cdot \left(\mathsf{h}_{wall} + \mathsf{t}_{footing} \right) \\ &\qquad \mathsf{M}_{uFtLC4StrI} = 140.34 \cdot \frac{\mathsf{kip} \cdot \mathsf{ft}}{\mathsf{ft}} \end{split}$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU Load Case I

Factored vertical force

$$F_{VFtLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 43.32 \cdot \frac{kip}{ft}$$
Factored shear force parallel to the
transverse axis of the footing
$$V_{uFtLC1SerI} := P_{EHFooting} = 11.06 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$M_{uFtLC1SerI} \coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots + P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots + EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots + EV_{earthBk} \cdot \left(\frac{h_{eel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots + EV_{earthBk} \cdot \left(\frac{h_{eel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots + EV_{earthBk} \cdot \left(\frac{h_{eel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthBk} \cdot \left(\frac{h_{eel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthBk} \cdot \left(\frac{h_{eel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{eel}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{earthFt} \cdot \left(\frac{B_{eel}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{eartHt} \cdot \left(\frac{B_{eel}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{eartHt} \cdot \left(\frac{B_{eel}}{2} - \frac{h_{eel}}{2} \right) \dots + EV_{eartHt} \cdot \left(\frac{B_{eel}}{2} \right) \dots + EV_{eartHt} \cdot \left(\frac{B_{eel}}{2}$$

Load Case III

Factored vertical force

$$F_{VFtLC3SerI} \coloneqq DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFootingMax} + (EV_{earthFt} + EV_{earthBk})$$

$$F_{VFtLC3SerI} = 55.33 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC3SerI} := P_{EHFooting} = 11.06 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} + R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots \\ &+ EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force
$$F_{VFtLC4SerI} \coloneqq DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} \dots$$

+ $EV_{earthFt} + EV_{earthBk} + V_{LSFooting}$
 $F_{VFtLC4SerI} = 52.09 \cdot \frac{kip}{ft}$ Factored shear force parallel to the
transverse axis of the footing $V_{uFtLC4SerI} \coloneqq P_{EHFooting} + P_{LSFooting} + TU = 13.12 \cdot \frac{kip}{ft}$ Factored moment about the longitudinal axis of the footing $V_{uFtLC4SerI} \coloneqq P_{EHFooting} + P_{LSFooting} + TU = 13.12 \cdot \frac{kip}{ft}$

$$\begin{split} M_{uFtLC4SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) + P_{EHFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{footing} \right)}{3} \dots \\ &+ EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + P_{LSFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{footing} \right)}{2} \dots \\ &+ TU \cdot \left(h_{wall} + t_{footing} \right) \end{split}$$

Summary of Forces and Moments at the Base of the Footing

Factored vertical force, F_{VFt} (kip/ft)

	Strength I	Service I
LC I	56.79	43.32
LC III	74.75	55.33
LC IV	69.08	52.09

Factored shear force parallel to the transverse axis of the footing, $V_{uFt}\,(kip/ft)$

	Strength I	Service I
LC I	16.59	11.06
LC III	16.59	11.06
LC IV	19.85	13.12

Factored moment about the longitudinal axis of the footing, $M_{uFt} \left(kip \, ft/ft \right)$

	Strength I	Service I
LC I	87.92	32.22
LC III	143.27	69.22
LC IV	140.34	71.62

Step 2.6 Geotechnical Design of the Footing

Description

This step presents the geotechnical design of a spread footing considering the following strength and serviceability limit states:

LRFD 10.6.1.1

- 1. bearing resistance strength limit state
- 2. settlement service limit state
- 3. sliding resistance strength limit state
- 4. load eccentricity (overturning) strength limit state.

Step 2.9 presents the evaluation of structural resistance of the footing (internal stability).

Page Contents

- **37 Bearing Resistance Check**
- 41 Settlement Check
- 41 Sliding Resistance Check
- 43 Eccentric Load Limitation (Overturning) Check
Forces and Moments at the Base of the Footing

Step 2.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VFt} (kip/ft)

	Strength I	Service I
LC I	56.79	43.32
LC III	74.75	55.33
LC IV	69.08	52.09

Factored shear force parallel to the transverse axis of the footing, V_{uFt} (kip/ft)

	Strength I	Service I
LC I	16.59	11.06
LC III	16.59	11.06
LC IV	19.85	13.12

Factored moment about the longitudinal axis of the footing, MuFt (kip ft/ft)

	Strength I	Service I
LC I	87.92	32.22
LC III	143.27	69.22
LC IV	140.34	71.62

Bearing Resistance Check

For eccentrically loaded footings, the use of a reduced effective area is allowed for bearing resistance or settlement calculation. The point of load application shall be at the centroid of the reduced area.

Note: As a practice, the average pressure and the values at the toe and heel under different load cases and limit states are provided to the MDOT Geotechnical Services Section for verification.

 \mathbf{E}

This example presents the LRFD and MDOT methods.

Load Case I, Strength I

Factored vertical force

Factored moment about the longitudinal axis of the footing

$$F_{VFtLC1StrI} = 56.79 \cdot \frac{kip}{ft}$$
$$M_{uFtLC1StrI} = 87.92 \cdot \frac{kip \cdot ft}{ft}$$
$$e_{B} := \frac{M_{uFtLC1StrI}}{F_{VFtLC1StrI}} = 1.55 \text{ ft}$$

Eccentricity in the footing width direction

LRFD Method

A reduced effective footing width is used for bearing resistance and settlement design.

 $B_{eff} := B_{footing} - 2 \cdot e_B = 13.9 \text{ ft}$ LRFD Eq. 10.6.1.3-1 Effective footing width $q_{\text{bearing}_\text{LC1}} := \frac{\text{FvFtLC1StrI}}{\text{B}_{\text{eff}}} = 4.08 \cdot \text{ksf}$ Bearing pressure

LRFD 10.6.1.3

LRFD 10.6.1.3

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case III, Strength I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case IV, Strength I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

$$q_{avgLC1} \coloneqq \frac{F_{VFtLC1StrI}}{B_{footing}} = 3.34 \cdot ksf$$

$$q_{toeLC1} \coloneqq \frac{F_{VFtLC1StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 5.17 \cdot ksf$$

$$q_{heelLC1} \coloneqq \frac{F_{VFtLC1StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.52 \cdot ksf$$

$$F_{VFtLC3StrI} = 74.75 \cdot \frac{kip}{ft}$$

$$M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC3StrI}}{F_{VFtLC3StrI}} = 1.92 \text{ ft}$$

 $B_{eff} := B_{footing} - 2 \cdot e_{B} = 13.17 \text{ ft} \qquad LRFD Eq. 10.6.1.3-1$ $q_{bearing_LC3} := \frac{F_{VFtLC3StrI}}{B_{eff}} = 5.68 \cdot \text{ksf}$

$$q_{avgLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} = 4.4 \cdot ksf$$

$$q_{toeLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 7.37 \cdot ksf$$

$$q_{heelLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.42 \cdot ksf$$

$$F_{VFtLC4StrI} = 69.08 \cdot \frac{kip}{ft}$$
$$M_{uFtLC4StrI} = 140.34 \cdot \frac{kip \cdot ft}{ft}$$
$$e_{B} := \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrI}} = 2.03 \text{ ft}$$

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case I, Service I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case III, Service I

Factored vertical force

Factored moment about the longitudinal axis of the footing

 $B_{eff} := B_{footing} - 2 \cdot e_{B} = 12.94 \text{ ft} \qquad LRFD Eq. 10.6.1.3-1$ $q_{bearing_LC4} := \frac{F_{VFtLC4StrI}}{B_{eff}} = 5.34 \cdot \text{ksf}$

$$q_{avgLC4} := \frac{F_{VFtLC4StrI}}{B_{footing}} = 4.06 \cdot ksf$$

$$q_{\text{toeLC4}} \coloneqq \frac{F_{\text{VFtLC4StrI}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 6.98 \cdot \text{ksf}$$
$$q_{\text{heelLC4}} \coloneqq \frac{F_{\text{VFtLC4StrI}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 1.15 \cdot \text{ksf}$$

$$F_{VFtLC1SerI} = 43.32 \cdot \frac{kip}{ft}$$

$$M_{uFtLC1SerI} = 32.22 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC1SerI}}{F_{VFtLC1SerI}} = 0.74 \text{ ft}$$

$$B_{eff} := B_{footing} - 2 \cdot e_{B} = 15.51 \text{ ft} \qquad LRFD Eq. 10.6.1.3-1$$
$$q_{bearing_LC1SerI} := \frac{F_{VFtLC1SerI}}{B_{eff}} = 2.79 \cdot \text{ksf}$$

$$q_{avgLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} = 2.55 \cdot ksf$$

$$q_{toeLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.22 \cdot ksf$$

$$q_{heelLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.88 \cdot ksf$$

$$F_{VFtLC3SerI} = 55.33 \cdot \frac{kip}{ft}$$
$$M_{uFtLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}$$

Eccentricity in the footing width direction

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

Load Case IV, Service I

Factored vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

LRFD Method

Effective footing width

Bearing pressure

MDOT Method

Average bearing pressure

Bearing pressure at the toe

Bearing pressure at the heel

$$e_{\rm B} := \frac{M_{\rm u} FtLC3SerI}{FVFtLC3SerI} = 1.25 \, {\rm ft}$$

 $B_{eff} := B_{footing} - 2 \cdot e_{B} = 14.5 \text{ ft} \qquad LRFD \text{ Eq. 10.6.1.3-1}$ $q_{bearing_LC3SerI} := \frac{F_{VFtLC3SerI}}{B_{eff}} = 3.82 \cdot \text{ksf}$

$$q_{avgLC3SerI} \coloneqq \frac{F_{VFtLC3SerI}}{B_{footing}} = 3.25 \cdot ksf$$

$$q_{toeLC3SerI} \coloneqq \frac{F_{VFtLC3SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.69 \cdot ksf$$

$$F_{VFtLC3SerI} \left(\begin{array}{c} 6 \cdot e_B \end{array}\right)$$

$$q_{\text{heelLC3SerI}} \coloneqq \frac{^{\text{FVFtLC3SerI}}}{B_{\text{footing}}} \cdot \left(1 - \frac{^{6 \cdot e_{\text{B}}}}{B_{\text{footing}}}\right) = 1.82 \cdot \text{ksf}$$

$$F_{VFtLC4SerI} = 52.09 \cdot \frac{kip}{ft}$$
$$M_{uFtLC4SerI} = 71.62 \cdot \frac{kip \cdot ft}{ft}$$
$$e_{B} := \frac{M_{uFtLC4SerI}}{F_{VFtLC4SerI}} = 1.37 \text{ ft}$$

$$B_{eff} := B_{footing} - 2 \cdot e_B = 14.25 \text{ ft}$$
 LRFD Eq. 10.6.1.3-1

$$q_{\text{bearing}_\text{LC4SerI}} \coloneqq \frac{F_{\text{VFtLC4SerI}}}{B_{\text{eff}}} = 3.66 \cdot \text{ksf}$$

$$q_{avgLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} = 3.06 \cdot ksf$$

$$q_{toeLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.55 \cdot ksf$$

$$q_{heelLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.58 \cdot ksf$$

Summary

LRFD Method

The controlling bearing pressure under strength limit states

 $q_b := max(q_{bearing_LC1}, q_{bearing_LC3}, q_{bearing_LC4}) = 5.68 \cdot ksf$

The controlling bearing pressure needs to be checked with the factored bearing resistance of the soil provided by the Geotechnical Services Section.

MDOT Method

A summary of bearing pressure values (in psf) is shown in the following table:

	Toe	Avg	Heel	Toe	Avg	Heel
	(Service I)	(Serivce I)	(Service I)	(Strength I)	(Strength I)	(Strength I)
LC I	3217	2549	1880	5166	3341	1516
LC III	4692	3254	1817	7371	4397	1422
LC IV	4551	3064	1577	6977	4064	1150

The Geotechnical Services Section uses these values for the verification of bearing resistance and settlement limits. If the bearing pressure exceeds the bearing strength of the soil, the size of the footing needs to be increased.

Settlement Check

The Geotechnical Services Section uses the controlling bearing pressure from the service limit state to check if the total settlement of foundation is less than 1.5 in., the allowable limit.

BDM 7.03.02G 2b

LRFD 10.6.3.4

BDM 7.03.02G

For the LRFD method, the controlling bearing pressure for settlement analysis is

 q_b settlement := max($q_{bearing LC1SerI}, q_{bearing LC3SerI}, q_{bearing LC4SerI}$) = 3.82·ksf

The Geotechnical Services Section uses this controlling bearing pressure to calculate the foundation total settlement.

For the MDOT method, the bearing pressures under service limit state are provided to the Geotechnical Services Section to calculate the settlement.

Note: Besides the total settlement, considerations should be given to prevent the differential settlement between the abutments and pier from exceeding the tolerable differential settlement limit. Differential settlement limits are given in the *Steel Plate Girder Design Example*.

Sliding Resistance Check

Spread footings must be designed to resist lateral loads without sliding. The sliding resistance of a footing on cohesionless soil is a function of the normal force and the interface friction between the foundation and the soil.

The Geotechnical Services Section should provide a coefficient of sliding resistance (μ) for a design. MDOT typically uses a sliding resistance coefficient of 0.5 for cast-in-place concrete footings. Consult the Geotechnical Services Section to identify the most suitable coefficient for a specific design.

Coefficient of sliding resistance

 $\mu := 0.5$

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used:

- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Load Case I

Factored shear force parallel to the transverse axis of the footing

 $V_{uFtLC1StrI} = 16.59 \cdot \frac{kip}{ft}$

 $V_{sliding} := V_{uFtLC1StrI} = 16.59 \cdot \frac{kip}{ft}$

 $\phi_{\tau} := 0.8$ BDM 7.03.02.F, LRFD Table 10.5.5.5.2-1

 $V_{\text{resistance}} := \phi_{\tau} \cdot \mu \cdot F_{\text{VFtLC1StrIMin}} = 16.65 \cdot \frac{\text{kip}}{\text{ft}}$

Check := if (V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"

Factored sliding force

Minimum vertical load

$$F_{VFtLC1StrIMin} := 0.9 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 41.63 \cdot \frac{kip}{ft}$$

Resistance factor for sliding

Sliding resistance

Check if V_{resistance} > V_{sliding}

Load Case III

Factored shear force parallel to the
transverse axis of the footing $V_{uFtLC3StrI} = 16.59 \cdot \frac{kip}{ft}$ Factored sliding force $V_{sliding} := V_{uFtLC3StrI} = 16.59 \cdot \frac{kip}{ft}$

When calculating the minimum vertical force for sliding and checking eccentric load limitation, the live load on the superstructure is excluded to develop a conservative design.

Minimum vertical load without the live load	$F_{VFtLC3StrIMin_noLL} := 0.9 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) \dots + 1.0 \cdot (EV_{earthBk} + EV_{earthFt})$
	$F_{VFtLC3StrIMin_noLL} = 46.72 \cdot \frac{kip}{ft}$
Resistance factor for sliding	$\phi_{\tau} := 0.8$ BDM 7.03.02.F, LRFD Table 10.5.5.5.2-1
Sliding resistance	$V_{resistance} \coloneqq \phi_{\tau} \cdot \mu \cdot F_{VFtLC3StrIMin_noLL} = 18.69 \cdot \frac{kip}{ft}$
Check if $V_{resistance} > V_{sliding}$	Check := if $(V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"$

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Factored shear force parallel to the	$V_{-10.85}$ kip
transverse axis of the footing	$v_{uFtLC4StrI} = 19.85 \cdot \frac{1}{ft}$

Factored sliding force without the live
load surcharge
$$V_{sliding} := V_{uFtLC4StrI} - 1.75P_{LSFooting} = 16.73 \cdot \frac{kip}{\hbar}$$
Minimum vertical load without
the live load surcharge $F_{VFtLC4StrIMin_noLS} := 0.9 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) \dots$
 $+ 1.0 \cdot (EV_{earthBk} + EV_{earthFt})$ $F_{VFtLC4StrIMin_noLS} = 46.72 \cdot \frac{kip}{\hbar}$ Sliding resistance $V_{resistance} > V_{sliding}$ Check if $V_{resistance} > V_{sliding}$ $Check := if(V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"$ With the live load surcharge:
Factored shear force parallel to the
transverse axis of the footing $V_{uFtLC4StrI} = 19.85 \cdot \frac{kip}{\hbar}$ Minimum vertical load with the
live load surcharge $F_{VFtLC4StrIMin} := 0.9 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) \dots$
 $+ 1.0 \cdot (EV_{earthBk} + EV_{earthFt}) + 1.75V_{LSFooting}$ With the live load surcharge $V_{uFtLC4StrI} = 19.85 \cdot \frac{kip}{\hbar}$ Factored sliding force $V_{sliding} := V_{uFtLC4StrI} = 19.85 \cdot \frac{kip}{\hbar}$ Minimum vertical load with the
live load surcharge $F_{VFtLC4StrIMin} := 0.9 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) \dots$
 $+ 1.0 \cdot (EV_{earthBk} + EV_{earthFt}) + 1.75V_{LSFooting}$ Sliding resistance $V_{resistance} := \phi_{\tau} : \mu \cdot F_{VFtLC4StrIMin} = 20.24 \cdot \frac{kip}{\hbar}$ Sliding resistance $V_{resistance} := \phi_{\tau} : \mu \cdot F_{VFtLC4StrIMin} := 0.9 \cdot (DC'_{sup} = "OK", "Not OK") = "OK"$

Eccentric Load Limitation (Overturning) Check

The eccentricity of loading at the strength limit state, evaluated based on factored loads, shall **LRFD 10.6.3.3** not exceed one-sixth of the corresponding dimension measured from the centerline of the footing for stability.

The eccentricity in the abutment length direction is not a concern. The following calculations present the evaluation of the eccentricity in the abutment width direction for the Strength I limit state:

Minimum vertical force

Moment about the longitudinal axis of the footing

Eccentricity in the footing width direction measured from the centerline

1/6 of footing width

Check if the eccentric load limitation is satisfied

$$F_{VFtLC1StrIMin} = 41.63 \cdot \frac{kip}{ft}$$

$$M_{uFtLC1StrI} = 87.92 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC1StrI}}{F_{VFtLC1StrIMin}} = 2.11 \text{ ft}$$

$$\frac{B_{footing}}{6} = 2.83 \cdot \text{ft}$$
Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OR"\right)$

= "OK"

Load Case III

Two cases need to be considered: without and with the live load

Without the live load:

Minimum vertical force without the live load

 $F_{VFtLC3StrIMin_noLL} = 46.72 \cdot \frac{kip}{ft}$

Moment about the longitudinal axis of the footing (with the live load)

$$M_{uFtLC3StrI} = 143.27 \cdot \frac{k_{IP} \cdot ft}{ft}$$

 $F_{VFtLC3StrIMin} = 56.27 \cdot \frac{kip}{ft}$

 $M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft}$

Moment about the longitudinal axis of the footing (without the live load)

$$M_{uFtLC3StrI_noLL} := M_{uFtLC3StrI} - \left(1.75 \cdot R_{LLFootingMax}\right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2}\right) = 113.82 \cdot \frac{kip \cdot ft}{ft}$$

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$e_{\rm B} := \frac{M_{\rm u} FtLC3StrI_noLL}{FVFtLC3StrIMin_noLL} = 2.44 \, {\rm ft}$$

Check := if
$$\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK" \right) = "OK"$$

F_{VFtLC3StrIMin} := F_{VFtLC3StrIMin} noLL + 1.75R_{LLFootingMax}

With the live load:

Minimum vertical force with the live load

Moment about the longitudinal axis of the footing (with the live load)

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

direction

$$e_{B} := \frac{M_{u}FtLC3StrI}{F_{V}FtLC3StrIMin} = 2.55 \text{ ft}$$
tion is satisfied

$$Check := if\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK"\right) = "OK"$$

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Minimum vertical force without the live load surcharge

Moment about the longitudinal axis of the footing (with the live load surcharge)

$$F_{VFtLC4StrIMin_noLS} = 46.72 \cdot \frac{kip}{ft}$$
$$M_{uFtLC4StrI} = 140.34 \cdot \frac{kip \cdot ft}{ft}$$

Moment about the longitudinal axis of the footing (without the live load surcharge)

$$M_{uFtLC4StrI_noLS} \coloneqq M_{uFtLC4StrI} - 1.75V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2}\right) \dots + -1.75 \cdot P_{LSFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{footing}\right)}{2} \dots$$
$$M_{uFtLC4StrI_noLS} = 116.67 \cdot \frac{kip \cdot ft}{ft}$$

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$e_{\rm B} := \frac{M_{\rm uFtLC4StrI_noLS}}{F_{\rm VFtLC4StrIMin_noLS}} = 2.5 \, {\rm ft}$$

Check := if
$$\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK" \right) = "OK"$$

With the live load surcharge:

Minimum vertical force with the live load surcharge

Moment about the longitudinal axis of the footing

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$\begin{split} F_{VFtLC4StrIMin} &= 50.61 \cdot \frac{kip}{ft} \\ M_{uFtLC4StrI} &= 140.34 \cdot \frac{kip \cdot ft}{ft} \\ e_{B} &\coloneqq \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrIMin}} = 2.77 \ ft \\ Check &\coloneqq if \left(e_{B} < \frac{B_{footing}}{6} \ , "OK" \ , "Not \ OK" \right) = "OK" \end{split}$$

Step 2.7 Backwall Design

Description

This step presents the design of the backwall.

PageContents47Forces and Moments at the Base of the Backwall47Design for Flexure

- 50 Design for Shear
- 52 Shrinkage and Temperature Reinforcement Design

Forces and Moments at the Base of the Backwall

Step 2.5 presents the load effects at the base of the backwall under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VBw} (kip/ft)

	Strength I	Service I
LC I	1.20	-
LC III	1.20	-
LC IV	1.20	0.96

Factored shear force parallel to the transverse axis of the backwall, V_{uBw} (kip/ft)

	Strength I	Service I
LC I	0.49	-
LC III	0.49	-
LC IV	1.02	0.63

Factored moment about the longitudinal axis of the backwall, MuBw (kip ft/ft)

	Strength I	Service I
LC I	0.69	-
LC III	0.69	-
LC IV	1.83	1.11

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

Moment demand at the base of the backwall

$$M_{\text{DemandBackwall}} := M_{uBwLC4StrI} = 1.83 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Flexural Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 6	
Nominal diameter of a reinforcing steel bar	$d_{\text{bar}} := \text{Dia}(\text{bar}) = 0.75 \cdot \text{in}$	
Cross-section area of the bar	$A_{\text{bar}} := \text{Area}(\text{bar}) = 0.44 \cdot \text{in}^2$	
The spacing of the main reinforcing steel bars in walls a lesser of 1.5 times the thickness of the member or 18 in.	nd slabs shall not be greater than the	LRFD 5.10.3.2
Note: MDOT limits reinforcement spacing to a maximu	m of 18 in.	BDG 6.20.03 and 6.20.03A

Note: MDOT limits reinforcement spacing to a maximum of 18 in.

Backwall thickness

Select a spacing for reinforcing steel bars

 $t_{backwall} = 18 \cdot in$ $s_{bar} := 18 \cdot in$

0.3.2

LRFD 5.6.3.2

47

Select a 1-ft wide strip for the design.

Area of reinforcing steel provided in a 1-ft wide section

Effective depth

Resistance factor for flexure

Width of the compression face of the section

Stress block factor

Solve the following equation of A_s to calculate the required area of steel to satisfy the moment demand. Use an assumed initial A_s value to solve the equation.

 $\phi_{f} \coloneqq 0.9$

b := 12in

 $A_{s} := 0.3 in^{2}$

 $A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.29 \cdot in^2$

 $d_e := t_{backwall} - Cover_{bw} = 15 \cdot in$

 $A_{s,reg} := Find(A_s) = 0.03 \cdot in^2$

 $M_{CapacityBackwall} := \phi_f \cdot A_{sProvided} \cdot f_y$

 $M_{CapacityBackwall} = 19.42 \cdot \frac{kip \cdot ft}{ft}$

 $\beta_1 := \min \left| \max \left| 0.85 - 0.05 \cdot \left(\frac{f_c - 4ksi}{ksi} \right), 0.65 \right|, 0.85 \right| = 0.85$

Given $M_{\text{DemandBackwall}}$ ft = $\phi_f \cdot A_s \cdot f_y \cdot \left| d_e - \frac{1}{2} \cdot \left(\frac{A_s \cdot f_y}{0.85 \cdot f_s \cdot b} \right) \right|$

Check := $if(A_{sProvided} > A_{s.req}, "OK", "Not OK") = "OK"$

Initial assumption

Required area of steel

Check if A_{sProvided} > A_{sRequired}

Moment capacity of the section with the provided steel

Distance from the extreme compression fiber to the neutral axis

Check the validity of assumption, $f_s = f_v$

Limits for Reinforcement

 $c := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot \beta_{1} \cdot b} = 0.68 \cdot in$ Check_f_s := if $\left(\frac{c}{d_{e}} < 0.6, "OK", "Not OK"\right) = "OK"$

LRFD 5.6.3.3

 $d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} Provided \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right)$

LRFD 5.5.4.2

LRFD 5.6.2.2

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement $\gamma_1 := 1.6$ For concrete structures that are not precast segmental $\gamma_3 := 0.67$ For ASTM A615 Grade 60 reinforcement

 f_{ss} (not to exceed 0.6 f_y)

service limit state moment

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to

compression fiber to the neutral axis Given

Assumed distance from the extreme

Position of the neutral axis

of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

 $x := 3 \cdot in$

Control of Cracking by Distribution of Reinforcement

stress in the reinforcement does not exceed the service limit state stress.

condition

Distance from extreme tension fiber to the

center of the closest flexural reinforcement

steel reinforcement in the layer closest

The spacing requirement for the mild

1.33 times the factored moment demand

Check the adequacy of the section capacity

Factored moment to satisfy the minimum reinforcement requirement

Section modulus

Cracking moment

to the tension face

Exposure factor for the Class 1 exposure

Ratio of flexural strain at the extreme tension face to the strain at the centroid

 $\frac{1}{2} \cdot \mathbf{b} \cdot \mathbf{x}^2 = \frac{\mathbf{E}_s}{\mathbf{E}_c} \cdot \mathbf{A}_{s\text{Provided}} \cdot (\mathbf{d}_e - \mathbf{x})$

$$x_{na} := Find(x) = 2.234 \cdot in$$

$$T_{s} := \frac{M_{uBackwallSerI}}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 0.9 \cdot kip$$
$$f_{ss1} := \frac{T_{s}}{A_{sProvided}} = 3.19 \cdot ksi$$

$$f_{ss} := \min(f_{ss1}, 0.6f_y) = 3.19 \cdot ksi$$

$$d_c := Cover_{bw} = 3 \cdot in$$

 $s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$

 $\gamma_{e} := 1.00$

$$\beta_{\rm s} \coloneqq 1 + \frac{d_{\rm c}}{0.7(t_{\rm backwall} - d_{\rm c})} = 1.29$$

LRFD Ea. 5.6.7-1

49

 $1.33 \cdot M_{\text{DemandBackwall}} = 2.43 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 $M_{req} := min(1.33M_{DemandBackwall}, M_{cr}) = 2.43 \cdot \frac{kip \cdot ft}{ft}$

Check := if (M_{CapacityBackwall} > M_{req}, "OK", "Not OK") = "OK"

 $M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 24.06 \cdot \frac{kip \cdot ft}{ft}$

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual



According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

The maximum factored shear force at the base of the backwall	$V_{uBwLC4StrI} = 1.02 \cdot \frac{kip}{ft}$	
Effective width of the section	$b_v := b = 12 \cdot in$	
Depth of the equivalent rectangular stress block	$a := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} = 0.58 \cdot in$	
Effective shear depth	$d_{v} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{backwall}\right) = 14.71 \cdot in$	LRFD 5.7.2.8

Note: Since there is no transverse reinforcement in the backwall and the overall depth of the backwall is greater than 16 in., the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used.

The factored N_u , V_u , and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the backwall.

Factored axial force at the critical section (use negative if compression)

Lateral earth load at the critical section

Load at the critical section due to live load surcharge

Factored shear force (demand) at the critical section

Factored moment at the critical section

Check M_u since it cannot be taken less than $V_u d_v$

Net longitudinal tensile strain in the section at the centroid of the tension reinforcement

Crack spacing parameter

Maximum aggregate size (in.)

Crack spacing parameter as influenced by the maximum aggregate size

 $N_{uBackwallShear} := - \left[1.25 \cdot \left(DC_{backwall} - d_{v} \cdot t_{backwall} \cdot W_{c} \right) \right]$ $N_{uBackwallShear} = -0.85 \cdot \frac{kip}{r}$ $P_{\text{EHBackwallShear}} \coloneqq \frac{1}{2} \cdot k_{a} \cdot \gamma_{s} \cdot \left(h_{\text{backwall}} - d_{v}\right) \cdot \left(h_{\text{backwall}} - d_{v}\right)$ $P_{\text{EHBackwallShear}} = 0.16 \cdot \frac{\text{kip}}{\alpha}$ $P_{LSBackwallShear} := k_a \cdot \gamma_s \cdot h_{eq} \cdot (h_{backwall} - d_v) = 0.22 \cdot \frac{kip}{ft}$ $V_{uBackwallShear} := 1.5 \cdot P_{EHBackwallShear} + 1.75 \cdot P_{LSBackwallShear}$ $V_{uBackwallShear} = 0.63 \cdot \frac{k_{1p}}{ft}$ $M_{uBackwallShear} := 1.5 \cdot P_{EHBackwallShear} \cdot \frac{\left(h_{backwall} - d_{v}\right)}{3} \dots \\ + 1.75 \cdot P_{LSBackwallShear} \cdot \frac{\left(h_{backwall} - d_{v}\right)}{2}$ $M_{uBackwallShear} = 0.82 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ $M_{uWallShear} := max(M_{uBackwallShear}, V_{uBackwallShear} \cdot d_v)$ $M_{uWallShear} = 0.82 \cdot \frac{\text{kip} \cdot \text{ft}}{\alpha}$ $\frac{\int M_{uBackwallShear}}{d_{v}} + 0.5 \cdot N_{uBackwallShear} + V_{uBackwallShear}}$ $E_{s} \cdot \frac{A_{sProvided}}{ft}$ $\varepsilon_{\rm s} = 1.03 \times 10^{-4}$ LRFD Eq. 5.7.3.4.2-4 $s_x := d_v = 1.23 \text{ ft}$ **MDOT Standard Specifications** $a_g := 1.5$ for Construction Table 902-1 $s_{xe} := \min \left[\begin{array}{c} (3011) \\ (12in) \\ s_{x} \cdot \frac{1.38}{2 + 0.63} \end{array} \right] = 12 \cdot in \quad LRFD Eq. 5.7.3.4.2-7$

Factor indicating the ability of $\beta := \frac{4.8}{\left(1 + 750 \cdot \varepsilon_{\rm s}\right)} \cdot \frac{51}{\left(39 + \frac{s_{\rm xe}}{10}\right)} = 4.46$ LRFD Eq. 5.7.3.4.2-2 diagonally cracked concrete to transmit tension and shear Nominal shear resistance of concrete, V_n, is calculated as follows: $V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 43.9 \cdot kip$ LRFD Eq. 5.7.3.3-3 $V_{c2} := 0.25 f_c \cdot b \cdot d_e = 135 \cdot kip$ LRFD Eq. 5.7.3.3-2 $V_n := \min(V_{c1}, V_{c2}) = 43.9 \cdot \text{kip}$ $\phi_{\rm v} \coloneqq 0.9$ LRFD 5.5.4.2 Resistance factor for shear $V_r := \phi_v \cdot V_n = 39.51 \cdot kip$ Factored shear resistance (capacity) Check := if $\left(\frac{V_r}{ft} > V_{uBackwallShear}, "OK", "Not OK"\right) = "OK"$ Check if the shear capacity is greater than the demand Shrinkage and Temperature Reinforcement Design The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the backwall. **LRFD 5.10.6** The spacing of the main reinforcing steel bars in walls and slabs shall not be greater than the lesser of 1.5 times the thickness of the member or 18 in. The spacing of shrinkage and temperature reinforcement shall not exceed the following: **LRFD 5.10.6** 12 in. for walls and footings greater than 18 in. For all other situations, 3 times the component thickness but not less than 18 in. Note: MDOT limits reinforcement spacing to a maximum of 18 in. BDG 6.20.03 and 6.20.03A bar := 6 Select a trial bar size $d_{bST} := Dia(bar) = 0.75 \cdot in$ Nominal diameter of a reinforcing steel bar $A_{barST} := Area(bar) = 0.44 \cdot in^2$ Cross-section area of the bar Select a spacing for reinforcing steel bars $s_{barST} := 18 \cdot in$ For the 18 in. thick backwall $A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{SharST} = 0.29 \cdot in^2$ Horizontal reinforcing steel area provided in the section

The required minimum shrinkage and temperature reinforcement area at the backwall was previously calculated during the design of flexural reinforcement.

Required shrinkage and temperature steel area

Check if the provided steel area > the required area of shrinkage and temperature steel

 $A_{\text{shrink.temp}} = 0.14 \cdot \text{in}^2$

Check := if $(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"$

The backwall design presented in this step provides the following details:

- No. 6 bars @ 18.0 in. spacing $(A_s = 0.29 \text{ in.}^2/\text{ft})$ as the back face flexural reinforcement
- No. 6 bars @ 18.0 in. spacing $(A_s = 0.29 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 18.0 in. spacing ($A_s = 0.29 \text{ in.}^2/\text{ft}$) as the front and back face horizontal shrinkage and temperature reinforcement.

Step 2.8 Abutment Wall Design

Description

This step presents the design of the abutment wall.

Page	Contents
55	Forces and Moments at the Base of the Abutment Wall
56	Design for Flexure
59	Design for Shear
60	Development Length of Reinforcement
61	Shrinkage and Temperature Reinforcement Design

Forces and Moments at the Base of the Abutment Wall

Step 2.5 presents the load effects at the base of the abutment wall under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VWall} (kip/ft)

	Strength I	Service I
LC I	11.61	9.29
LC III	29.86	21.46
LC IV	20.01	15.83

Factored shear force parallel to the transverse axis of the abutment wall, $V_{uWall}(kip/ft)$

	Strength I	Service I
LC I	12.82	8.55
LC III	12.82	8.55
LC IV	15.70	10.39

Factored moment about the longitudinal axis of the abutment wall, M_{uWall} (kip ft/ft)

	Strength I	Service I
LC I	92.40	61.28
LC III	106.09	70.41
LC IV	131.04	88.15

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

 $M_{\text{DemandWall}} := M_{uWallLC4StrI} = 131.04 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

LRFD 5.6.3.2

Moment demand at the base of the wall

Flexural Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

har := 9

Select a trial bar size

Nominal diameter of a reinforcing steel bar	$d_{bar} := Dia(bar) = 1.13 \cdot in$	
Cross-section area of the bar	$A_{\text{bar}} := \text{Area}(\text{bar}) = 1 \cdot \text{in}^2$	
The spacing of the main reinforcing steel bars lesser of 1.5 times the thickness of the membe	in walls and slabs shall not be greater than the er or 18 in.	LRFD 5.10.3.2
The spacing of shrinkage and temperature reir wall thickness is greater than 18 in.	nforcement shall not exceed 12 in. when the	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a	a maximum of 18 in.	BDG 5.22.01
Wall thickness	$t_{wall} = 38 \cdot in$	
Select a spacing for reinforcing steel bars	$s_{bar} := 12 \cdot in$	
Select a 1-ft wide strip for the design.		
Area of reinforcing steel provided in a 1-ft wide section	$A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 1 \cdot in^2$	2
Effective depth	$d_e := t_{wall} - Cover_{wall} = 35 \cdot in$	
Resistance factor for flexure	$\phi_{f} \coloneqq 0.9$	LRFD 5.5.4.2
Width of the compression face of the section	b := 12in	
Stress block factor	$\beta_1 := \min \Biggl[\max \Biggl[0.85 - 0.05 \cdot \Biggl(\frac{f_c - 4ksi}{ksi} \Biggr), 0$.65, 0.85 = 0.85 LRFD 5.6.2.2
Solve the following equation of A_s to calculate assumed initial A_s value to solve the equation.	e the required area of steel to satisfy the moment o	demand. Use an
Initial assumption	$A_s := 1 in^2$	
	Given $M_{\text{DemandWall}} \cdot \text{ft} = \phi_{f} \cdot A_{s} \cdot f_{y} \cdot \left[d_{e} \right]$	$= \frac{1}{2} \cdot \left(\frac{\mathbf{A}_{\mathbf{s}} \cdot \mathbf{f}_{\mathbf{y}}}{0.85 \cdot \mathbf{f}_{\mathbf{c}} \cdot \mathbf{b}} \right) \qquad \mathbf{LRFD} \qquad 5.6.3.2$
Required area of steel	$A_{sRequired} := Find(A_s) = 0.85 \cdot in$	n ²
Check if $A_{sProvided} > A_{sRequired}$	Check := if $(A_{sProvided} > A_{sRequir})$	$_{\text{red}}$, "OK", "Not OK") = "OK"

Moment capacity of the section with the provided steel area

Distance from the extreme compression fiber to the neutral axis

Check the validity of assumption, $f_s = f_v$

LRFD 5.6.3.3

 $d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} Provided f_{y}}{0.85 \cdot f_{c} \cdot b} \right)$

Limits for Reinforcement

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

1.33 times the factored moment demand

The factored moment to satisfy the minimum reinforcement requirement

Check the adequacy of the section capacity

Control of Cracking by Distribution of Reinforcement

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement does not exceed the service limit state stress.

Exposure factor for the Class 1 exposure condition

$$s \le \frac{700 \cdot \gamma_{e}}{\beta_{s} \cdot f_{ss}} - 2 \cdot d_{c}$$
LRFD Eq. 5.6.7-1

$$\gamma_{e} := 1.00$$

$\gamma_1 \coloneqq 1.6$ For concrete structures that are not precast segmental $\gamma_3 := 0.67$ For ASTM A615 Grade 60 reinforcement $S_c := \frac{1}{6} \cdot b \cdot t_{wall}^2 = 2.89 \times 10^3 \cdot in^3$ $M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{f_r} = 107.25 \cdot \frac{kip \cdot ft}{f_r}$ $1.33 \cdot M_{\text{DemandWall}} = 174.29 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ $M_{req} := min(1.33M_{DemandWall}, M_{cr}) = 107.25 \cdot \frac{kip \cdot ft}{ft}$ Check := if (M_{CapacityWall} > M_{req}, "OK", "Not OK") = "OK"

Check := if $\left(\frac{c}{d_e} < 0.6, "OK", "Not OK"\right)$ = "OK"

 $M_{CapacityWall} \coloneqq \phi_f \cdot A_{sProvided} \cdot f_v$

 $M_{CapacityWall} = 153.09 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 $c := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot \beta_{1} \cdot b} = 2.31 \cdot in$

LRFD 5.6.7

Distance from extreme tension fiber to center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Given

 $x := 6 \cdot in$

Assumed distance from the extreme compression fiber to the neutral axis

Position of the neutral axis

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to service limit state moment

 f_{ss} (not to exceed 0.6 f_{v})

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement Requirement

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the wall:

Minimum area of shrinkage and

temperature reinforcement

Check if the provided area of steel > the required area of shrinkage and temperature steel

$$A_{shrink.temp} \coloneqq \min \left[\begin{array}{c} \left(0.60 \frac{in^2}{ft} \right) \\ \left[\left(0.11 \frac{in^2}{ft} \right) \\ \left[\frac{1.3 \cdot h_{wall} \cdot t_{wall} \cdot \frac{kip}{in \cdot ft}}{2(h_{wall} + t_{wall}) \cdot f_y} \right] \\ \end{array} \right] \right] \cdot ft = 0.35 \cdot in^2$$

$$Check \coloneqq if \left(A_{sProvided} > A_{shrink.temp}, "OK", "Not OK" \right) = "OK"$$

$$f_{ss1} := \frac{T_s}{A_{sProvided}} = 32.12 \cdot ksi$$

$$f_{ss} := \min(f_{ss1}, 0.6f_y) = 32.12 \cdot ksi$$

$$s_{barRequred} := \frac{700 \cdot \gamma_e \cdot \frac{kip}{in}}{\beta_s \cdot f_{ss}} - 2 \cdot d_c = 13.42 \cdot in$$
Check := if(s_{bar} < s_{barRequred}, "OK", "Not OK") = "OK"

$$d_c := Cover_{wall} = 3 \cdot in$$

$$\beta_{\rm s} := 1 + \frac{d_{\rm c}}{0.7(t_{\rm wall} - d_{\rm c})} = 1.12$$

LRFD 5.10.6

 $T_{s} := \frac{M_{u} \text{WallLC4SerI}}{d_{e} - \frac{x_{na}}{3}} \cdot \text{ft} = 32.1 \cdot \text{kip}$

 $\frac{1}{2} \cdot \mathbf{b} \cdot \mathbf{x}^{2} = \frac{\mathbf{E}_{s}}{\mathbf{E}_{c}} \cdot \mathbf{A}_{sProvided} \cdot (\mathbf{d}_{e} - \mathbf{x})$ $x_{na} := Find(x) = 6.197 \cdot in$

Design for Shear

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

 $V_{uWallLC4StrI} = 15.7 \cdot \frac{kip}{ft}$ The maximum factored shear force at the base of the abutment wall Effective width of the section $\mathbf{b}_{\mathbf{v}} := \mathbf{b} = 12 \cdot \mathbf{i} \mathbf{n}$ $a := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} = 1.96 \cdot in$ Depth of the equivalent rectangular stress block $d_{v} := max \left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{wall} \right) = 34.02 \cdot in \quad \frac{LRFD}{5.7.2.8}$ Effective shear depth Note: Since there is no transverse reinforcement in the wall and the overall depth of the wall is greater than 16 in.,

the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used.

The factored N_u, V_u, and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the abutment wall.

Factored axial force at the critical section (use negative if compression)

$$N_{uWallShear} := -\left[1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} - d_{v} \cdot t_{wall} \cdot W_{c}\right) + 1.5DW_{Sup}\right] = -18.33 \cdot \frac{kip}{ft}$$

Lateral earth load at the critical section

Load at the critical section due to live load surcharge

critical section

$$\begin{split} P_{\text{EHWallShear}} &\coloneqq \frac{1}{2} \cdot \left[k_{a} \cdot \gamma_{s} \cdot \left(h_{\text{backwall}} + h_{\text{wall}} - d_{v} \right) \right] \cdot \left(h_{\text{backwall}} + h_{\text{wall}} - d_{v} \right) \\ P_{\text{EHWallShear}} &= 6.47 \cdot \frac{\text{kip}}{\text{ft}} \\ P_{\text{LSWallShear}} &\coloneqq k_{a} \cdot \gamma_{s} \cdot h_{eq} \cdot \left(h_{\text{backwall}} + h_{\text{wall}} - d_{v} \right) = 1.36 \cdot \frac{\text{kip}}{\text{ft}} \\ V_{uWallShear} &\coloneqq 1.5 \cdot P_{\text{EHWallShear}} + 1.75 \cdot P_{\text{LSWallShear}} + 0.5 \text{TU} \\ V_{uWallShear} &= 12.23 \cdot \frac{\text{kip}}{\text{ft}} \end{split}$$

Factored moment at the critical section

Factored shear force (demand) at the

$$\begin{split} M_{uWallShear} &\coloneqq 0.9 \cdot DC_{backwall} \cdot \frac{\left(\frac{t_{backwall} - t_{wall}}{2} + \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} \right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHWallShear} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} - d_{v} \right)}{3} \dots \\ &+ 1.75 \cdot P_{LSWallShear} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} - d_{v} \right)}{3} + 0.5 \cdot TU \cdot \left(h_{wall} - d_{v} \right) \\ &M_{uWallShear} = 91.55 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Check less than V_ud_v

ft

•)

60

 $\frac{\left[\frac{M_{uWallShear}}{d_{v}} + 0.5 \cdot N_{uWallShear} + V_{uWallShear}\right]}{E_{s} \cdot \frac{A_{sProvided}}{ft}} = 1.22 \times 10^{-3}$ Net longitudinal tensile strain in the section at the centroid of the $\varepsilon_s :=$ tension reinforcement Crack spacing parameter $s_x := d_v = 2.83 \text{ ft}$ **MDOT Standard Specifications** $a_g := 1.5$ Maximum aggregate size (in.) for Construction Table 902-1 (80in) $s_{xe} := \min \left| \begin{array}{c} (80in) \\ (12in) \\ s_{x} \cdot \frac{1.38}{a_{x} + 0.63} \end{array} \right| = 22.04 \cdot in \quad LRFD Eq. \\ 5.7.3.4.2-7 \quad (80in) \\ (12in) \\ (12in$ Crack spacing parameter as influenced by the maximum aggregate size $\beta := \frac{4.8}{\left(1 + 750 \cdot \varepsilon_{s}\right)} \cdot \frac{51}{\left(39 + \frac{s_{xe}}{\cdot}\right)} = 2.09$ LRFD Eq. 5.7.3.4.2-2 Factor indicating the ability of diagonally cracked concrete to transmit tension and shear Nominal shear resistance of concrete, V_n, is calculated as follows: $V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 48.2 \cdot kip$ LRFD Eq. 5.7.3.3-3 $V_{c2} := 0.25 f_c \cdot b \cdot d_e = 315 \cdot kip$ LRFD Eq. 5.7.3.3-2 $V_n := \min(V_{c1}, V_{c2}) = 48.16 \cdot \text{kip}$ $\phi_{v} \coloneqq 0.9$ LRFD 5.5.4.2 Resistance factor for shear $V_r := \phi_V \cdot V_n = 43.34 \cdot kip$ Factored shear resistance (capacity) Check := if $\left(\frac{V_r}{ft} > V_{uWallShear}, "OK", "Not OK"\right) = "OK"$

Check if the capacity > the demand

Development Length of Reinforcement

The flexural reinforcing steel must be developed on each side of the critical section for its full development length.

Basic development length

Reinforcement location factor

Coating factor

Distance from center of the bar to the nearest concrete surface

LRFD Eq. 5.10.8.2.1a-2

No more than 12 in. concrete below

 $c_b := Cover_{wall} = 3 \cdot in$

 $x_{r1} := 1$

LRFD 5.10.8.1.2, 5.10.8.2.1



 $\lambda_{cf} := 1.5$ Epoxy coated bars with less than $3d_b$ cover

Reinforcement confinement factor	$\lambda_{\rm rc} := \frac{d_{\rm bar}}{c_{\rm b}} = 0.38$	
Excess reinforcement factor	$\lambda_{\text{er}} \coloneqq \frac{A_{\text{sRequired}}}{A_{\text{sProvided}}} = 0.85$	
Factor for normal weight concrete	$\lambda := 1$	
Required development length	$l_{d} := l_{db} \cdot \frac{\left(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er}\right)}{\lambda} = 3.76 \text{ ft} \text{LRFD Eq. 5.10.8.2.1a-1}$	
Since the footing thickness is 3 ft, an adequate space is not available for straight bars. The common practice is to use hooked bars which are set on the bottom reinforcing steel layer.		

Shrinkage and Temperature Reinforcement

The following calculations check the required am to control shrinkage and temperature stresses in th	ount of reinforcing steel in the secondary direction e abutment wall.	
The reinforcement at the front face of the abutment wall and the horizontal reinforcement at the interior should satisfy the shrinkage and temperature reinforcement requirements.		LRFD 5.10.6
The spacing of shrinkage and temperature reinform 12 in. for walls and footings greater than	cement shall not exceed the following: 18 in.	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a ma	aximum of 18 in.	BDG 5.16.01
Select a trial bar size	bar := 6	
Nominal diameter of a reinforcing steel bar	$d_{bST} := Dia(bar) = 0.75 \cdot in$	
Cross-section area of the bar	$A_{barST} := Area(bar) = 0.44 \cdot in^2$	
Select a spacing for reinforcing steel bars	$s_{barST} := 12 \cdot in$	
Reinforcing steel area provided in the section	$A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{{}^{s}barST} = 0.44 \cdot in^2$	
The required minimum shrinkage and temperature calculated during the design of flexural reinforcer	e reinforcement area at the abutment wall was previously nent.	
Required shrinkage and temperature steel area	$A_{\text{shrink.temp}} = 0.35 \cdot \text{in}^2$	
Check if the provided steel area >	Check := if $(A_{sProvidedST} > A_{shrink.temp}, "OK")$, "Not OK") = "OK"

Check if the provided steel area > the required area of shrinkage and temperature steel

The abutment wall design presented in this step provides the following details:

- No. 9 bars @ 12.0 in. spacing ($A_s = 1.0 \text{ in.}^2/\text{ft}$) as the back face flexural reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 12.0 in. spacing ($A_s = 0.44 \text{ in.}^2/\text{ft}$) as the front and back face horizontal shrinkage and temperature reinforcement.

Step 2.9 Structural Design of the Footing

Description

This step presents the structural design of the abutment footing.

Page	Contents
63	Forces and Moments at the Base of the Abutment Footing
64	Toe Design
70	Heel Design
79	Shrinkage and Temperature Reinforcement Design

Forces and Moments at the Base of the Abutment Footing

Step 2.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, FVFt (kip/ft)

	Strength I	Service I
LC I	56.79	43.32
LC III	74.75	55.33
LC IV	69.08	52.09

	Strength I	Service I
LC I	16.59	11.06
LC III	16.59	11.06
LC IV	19.85	13.12

Factored shear force parallel to the transverse axis

of the footing, V_{uFt} (kip/ft)

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/ft)

	Strength I	Service I
LC I	87.92	32.22
LC III	143.27	69.22
LC IV	140.34	71.62

Note: In this example, the length of the footing and the abutment wall is 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Toe Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:



For structural design of an eccentrically loaded foundation, a triangular or trapezoidal bearing pressure distribution is used.

LRFD 10.6.5

According to the loads in the summary tables, Load Case III under the Strength I limit state is identified as the governing load case for the design of flexure and shear at the toe.

$$F_{VFtLC3StrI} = 74.75 \cdot \frac{kip}{ft}$$
 $M_{uFtLC3StrI} = 143.27 \cdot \frac{kip \cdot ft}{ft}$

Eccentricity in the footing width direction

$$e_{\rm B} := \frac{M_{\rm u} FtLC3StrI}{F_{\rm V} FtLC3StrI} = 1.92 \cdot ft$$

Maximum and minimum bearing pressure

$$q_{max} := \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 7.37 \cdot ksf$$
$$q_{min} := \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 1.42 \cdot ksf$$

The critical section for flexural design is at the front face of the wall.

Bearing pressure at the critical section

$$q_{toe} \coloneqq q_{min} + \frac{(q_{max} - q_{min})}{B_{footing}} \cdot (B_{footing} - l_{toe}) = 5.77 \cdot ksf$$

A simplified analysis method is used in this example to determine the maximum moments at the front face of the wall by selecting load factors to produce the maximum bearing pressure and minimum resisting loads. This method is conservative and eliminates the need for using multiple combinations.

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum moment at the front face of the wall.

LRFD 5.12.8.4

 $M_{rDemand} = 62.51 \cdot \frac{kip \cdot ft}{ft}$ **Flexural Resistance** LRFD 5.6.3.2 The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses. Select a trial bar size bar := 8 Nominal diameter of a reinforcing steel bar $d_{har} := Dia(bar) = 1 \cdot in$ Cross-section area of a bar on the $A_{bar} := Area(bar) = 0.79 \cdot in^2$ flexural tension side The spacing of the main reinforcing steel bars in walls and slabs shall not be greater than the LRFD 5.10.3.2 lesser of 1.5 times the thickness of the member or 18 in. The spacing of shrinkage and temperature reinforcement shall not exceed the following: LRFD 5.10.6 12 in. for walls and footings greater than 18 in. Note: MDOT limits reinforcement spacing to a maximum of 18 in. BDG 5.16.01 and 5.22.01 Footing thickness $t_{footing} = 3 ft$ $s_{\text{bar}} := 12 \cdot \text{in}$ Select a spacing for reinforcing steel bars Select a 1-ft wide strip for the design. $A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.79 \cdot in^2$ Area of tension steel provided in a 1-ft wide strip $d_e := t_{footing} - Cover_{ft} = 32 \cdot in$ Effective depth $\phi_{f} \coloneqq 0.9$ LRFD 5.5.4.2 Resistance factor for flexure Width of the compression face of the section b := 12in Stress block factor $\beta_1 = 0.85$ Solve the following equation of As to calculate the required area of steel to satisfy the moment demand. Use an assumed initial A_s value to solve the equation. $A_s := 1 in^2$ Initial assumption Given $M_{rDemand}$ ft = $\phi_f \cdot A_s \cdot f_y$ $\left| d_e - \frac{1}{2} \cdot \left(\frac{A_s \cdot f_y}{0.85 \cdot f_c \cdot b} \right) \right|$

 $A_{sRequired} := Find(A_s) = 0.44 \cdot in^2$

Check := if (A_{sProvided} > A_{sRequired}, "OK", "Not OK") = "OK"

Required area of steel

Check if A_{sProvided} > A_{sRequired}

The moment demand at the critical section

$M_{rDemand} := q_{toe} \cdot \frac{l_{toe}^2}{2} + (q_{max} - q_{toe}) \cdot \frac{l_{toe}^2}{3} - 0.9 \cdot W_c \cdot t_{footing} \cdot \frac{l_{toe}^2}{2} - 1.0 \gamma_s \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{l_{toe}^2}{2}$

Moment capacity of the section with the provided steel

Distance from the extreme compression fiber to the neutral axis

Check the validity of the assumption, $f_s = f_v$

Limits for Reinforcement

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

1.33 times the factored moment demand

The factored moment to satisfy the minimum reinforcement requirement

Check the adequacy of section capacity

Control of Cracking by Distribution of Reinforcement

LRFD 5.6.3.3

 $\gamma_1 := 1.6$ For concrete structures that are not precast segmental $\gamma_3 := 0.67$ For ASTM A615 Grade 60 reinforcement $S_{c} := \frac{1}{6} \cdot b \cdot t_{footing}^{2} = 2.59 \times 10^{3} \cdot in^{3}$ $M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.25 \cdot \frac{kip \cdot ft}{ft}$ $1.33 \cdot M_{\text{rDemand}} = 83.14 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ $M_{req} := min(1.33M_{rDemand}, M_{cr}) = 83.14 \cdot \frac{kip \cdot ft}{ft}$ Check := if (M_{Provided} > M_{reg}, "OK", "Not OK") = "OK"

 $M_{\text{Provided}} \coloneqq \phi_{f} \cdot A_{s\text{Provided}} \cdot f_{y} \cdot \underbrace{\left[\frac{d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s\text{Provided}} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right)^{2} \right]}_{M}$

Check_ $f_s := if\left(\frac{c}{d_e} < 0.6, "OK", "Not OK"\right) = "OK"$

 $M_{\text{Provided}} = 111.01 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

 $c := \frac{A_{sProvided} f_y}{0.85 f_c \beta_1 b} = 1.82 \cdot in$

LRFD 5.6.7

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement does not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest bar

$$s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$$

$$RFD Eq. 5.6.7-1$$

$$\gamma_e := 1.00$$

$$d_c := Cover_{ff} = 4 \cdot in$$

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

$$\beta_{\rm s} \coloneqq 1 + \frac{d_{\rm c}}{0.7(t_{\rm footing} - d_{\rm c})} = 1.18$$

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, f_{ss} , requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme compression fiber to the neutral axis

Given

$$\frac{1}{2} \cdot b \cdot x^{2} = \frac{E_{s}}{E_{c}} \cdot A_{sProvided} \cdot (d_{e} - x)$$

$$x_{na} := Find(x) = 5.303 \cdot in$$

Position of the neutral axis

Vertical force and moment at the base of the footing from Load Case III under the Service I limit state are:

$$F_{VFtLC3SerI} = 55.33 \cdot \frac{kip}{ft} \qquad M_{uFtLC3SerI} = 69.22 \cdot \frac{kip \cdot ft}{ft}$$
Eccentricity in the footing width
direction under Service I limit state
$$e_{BSerI} := \frac{M_{uFtLC3SerI}}{F_{VFtLC3SerI}} = 1.25 \cdot ft$$
Maximum and minimum bearing
pressure under Service I limit state
$$q_{maxSerI} := \frac{F_{VFtLC3SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{BSerI}}{B_{footing}}\right) = 4.69 \cdot ksf$$

$$q_{minSerI} := \frac{F_{VFtLC3SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{BSerI}}{B_{footing}}\right) = 1.82 \cdot ksf$$
Bearing pressure at the critical
section under Service I limit state
$$q_{toeSerI} := q_{minSerI} + \frac{(q_{maxSerI} - q_{minSerI})}{B_{footing}} \cdot \left(B_{footing} - I_{toe}\right)$$

$$q_{toeSerI} = 3.92 \cdot ksf$$

The moment at the critical section under the Service I limit state:

$$M_{r}SerI := q_{toe}SerI \cdot \frac{l_{toe}^{2}}{2} + (q_{max}SerI - q_{toe}SerI) \cdot \frac{l_{toe}^{2}}{3} - W_{c} \cdot t_{footing} \cdot \frac{l_{toe}^{2}}{2} - \gamma_{s} \cdot (h_{toe}Depth - t_{footing}) \cdot \frac{l_{toe}^{2}}{2}$$

$$M_{r}SerI = 36.8 \cdot \frac{kip \cdot ft}{ft}$$
Tensile force in the reinforcing steel due
to the service limit state moment
$$T_{s} := \frac{M_{r}SerI}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 14.6 \cdot kip$$
Stress in the reinforcing steel due to
the service limit state moment
$$f_{ss1} := \frac{T_{s}}{A_{s}Provided} = 18.49 \cdot ksi$$

$$f_{ss}$$
 (not to exceed 0.6 f_{y})

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement Requirement

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the toe:

$$\begin{array}{l} \text{Minimum area of shrinkage and} \\ \text{temperature reinforcement} \end{array} \quad A_{\text{shrink.temp}} \coloneqq \min \left[\begin{array}{c} \left(0.60 \frac{\text{in}^2}{\text{ft}} \right) \\ \left[\left(0.11 \frac{\text{in}^2}{\text{ft}} \right) \\ \left[\frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{\text{kip}}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{\text{kip}}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{\text{kip}}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{\text{kip}}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{\text{kip}}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}} \cdot \frac{1}{\text{in} \cdot \text{ft}} \\ \frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \frac{1}{\text{i$$

Design for Shear

Effective width of the section

Depth of the equivalent rectangular stress block

Effective shear depth

The critical section for shear at the toe is located at a dista

Distance from the toe to the critical section

Bearing pressure at the critical section

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum shear at the front face of the wall.

Factored shear force (demand) at the critical section

$$V_{uFtToe} := \frac{\left(q_{max} + q_{d}\right)}{2} \cdot l_{shear} - 0.9 \cdot W_{c} \cdot t_{footing} \cdot l_{shear} - 1.0 \cdot \gamma_{s} \cdot \left(h_{toeDepth} - t_{footing}\right) \cdot l_{shear} = 12.16 \cdot \frac{kip}{ft}$$

$$d_{v} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{footing}\right) = 31.23 \cdot \text{in} \qquad \begin{array}{l} \text{LRFD} \\ \text{5.7.2.8} \end{array}$$

ance d_{v} from the front face of the wall.
 $l_{shear} := l_{toe} - d_{v} = 1.98 \text{ ft} \end{array}$

$$b = 12 \cdot in$$

$$s_{barRequired} := \frac{700 \cdot \gamma_e \cdot \frac{kip}{in}}{\beta_s \cdot f_{ss}} - 2 \cdot d_c = 24.13 \cdot in$$

Check := if
$$(s_{bar} < s_{barRequired}, "OK", "Not OK") = "OK"$$

'n.

LRFD 5.10.6

hrink temp := min
$$\begin{bmatrix} 0.60 \frac{\text{in}^2}{\text{ft}} \\ 0.11 \frac{\text{in}^2}{\text{ft}} \end{bmatrix}$$

 $f_{ss} := \min(f_{ss1}, 0.6f_y) = 18.49 \cdot ksi$

$$= 12 \cdot \text{in}$$

$$:= \frac{A_{\text{sProvided}} \cdot f_{\text{y}}}{0.85 \cdot f_{\text{s}} \cdot h} = 1.55 \cdot \text{in}$$

$$0.85 \cdot f_c \cdot b$$

 $d_v := \max\left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{footing}\right) = 31.23 \cdot in$ LRF
5.7.2

$$l_{shear} := l_{toe} - d_{v} = 1.98 \text{ ft}$$
$$q_{d} := q_{min} + \frac{\left(q_{max} - q_{min}\right)}{B_{footing}} \cdot \left(B_{footing} - l_{shear}\right) = 6.68 \cdot \text{ksf}$$

b = 12·in
a :=
$$\frac{A_s Provided f_y}{0.85 f_s h} = 1.55 \cdot in$$

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than 3d_v.

Check if the distance l_{toe} is less than $3d_{\rm v}$

Check :=
$$if(l_{toe} < 3 \cdot d_V, "Yes", "No") = "Yes"$$

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, $\boldsymbol{V}_n,$ is calculated as follows:

	$V_{c1} \coloneqq 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot \text{ksi} \cdot b \cdot d_e} = 42 \cdot \text{kip}$ $V_{c2} \coloneqq 0.25f_c \cdot b \cdot d_e = 288 \cdot \text{kip}$	LRFD Eq. 5.7.3.3-3 LRFD Eq. 5.7.3.3-2
	$V_{n} := \min(V_{c1}, V_{c2}) = 42.03 \cdot kip$	
Resistance factor for shear	$\phi_{v} := 0.9$	LRFD 5.5.4.2
Factored shear resistance (capacity)	$V_r := \phi_V \cdot V_n = 37.83 \cdot kip$	
Check if the capacity > the shear demand	Check := if $\left(\frac{V_r}{ft} > V_{uFtToe}, "OK", "Not \right)$	OK") = "OK"

 $\beta := 2$

Development Length of Reinforcement

The flexural reinforcing steel must be developed on eac full development length.	The side of the critical section for its LRFD 5.10.8.1.2
Available length for rebar development	$l_{d.available} := l_{toe} - Cover_{ft} = 4.25 \text{ ft}$
Basic development length	$l_{db} := 2.4 \cdot d_{bar} \cdot \frac{f_y}{\sqrt{f_c \cdot ksi}} = 6.93 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-2
Reinforcement location factor	$\lambda_{rl} := 1$ No more than 12 in. concrete below
Coating factor	$\lambda_{cf} := 1.5$ Epoxy coating bars with less than $3d_b$ cover
Reinforcement confinement factor	$\lambda_{rc} := 0.4$ For $c_b > 2.5$ in and No. 8 bars or smaller
Excess reinforcement factor	$\lambda_{\text{er}} := \frac{A_{\text{sRequired}}}{A_{\text{sProvided}}} = 0.56$ LRFD Eq. 5.10.8.2.1c-4
Factor for normal weight concrete	$\lambda := 1$
Required development length	$l_{d.required} := l_{db} \cdot \frac{\left(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er}\right)}{\lambda} = 2.32 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-1
Check if $l_{d.available} > l_{d.required}$	Check := if $(l_{d.available} > l_{d.required}, "OK", "Not OK") = "OK"$

Heel Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:



The self-weight of the footing, the weight of soil, live load surcharge and the bearing pressure act on the heel. The critical load combination for the design selects the load factors to produce the minimum vertical loads and maximum eccentricities resulting in the minimum bearing pressure.

The critical location for the design of flexure is located at the back face of the wall. LRFD 5.12.8.4

In the general case of a cantilever abutment wall, where the downward load on the heel is larger than the upward reaction of the soil under the heel, the top of the heel is in tension. Therefore, the critical section for shear is taken at the back face of the abutment wall.

LRFD C5.12.8.6.1

Load cases I, III, and IV under the Strength I limit state are used to calculate the maximum moment and shear at the critical sections.

Load Case I

Minimum vertical force	$F_{VFtLC1StrIMin} = 41.63 \cdot \frac{kip}{ft}$	Step 2.6, sliding resistance check
Factored moment about the longitudinal axis of the footing	$M_{uFtLC1StrI} = 87.92 \cdot \frac{kip \cdot ft}{ft}$	Step 2.6, summary table
Eccentricity in the footing width direction	$e_{\rm B} := \frac{M_{\rm uFtLC1StrI}}{F_{\rm VFtLC1StrIMin}} = 2.11 \cdot f$	ì

Maximum and minimum bearing pressure

$$q_{max} := \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.27 \cdot ksf$$
$$q_{min} := \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.62 \cdot ksf$$
$$q_{heelLC1StrI} := q_{min} + \left(q_{max} - q_{min}\right) \frac{l_{heel}}{B_{footing}} = 2.61 \cdot ksf$$

Bearing pressure at the critical section

Factored moment at the critical section

$$M_{rLC1StrI} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|heel^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{|heel}{2} - q_{min} \cdot l_{heel} \cdot \frac{|heel}{2} - \frac{1}{6} (q_{heelLC1StrI} - q_{min}) |heel^{2}$$
$$M_{rLC1StrI} = 120.08 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC1StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC1StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC1StrI} = 22.9 \cdot \frac{kip}{ft}$$

Load Case III

Two cases need to be considered: without and with the live load.

Without the live load

Minimum vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Bearing pressure at the critical section

$$F_{VFtLC3StrIMin_noLL} = 46.72 \cdot \frac{kip}{ft} \qquad \begin{array}{l} Step 2.6, sliding \\ resistance check \end{array}$$

$$M_{uFtLC3StrI_noLL} = 113.82 \cdot \frac{kip \cdot ft}{ft} \qquad \begin{array}{l} Step 2.6, eccentric load \\ limitation check \end{array}$$

$$e_{B} := \frac{M_{uFtLC3StrI_noLL}}{F_{VFtLC3StrIMin_noLL}} = 2.44 \cdot ft$$

$$q_{max} := \frac{F_{VFtLC3StrIMin_noLL}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 5.11 \cdot ksf$$

$$q_{min} := \frac{F_{VFtLC3StrIMin_noLL}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 0.39 \cdot ksf$$

$$q_{heelLC3StrI} := q_{min} + \left(q_{max} - q_{min}\right) \frac{l_{heel}}{B_{footing}} = 2.96 \cdot ksf$$

Factored moment at the critical section

$$M_{rLC3StrI_noLL} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{l_{heel}^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^{2}$$
$$M_{rLC3StrI_noLL} = 121.93 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC3StrI_noLL} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC3StrI_noLL} = 22.4 \cdot \frac{kip}{ft}$$

With the live load

Minimum vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

$$F_{VFtLC3StrIMin} = 56.27 \cdot \frac{kip}{ft}$$
 Step 2.6, sliding
resistance check

$$M_{uFtLC3StrI} = 143.27 \cdot \frac{k_{IP} \cdot ft}{ft}$$
 Step 2.6,
summary table

$$e_{\rm B} := \frac{M_{\rm u} FtLC3StrI}{F_{\rm V} FtLC3StrIMin} = 2.55 \cdot ft$$

$$q_{\text{max}} \coloneqq \frac{F_{\text{VFtLC3StrIMin}}}{B_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 6.28 \cdot \text{ksf}$$
$$q_{\text{min}} \coloneqq \frac{F_{\text{VFtLC3StrIMin}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 0.34 \cdot \text{ksf}$$

 $q_{heelLC3StrI} := q_{min} + (q_{max} - q_{min}) \frac{l_{heel}}{B_{footing}} = 3.57 \cdot ksf$

Bearing pressure at the critical section

$$M_{rLC3StrI} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{l_{heel}^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^{2}$$
$$M_{rLC3StrI} = 114.56 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC3StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC3StrI} = 19.78 \cdot \frac{kip}{ft}$$
Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge

Minimum vertical force
$$F_{VFtLC4StrIMin_noLS} = 46.72 \cdot \frac{kip}{ft}$$
Step 2.6, sliding
resistance checkFactored moment about the longitudinal axis of
the footing $M_{uFtLC4StrI_noLS} = 116.67 \cdot \frac{kip \cdot ft}{ft}$ Step 2.6, eccentric load
limitation checkEccentricity in the footing width direction $e_B \coloneqq \frac{M_uFtLC4StrI_noLS}{F_VFtLC4StrIMin_noLS} = 2.5 \cdot ft$ $e_B \coloneqq \frac{F_VFtLC4StrIMin_noLS}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 5.17 \cdot ksf$ Maximum and minimum bearing pressure $q_{min} \coloneqq \frac{F_VFtLC4StrIMin_noLS}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.33 \cdot ksf$ Bearing pressure at the critical section $q_{heelLC4StrI} \coloneqq q_{min} + (q_{max} - q_{min}) \frac{l_{heel}}{B_{footing}} = 2.96 \cdot ksf$

Factored moment at the critical section

$$M_{rLC4StrI_noLS} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{l_{heel}^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{l_{heel}}{2} - \frac{1}{6} (q_{heelLC4StrI} - q_{min}) l_{heel}^{2} M_{rLC4StrI_noLS} = 123.54 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC4StrI_noLS} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC4StrI} - q_{min}) \cdot l_{heel}$$

$$V_{uHeelLC4Strl_noLS} = 22.65 \cdot \frac{kip}{ft}$$

 $F_{VFtLC4StrIMin} = 50.61 \cdot \frac{kip}{ft}$

Step 2.6, sliding

resistance check

With the live load surcharge

Minimum vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

$$\begin{split} M_{uFtLC4StrI} &= 140.34 \cdot \frac{kip \cdot ft}{ft} & \text{Step 2.6, summary} \\ e_{B} &:= \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrIMin}} = 2.77 \cdot ft \end{split}$$

 $q_{max} \coloneqq \frac{F_{VFtLC4StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 5.89 \cdot ksf$ Maximum and minimum bearing pressure $q_{min} := \frac{F_{VFtLC4StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 0.06 \cdot ksf$ $q_{heelLC4StrI} := q_{min} + (q_{max} - q_{min}) \frac{l_{heel}}{B_{footing}} = 3.23 \cdot ksf$ Bearing pressure at the critical section

Factored moment at the critical section

$$M_{rLC4StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|hee|^{2}}{2} + 1.35 EV_{earthBk} \cdot \frac{|hee|}{2} - q_{min} \cdot l_{heel} \cdot \frac{|hee|}{2} - \frac{1}{6} (q_{heelLC4StrI} - q_{min}) l_{heel}^{2}$$
$$M_{rLC4StrI} = 127.15 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC4StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC4StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC4StrI} = 22.6 \cdot \frac{kip}{ft}$$

Moment demand at the critical section

$$M_{\text{HeelDemand}} \coloneqq \max\left(M_{\text{rLC1StrI}}, M_{\text{rLC3StrI}noLL}, M_{\text{rLC3StrI}}, M_{\text{rLC4StrI}noLS}, M_{\text{rLC4StrI}}\right) = 127.15 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Shear demand at the critical section

$$v_{\text{HeelDemand}} \coloneqq \max \left(v_{\text{u}\text{HeelLC1StrI}}, v_{\text{u}\text{HeelLC3StrI_noLL}}, v_{\text{u}\text{HeelLC3StrI}}, v_{\text{u}\text{HeelLC4StrI_noLS}}, v_{\text{u}\text{HeelLC4StrI_noLS}} \right)$$

$$V_{\text{HeelDemand}} = 22.9 \cdot \frac{\text{kip}}{\text{ft}}$$

Flexural Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 9	
Nominal diameter of a reinforcing steel bar	$d_{\text{bar}} := \text{Dia}(\text{bar}) = 1.13 \cdot \text{in}$	
Cross-section area of a bar on the flexural tension side	$A_{bar} := Area(bar) = 1 \cdot in^2$	
The spacing of the main reinforcing steel bars in walls and lesser of 1.5 times the thickness of the member or 18 in.	d slabs shall not be greater than the	LRFD 5.10.3.2
The spacing of shrinkage and temperature reinforcement 12 in. for walls and footings greater than 18 in.	shall not exceed the following:	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a maximum	of 18 in.	BDG 5.16.01 and 5.22.01

LRFD 5.6.3.2

Footing thickness	$t_{footing} = 3 ft$	
Select a spacing for reinforcing steel bars	$s_{bar} := 10 \cdot in$	
Select a 1-ft wide strip for the design.		
Area of tension steel provided in a 1-ft wide strip	$A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 1.2 \cdot in^2$	
Effective depth	$d_e := t_{footing} - Cover_{ft} = 32 \cdot in$	
Resistance factor for flexure	$\phi_{f} := 0.9$ LRFD 5.5.4.2	
Width of the compression face of the section	$\mathbf{b} := 12\mathbf{i}\mathbf{n}$	
Stress block factor	$\beta_1 = 0.85$	
Solve the following equation of A_s to calculate the red assumed initial A_s value to solve the equation.	quired area of steel to satisfy the moment demand. Use an	
Initial assumption	$A_s := 1in^2$	
	Given $M_{\text{HeelDemand}} \cdot \text{ft} = \phi_{f} \cdot A_{s} \cdot f_{y} \cdot \left[d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) \right]$	
Required area of steel	$A_{sRequired} := Find(A_s) = 0.91 \cdot in^2$	
Check if A _{sProvided} > A _{sRequired}	Check := if $(A_{sProvided} > A_{sRequired}, "OK", "Not OK") = "OK"$	"
Moment capacity of the section with the provided steel	$M_{Provided} := \phi_{f} \cdot A_{sProvided} \cdot f_{y} \cdot \underbrace{\left[d_{e} - \frac{1}{2} \cdot \left(\frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) \right]}_{ft}$	
	$M_{\text{Provided}} = 166.45 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$	
	$A_{sProvided} \cdot f_{v}$	

Distance from the extreme compression fiber to the neutral axis

Check the validity of the assumption, $f_s = f_v$

$$M_{\text{Provided}} = 166.45 \cdot \frac{1}{\text{ft}}$$

$$c := \frac{A_{\text{sProvided}} \cdot f_{\text{y}}}{0.85 \cdot f_{\text{c}} \cdot \beta_{1} \cdot b} = 2.77 \cdot \text{in}$$

$$Check_f_{\text{s}} := if\left(\frac{c}{d_{\text{e}}} < 0.6, "\text{OK"}, "\text{Not OK"}\right) = "\text{OK"}$$

Limits for Reinforcement

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement



For concrete structures that are not precast segmental

For ASTM A615 Grade 60 reinforcement

LRFD 5.6.3.3

Section modulus
$$S_c := \frac{1}{6} \cdot b \cdot t_{footing}^2 = 2.59 \times 10^3 \cdot in^3$$
Cracking moment $M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.25 \cdot \frac{kip \cdot ft}{ft}$ 1.33 times the factored moment demand $1.33 \cdot M_{HeelDemand} = 169.12 \cdot \frac{kip \cdot ft}{ft}$ The factored moment to satisfy the
minimum reinforcement requirement $M_{req} := min(1.33M_{HeelDemand}, M_{cr}) = 96.25 \cdot \frac{kip \cdot ft}{ft}$ Check the adequacy of section capacityCheck := if(M_{Provided} > M_{req}, "OK", "Not OK") = "OK"

Control of Cracking by Distribution of Reinforcement

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, fss, requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme
compression fiber to the neutral axis

$$\begin{aligned}
\mathbf{x} &:= 5 \cdot \mathbf{in} \\
\text{Given} \quad \frac{1}{2} \cdot \mathbf{b} \cdot \mathbf{x}^2 = \frac{\mathbf{E}_s}{\mathbf{E}_c} \cdot \mathbf{A}_{sProvided} \cdot (\mathbf{d}_e - \mathbf{x}) \\
\text{Position of the neutral axis} \\
\text{Maximum and minimum bearing pressure} \\
\text{under Service I limit state} \\
\text{(from the toe design)} \\
\text{Bearing pressure at the critical section} \\
\text{ReelSerI} &:= q_{minSerI} + \frac{(q_{maxSerI} - q_{minSerI})}{\mathbf{B}_{footing}} \cdot \mathbf{1}_{heel} = 3.38 \cdot ksf \end{aligned}$$

LRFD 5.6.7

LRFD Eq. 5.6.7-1

$$\beta_{\rm S} \coloneqq 1 + \frac{d_{\rm c}}{0.7(t_{\rm footing} - d_{\rm c})} =$$

 $s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$

 $d_c := Cover_{ft} = 4 \cdot in$

 $\gamma_e := 1.00$

$$\beta_{\rm s} \coloneqq 1 + \frac{\mathbf{d}_{\rm c}}{0.7 \left(\mathbf{t}_{\rm footing} - \mathbf{d}_{\rm c} \right)} = 1.18$$

$$B_{s} := 1 + \frac{d_{c}}{0.7(t_{c-s}; t_{c-s} - d_{s})} = 1.$$

76

$$\begin{split} & \mathsf{M}_{hcelSerI} \coloneqq \mathsf{W}_{c} \mathsf{t}_{footing} \cdot \frac{\mathsf{l}_{hcel}}{2} + \mathsf{EV}_{earthBk} \cdot \frac{\mathsf{l}_{hcel}}{2} \cdots \\ & + \mathsf{V}_{LSFooting} \cdot \frac{\mathsf{l}_{hcel}}{2} - \mathsf{q}_{minSerl} \cdot \frac{\mathsf{l}_{hcel}}{2} - \left(\mathsf{q}_{HeelSerl} - \mathsf{q}_{minSerl}\right) \cdot \frac{\mathsf{l}_{hcel}}{6} \\ & \mathsf{M}_{hcelSerI} = 41.33 \cdot \frac{\mathsf{kip} \cdot \mathsf{f}}{\mathsf{f}} \\ & \mathsf{Tensile force in the reinforcing steel due to the service limit state moment} \\ & \mathsf{T}_{s} \coloneqq \frac{\mathsf{M}_{hcelSerI}}{\mathsf{d}_{c}} - \frac{\mathsf{x}_{na}}{3} \cdot \mathsf{f} = 16.6 \cdot \mathsf{kip} \\ & \mathsf{d}_{c} - \frac{\mathsf{x}_{na}}{3} \cdot \mathsf{f} = 13.84 \cdot \mathsf{ksi} \\ & \mathsf{stess in the reinforcing steel due to the service limit state moment} \\ & \mathsf{f}_{ss1} \coloneqq \frac{\mathsf{T}_{s}}{\mathsf{A}_{s}\mathsf{provided}} = 13.84 \cdot \mathsf{ksi} \\ & \mathsf{Required reinforcement spacing} \\ & \mathsf{Required reinforcement spacing} \\ & \mathsf{Sharkequired} \coloneqq \frac{700 \cdot \mathsf{v}_{c} \cdot \frac{\mathsf{kip}}{\mathsf{in}}}{\mathsf{\beta}_{s} \mathsf{f}_{ss}} - 2 \cdot \mathsf{d}_{c} = 34.92 \cdot \mathsf{in} \\ & \mathsf{Check} \Leftrightarrow \mathsf{if} \mathsf{th} \mathsf{spacing provided} < \\ & \mathsf{Check} \coloneqq \mathsf{if} (\mathsf{s}_{bar} < \mathsf{s}_{barRequired}, "OK", "Not OK") = "OK" \\ & \mathsf{The required minimum shrinkage and temperature reinforcement area was calculated previously for the toe.} \\ & \mathsf{Required minimum shrinkage and temperature steel area \\ & \mathsf{A}_{shrink.temp} = 0.33 \cdot \mathsf{in}^{2} \\ & \mathsf{Check} \coloneqq \mathsf{if} (\mathsf{A}_{sProvided} > \mathsf{A}_{shrink.temp}, "OK", "Not OK") = "OK" \\ & \mathsf{Design for Shear} \\ \end{array}$$

The critical section for shear in the heel is located at the back face of the abutment wall.

Shear demand at the critical section (max. from the load cases)

Effective width of the section

Depth of the equivalent rectangular stress block

LRFD C5.12.8.6.1

$$V_{\text{HeelDemand}} = 22.9 \cdot \frac{\text{kip}}{\text{ft}}$$

 $b = 12 \cdot in$

$$a := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} = 2.35 \cdot in$$

Effective shear depth

$$d_{V} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{footing}\right) = 30.82 \cdot in$$
 LRFD 5.7.2.8

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than 3d_v.

Check if the distance $l_{heel} < 3d_v$

Check := if
$$(l_{heel} < 3 \cdot d_v, "Yes", "No") = "No"$$

LRFD 5.7.3.4.1

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n, is calculated as follows:

 $V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 42 \cdot kip$ LRFD Eq. 5.7.3.3-3 $V_{c2} := 0.25 f_c \cdot b \cdot d_e = 288 \cdot kip$ LRFD Eq. 5.7.3.3-2 $V_n := \min(V_{c1}, V_{c2}) = 42.03 \cdot kip$ $\phi_{\rm V} \coloneqq 0.9$ LRFD 5.5.4.2 Resistance factor for shear $V_r := \phi_V \cdot V_n = 37.83 \cdot kip$ Factored shear resistance (capacity) Check := if $\left(\frac{V_r}{ft} > V_{\text{HeelDemand}}, "OK", "Not OK"\right) = "OK"$ Check if the shear capacity > the demand

 $\beta := 2$

Development Length of Reinforcement

The flexural reinforcing steel must be developed on each full development length.	n side of the critical section for its LRFD 5.10.8.1.2
Available length for rebar development	$l_{d.available} := l_{heel} - Cover_{ft} = 8.92 \text{ ft}$
Basic development length	$l_{db} := 2.4 \cdot d_{bar} \cdot \frac{f_y}{\sqrt{f_c \cdot ksi}} = 7.82 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-2
Reinforcement location factor	$\lambda_{rl} := 1.3$ More than 12 in. concrete below
Coating factor	$\lambda_{\rm cf} \coloneqq 1.5$
Reinforcement confinement factor	$\lambda_{\rm rc} := 0.4$
Excess reinforcement factor	$\lambda_{\text{er}} := \frac{A_{\text{sRequired}}}{A_{\text{sProvided}}} = 0.76$ LRFD Eq. 5.10.8.2.1c-4
Factor for normal weight concrete	$\lambda := 1$
Required development length	$l_{d.required} \coloneqq l_{db} \cdot \frac{\left(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er}\right)}{\lambda} = 4.61 \text{ ft} \begin{array}{c} \text{LRFD Eq.} \\ \text{5.10.8.2.1a-1} \end{array}$
Check if $l_{d.available} > l_{d.required}$	Check := if $(l_{d.available} > l_{d.required}, "OK", "Not OK") = "OK"$

Shrinkage and Temperature Reinforcement Design

The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing.

The reinforcement along the longitudinal direction of the footing at the top and bottom should LRFD 5.10.6 satisfy the shrinkage and temperature reinforcement requirements.

bar := 6

The spacing of shrinkage and temperature reinforcement shall not exceed the following: 12 in. for walls and footings greater than 18 in.

Note: MDOT limits reinforcement spacing to a maximum of 18 in.

Select a trial bar size

Nominal diameter of a reinforcing steel bar

Cross-section area of the bar

Select a spacing for reinforcing steel bars

Reinforcing steel area provided in the section

Required minimum area of shrinkage and temperature reinforcement in the footing

Check if the provided steel area > the required area for shrinkage and temperature steel

$$A_{barST} := Area(bar) = 0.44 \cdot in^{2}$$

$$s_{barST} := 12 \cdot in$$

$$A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{s_{barST}} = 0.44 \cdot in^{2}$$

LRFD 5.10.6

BDG 5.16.01 and 5.22.01

$$A_{\text{shrink.temp}} = 0.33 \cdot \text{in}^2$$

 $d_{bST} := Dia(bar) = 0.75 \cdot in$

Check := if $(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"$

The footing design presented in this step provides the following details:

- No. 9 bars @ 10.0 in. spacing ($A_s = 1.0 \text{ in.}^2/\text{ft}$) as the transverse flexural reinforcement at the top of the footing
- No. 8 bars @ 12.0 in. spacing (A_s=0.79 in.²/ft) as the transverse flexural reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing (A_s = 0.44 in.²/ft) as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.



Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

Appendix 2.A Braking Force and Wind Load Calculation

Description

This appendix presents the braking force and wind load calculation procedures for illustrative purposes.

Braking Force

Since the abutments have expansion bearings, the fixed bearings at the pier resist the braking force along the longitudinal direction of the bridge.

The braking force (BR) shall be taken as the greater of:

LRFD 3.6.4

25% of the axle weight of the design truck / tandem
5% of the design truck / tandem weight plus lane load

The braking force is applied on all design lanes assuming that the bridge carries traffic in one direction.

Braking force per lane due to 25% of the axle weight of the design truck / tandem

 $BR_1 := 25\% \cdot (32kip + 32kip + 8kip) = 18 \cdot kip$

Braking force per lane due to 5% of the design truck / tandem weight plus plus lane load

$$BR_2 := 5\% \cdot \left(72kip + 0.64 \frac{kip}{ft} \cdot 2L_{span} \right) = 10 \cdot kip$$

Note: The MDOT practice, as reflected in the BDS, is to take only 5% of the design truck plus lane load as the breaking force. In addition, the HL-93 modification factor is not included in the braking force calculation. This example describes the MDOT practice.

Braking force selected for the design

```
BRK := BR_2 = 10 \cdot kip
```

The braking force transmitted to the bearings based on the number of lanes with the live load.

Braking force due to 1 loaded lane	$BRK_{1L} := BRK \cdot MPF(1) = 12 \cdot kip$
Braking force due to 2 loaded lanes	$BRK_{2L} := 2BRK \cdot MPF(2) = 20 \cdot kip$
Braking force due to 3 loaded lanes	$BRK_{3L} := 3BRK \cdot MPF(3) = 25.5 \cdot kip$
Braking force due to 4 loaded lanes	$BRK_{4L} := 4BRK \cdot MPF(4) = 26 \cdot kip$
Braking force due to 5 loaded lanes	$BRK_{5L} := 5BRK \cdot MPF(5) = 32.5 \cdot kip$

The braking force is assumed to be equally shared by the bearings at the pier.

Wind Load

Since the expansion bearings are located over the abutments, the fixed bearings at the pier resist the longitudinal component of the wind load acting on the superstructure.

Wind Load on Superstructure

LRFD 3.8.1.1, 3.8.1.2

To calculate the wind load acting on the superstructure, the total depth from the top of the barrier to the bottom of the girder is required. Once the total depth is known, the wind exposure area is calculated. The wind pressure and the exposure area are used to calculate the wind load.

Total depth of the superstructure	$D_{total} := h_{Rail}$	$triang + t_{Deck} + t_{Haunch} + d_{Girder} = 7.08 \text{ ft}$
Span length for the superstructure wind load on the abutment	$L_{\text{Wind}} \coloneqq \frac{L_{\text{spa}}}{2}$	$\frac{\mathrm{dn}}{\mathrm{d}t} = 50\mathrm{ft}$
Effective wind area for the superstructure wind load on the abutment	A _{WindSuper} :=	$D_{total} \cdot L_{Wind} = 354.17 \text{ft}^2$
Basic wind speed (mph)	V _w := 115	LRFD 3.8.1.1
Gust effect factor	Gust := 1	LRFD Table 3.8.1.2.1-1, no sound barrier

Drag coefficient, superstructure	C _{DSup} := 1.1	LRFD Table 3.8	3.1.2.1-2
Superstructure height (ft), assuming that the structure height is less than 33 ft	Z := 33		
Wind exposure category			
Pressure exposure and elevation coefficient for Strength III and Service IV load combinations	$K_{ZSup} := \frac{\left(2.5 \cdot 1\right)}{2.5 \cdot 1}$	$\frac{n\left(\frac{Z}{0.9832}\right) + 6.87\right)^2}{345.6} = 0.71$	LRFD Eq. 3.8.1.2.1-2
Wind pressure on superstructure, Strength III, Service IV (ksf)	PZSup.StrIII.ServIV :=	$2.56 \cdot 10^{-6} \cdot K_{ZSup} \cdot V_w^2 \cdot Gus$	t $C_{\text{DSup}} = 0.03$
Wind pressure on superstructure, Strength V, Service I (ksf)	PZSup.StrV.ServI := 2.5	$56 \cdot 10^{-6} \cdot V_{W}^{2} \cdot \text{Gust} \cdot \text{C}_{\text{DSup}} =$	= 0.04 LRFD Eq. 3.8.1.2.1-1
The wind load from the superstructure tran angle of the wind. The attack angle is mea axis of the bridge.	nsmitted to the abutment dependence asured from a line perpendicu	ends on the attack alar to the longitudinal	LRFD 3.8.1.2.2
Since the span length and height of this gir respectively, the following wind load com	rder bridge are less than 150 ponents are used:	ft and 33 ft	LRFD 3.8.1.2.3a
 Transverse: 100 percent of the wind l perpendicular to the longitudinal axis Longitudinal: 25 percent of the transv 	oad calculated based on wind of the bridge yerse load.	d direction	
The transverse component of the wind loa	ad acting on the abutment		
WS _{STran.StrIII.Se}	$rvIV := P_{ZSup.StrIII.Serv}$	$V \cdot ksf \cdot A_{WindSuper} = 9.35 \cdot 1$	kip
WS _{STran.Str} V.Ser	$v_{I} := P_{ZSup.StrV.ServI}$ ks	$f \cdot A_{WindSuper} = 13.19 \cdot kip$	
Wind Load on Substructure			
The wind pressure on the abutment wall is an embankment fill.	s ignored since the wall is usu	ally shielded from wind by win	gwalls or
Wind Load on Live Load			
 Since the span length and height of this girespectively, the following wind load com 0.10 klf, transverse 0.04 klf, longitudinal. 	rder bridge are less than 150 ponents are used:	ft and 33 ft	LRFD 3.8.1.3
The transverse and longitudinal component	nts of the wind load acting or	n the live load and transmitted to	the abutment
$WL_{Tran} := 0.1 \frac{kir}{ft}$	$-L_{\text{Wind}} = 5 \cdot \text{kip}$		
$WL_{Long} := 0.04 - \frac{k}{2}$	$\frac{\mathrm{dip}}{\mathrm{ft}} \cdot \mathrm{L}_{\mathrm{Wind}} = 2 \cdot \mathrm{kip}$		

Appendix 2.B Sliding Resistance Check for Spread Footings on Clay

Description

This appendix presents the calculation procedure for checking the sliding resistance of spread footings located on a clay layer.

Undrained shear strength (provided by the Geotechnical Service Section)



For footings that rest on clay, where footings are supported on at least 6.0 in. of compacted granular material, the sliding resistance may be taken as the lesser of

- the cohesion of the clay, or
- one-half the normal stress on the interface between the footing and soil.



Figure 10.6.3.4-1—Procedure for Estimating Nominal Sliding Resistance for Walls on Clay

 $\phi_{\tau} \coloneqq 0.85$

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used.

- Live load on the bridge is excluded.
- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to the horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Resistance factor for sliding

LRFD Table 10.5.5.5.2-1

According to the loads in the summary tables provided at the end of Step 2.5, LC I or IV could control the design. Therefore, both load cases are checked.

Load Case I

Factored shear force parallel to the transverse axis of the footing

Factored sliding force (demand)

Minimum vertical load

Eccentricity in the footing width direction

$$V_{uFtLC1StrI} = 16.59 \cdot \frac{kip}{ft}$$

$$V_{sliding} \coloneqq V_{uFtLC1StrI} = 16.59 \cdot \frac{kip}{ft}$$

$$F_{VFtLC1StrIMin} = 41.63 \cdot \frac{kip}{ft}$$

$$e_{B} \coloneqq \frac{M_{uFtLC1StrI}}{F_{VFtLC1StrIMin}} = 2.11 \cdot ft$$

LRFD 10.6.3.4

Maximum and minimum bearing pressure

$$\begin{split} q_{max} &\coloneqq \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.27 \cdot ksf \\ q_{min} &\coloneqq \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.62 \cdot ksf \\ B_{Su} &\coloneqq B_{footing} \cdot \frac{q_{max} - 2 \cdot S_u}{q_{max} - q_{min}} = 5.93 \text{ ft} \\ V_{resistance} &\coloneqq \varphi_{\tau} \cdot \left[B_{Su} \cdot S_u + \frac{1}{2} \cdot \left(B_{footing} - B_{Su}\right) \left(\frac{1}{2}q_{min} + S_u\right)\right] \\ V_{resistance} &= 16.09 \cdot \frac{kip}{ft} \\ Check &\coloneqq if \left(V_{resistance} > V_{sliding}, "OK", "Not OK"\right) = "Not OK" \end{split}$$

greater than 2S_u

Width of the footing with a normal stress

Sliding resistance (capacity)

Check if V_{resistance} > V_{sliding}

Therefore, the sliding resistance is inadequate. Since MD footing to enhance the sliding resistance. When the footin EPS as a backfill material.

Load Case IV

Factored shear force parallel to the transverse axis of the footing

Factored sliding force (demand)

Minimum vertical load

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Width of the footing with a normal stress greater than 2S_u

$$V_{resistance} = 16.09 \cdot \frac{kip}{ft}$$

$$v_{resistance} > V_{sliding}, "OK", "Not OK") = "Not OK"$$

$$v_{oT} \text{ typically does not use keyways, consider widening the ng width is too excessive and uneconomical, consider using}$$

$$V_{uFtLC4StrI} = 19.85 \cdot \frac{kip}{ft}$$

$$V_{sliding} \coloneqq V_{uFtLC4StrI} - 1.75P_{LSFooting} = 16.73 \cdot \frac{kip}{ft}$$

$$F_{VFtLC4StrIMin_noLS} = 46.72 \cdot \frac{kip}{ft} \quad From Step 2.6, sliding resistance check}$$

$$e_{B} \coloneqq \frac{M_{uFtLC4StrI_noLS}}{F_{VFtLC4StrIMin_noLS}} = 2.5 \cdot ft$$

$$q_{\text{max}} \coloneqq \frac{\text{FVFtLC4StrIMin_noLS}}{\text{B}_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot e_{\text{B}}}{\text{B}_{\text{footing}}}\right) = 5.17 \cdot \text{ksf}$$

$$q_{\min} := \frac{F_{VFtLC4StrIMin_noLS}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 0.33 \cdot ksf$$

$$B_{Su} \coloneqq B_{footing} \cdot \frac{q_{max} - 2 \cdot S_u}{q_{max} - q_{min}} = 7.62 \text{ ft}$$

$$V_{\text{resistance}} \coloneqq \phi_{\tau} \cdot \left[B_{\text{Su}} \cdot S_{\text{u}} + \frac{1}{2} \cdot \left(B_{\text{footing}} - B_{\text{Su}} \right) \left(\frac{1}{2} q_{\min} + S_{\text{u}} \right) \right]$$
$$V_{\text{resistance}} = 16.34 \cdot \frac{\text{kip}}{\text{ft}}$$
$$Check \coloneqq \text{if} \left(V_{\text{resistance}} > V_{\text{sliding}}, "OK", "Not OK" \right) = "Not OK"$$

Check if V_{resistance} > V_{sliding}

Therefore, the sliding resistance is inadequate. Since MDOT typically does not use keyways, consider widening the footing to enhance the sliding resistance. When the footing width is too excessive and uneconomical, consider using EPS as a backfill material.

Section 3 Abutment with Spread Footing and EPS Backfill

Step 3.1 Preliminary Abutment Dimensions

Description

This step presents the selected preliminary abutment dimensions.

The design criteria, bridge information, material properties, reinforcing steel cover requirements, soil types and properties, along with superstructure loads in this section are taken from Section 2.

►

This section presents the design of a full-depth reinforced concrete cantilever abutment with expanded polystyrene (EPS) blocks as the lightweight backfill material.

Geofoam made with EPS is effective at reducing lateral forces or settlement potential for bridge abutments (MDOT Geotechnical Manual 2019). The selection of a specific Geofoam grade depends on the project needs. A typical Geofoam embankment consists of the foundation soils, the Geofoam fill, and a load dissipater slab designed to transfer loads to the Geofoam.

Design guidelines for Geofoam embankments are provided in the National Cooperative Highway Research Program (NCHRP) web document 65, titled *Geofoam Applications in the Design and Construction of Highway Embankments (Stark et al., 2004).* It is cited as NCHRP w65 in this design example.

The designer should select the preliminary dimensions based on state-specific standards and past experience. The following figure shows the abutment geometry and dimensional variables:



Abutment length	$L_{abut} := W_{deck} = 63.75 \text{ ft}$	
This abutment has an independent backwall with a sliding of	deck slab.	BDG 6.20.03A
Backwall height	$h_{backwall} := 4.25 ft$	
Backwall thickness	$t_{backwall} := 1 ft + 6 in = 1.5 f$	t
Abutment wall height	$h_{wall} := 17.54 ft$	
Abutment wall thickness	$t_{wall} := 3ft + 2in = 3.167 ft$	
Distance from the toe to the front face of the abutment wall	$l_{toe} := 6ft + 4in = 6.333 ft$	
Distance from the heel to the back face of the abutment wall	$l_{heel} := 4ft$	
Distance from center of the bearing pad to the back face of the abutment wall	$l_{brtowall} \coloneqq 2ft + 4in = 2.333$	ft
Footing width	$B_{footing} \coloneqq l_{toe} + l_{heel} + t_{wa}$	11 = 13.5 ft
Footing length	$L_{footing} \coloneqq L_{abut} + 1ft + 1ft$	= 65.75 ft
Note: The footing is extended 1 ft beyond the end of the w	vall on either side.	
Footing thickness	$t_{footing} := 3ft$	
Toe fill depth to the bottom of the footing	$h_{toeDepth} := 7ft$	
Note: Bottoms of footings are normally set 4 ft below the e avoid frost heave.	existing or proposed ground line to	BDM 7.03.02 D
Passive earth pressure is excluded from the footing design	L.	BDM 7.03.02 F
For the backfill EPS blocks, assume the following properties	s:	
Unit weight of EPS blocks	$\gamma_{\rm EPS} \coloneqq 2 \frac{1b}{{\rm ft}^3}$	Michigan Geotechnica Manual page 109
Slope angle of the EPS block end profile	$\theta := 45 \deg$	
Internal friction angle of the backfill soil	$\phi := 32 \text{deg}$	
e friction angle of EPS/soil interface is typically assumed to	be equal to φ.	NCHRP w65
Friction angle of EPS/soil interface	$\delta_{\text{A}} := \phi = 32 \cdot \text{deg}$	

Active lateral earth pressure coefficient for the EPS blocks (based on the Coulomb's classical earth-pressure theory)	$k_{\text{EPS}} := \left(\frac{\sin(\theta - \phi) \cdot \frac{1}{\sin(\theta)}}{\sqrt{\sin(\theta + \delta)} + \sqrt{\frac{\sin(\phi + \delta) \cdot \sin(\phi)}{\sin(\theta)}}} \right)^{2}$ $k_{\text{EPS}} = 0.031$ NCHRP w65
Height of the EPS blocks	$h_{EPS} := 12ft$
Depth of the soil between bottom of the EPS blocks and top of the footing	$h_{SoilBelowEPS} := 2ft$
Height of backfill soil above the EPS blocks	$h_{SoilAboveEPS} := h_{wall} + h_{backwall} - h_{EPS} - h_{SoilBelowEPS} = 7.79 \text{ ft}$

If the fill above the EPS blocks is greater than 8 ft, the compressive strength of the blocks needs to be checked.

According to the MDOT Geotechnical Manual (2019), EPS blocks should not be used where the water table could rise and make geoform unstable due to buoyant forces. The structural engineer and the geotechnical engineer need to work together and check EPS stability for a 100-year flood.

Step 3.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of the future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$DC_{Sup} := \frac{2 \cdot R_{DCEx} + (N_{beams} - 2) \cdot R_{DCIn}}{L_{abut}} = 5.658 \cdot \frac{kip}{ft}$$

$$DW_{Sup} := \frac{2 \cdot R_{DWEx} + (N_{beams} - 2) \cdot R_{DWIn}}{L_{abut}} = 0.886 \cdot \frac{kip}{ft}$$

$$DC_{backwall} := h_{backwall} \cdot t_{backwall} \cdot W_{c} = 0.956 \cdot \frac{kip}{ft}$$

$$DC_{wall} := h_{wall} \cdot t_{wall} \cdot W_{c} = 8.332 \cdot \frac{kip}{ft}$$

$$DC_{footing} := B_{footing} \cdot t_{footing} \cdot W_{c} = 6.075 \cdot \frac{kip}{ft}$$

Step 3.3 Application of Live Load

Description

Please refer to Step 2.3. The same loads are applied following the procedures described in Step 2.3.

►

Step 3.4 Application of Other Loads

Description

This step typically includes the calculation of braking force, wind load, earth load, and temperature load.

The calculation of "Other Loads", except the earth load, is identical to Step 2.4. Since EPS blocks are used as the backfill and a different spread footing width is selected, the calculation of the earth load is different. Therefore, this step only presents the earth load calculation. Please refer to Step 2.4 for the rest of the calculations.

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the information received from the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. When possible, the hydrostatic pressure should be avoided at abutments and retaining walls using an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral pressure and the resultant force due to earth pressure are calculated.

The lateral component of the earth load on the abutment consists of seven parts as listed below and shown in the following figure:

EH 1: the lateral pressure from the soil located above the EPS blocks

EH 2: the lateral pressure due to the vertical load at the top of the EPS blocks

EH 3: the lateral pressure from the soil located behind the EPS blocks

EH 4: the lateral pressure from the soil located below the EPS blocks and above the top of the footing

EH 5: the lateral pressure due to the vertical load at the bottom of the EPS blocks

EH 6: the lateral pressure due to the vertical load at the top of the footing

EH 7: the lateral pressure from the soil located along the depth (thickness) of the footing.



Backwall

Lateral earth pressure at the base

 $p_{bw} := k_a \cdot \gamma_s \cdot h_{backwall} = 0.153 \cdot ksf$

Lateral load

 $P_{\text{EHBackwall}} \coloneqq \frac{1}{2} \cdot p_{\text{bw}} \cdot h_{\text{backwall}} = 0.325 \cdot \frac{\text{kip}}{\text{ft}}$

Abutment Wall

The calculation of lateral loads on the abutment wall with EPS blocks as the backfill follows the procedure outlined in the NCHRP web document 65, titled *Geoform Applications in the Design and Construction of Highway Embankments* by Stark et al. (2004).

Height of backfill soil above the EPS blocks

EH 1:

Lateral earth pressure at the top of EPS blocks

Lateral load from the soil located above the EPS blocks

EH 2:

Lateral earth pressure due to the vertical load at the top of the EPS blocks

Lateral load due to the vertical load at the top of the EPS blocks

EH 3:

Lateral earth pressure from the soil located behind the EPS blocks

Lateral load from the soil located behind the EPS blocks

EH 4:

Lateral earth pressure from the soil located below the EPS blocks and above the top of the footing

Lateral load from the soil located below the EPS blocks and above the top of the footing

EH 5:

Lateral earth pressure due to the vertical load at the bottom of the EPS blocks

Lateral load due to the vertical load at the bottom of the EPS blocks

Total resultant lateral load at the base of the wall

 $h_{SoilAboveEPS} = 7.79 \, \text{ft}$

LRFD Eq. 3.11.5.1-1

LRFD Eq. 3.11.5.1-1

$$p_{AboveEPS} := k_a \cdot \gamma_s \cdot h_{SoilAboveEPS} = 0.28 \cdot ksf$$

$$P_{EH1} := \frac{1}{2} \cdot p_{AboveEPS} \cdot h_{SoilAboveEPS} = 1.092 \cdot \frac{kip}{ft}$$

$$p_{VEPS} := \frac{1}{10} \gamma_s \cdot h_{SoilAboveEPS} = 0.093 \cdot ksf$$
 NCHRP w65

1.....

$$P_{EH2} := p_{VEPS} \cdot h_{EPS} = 1.122 \cdot \frac{\kappa p}{ft}$$

$$p_{\text{SoilBehind}} \coloneqq k_{\text{EPS}} \gamma_{\text{s}} \cdot h_{\text{EPS}} = 0.045 \cdot \text{ksf}$$
$$P_{\text{EH3}} \coloneqq \frac{1}{2} \cdot p_{\text{SoilBehind}} \cdot h_{\text{EPS}} = 0.268 \cdot \frac{\text{kip}}{\text{ft}}$$

 $p_{SoilBelowEPS} := k_a \cdot \gamma_s \cdot h_{SoilBelowEPS} = 0.072 \cdot ksf$

$$P_{EH4} := \frac{1}{2} \cdot p_{SoilBelowEPS} \cdot h_{SoilBelowEPS} = 0.072 \cdot \frac{kip}{ft}$$

 $p_{VSoilBelowEPS} := k_a \cdot \left(\gamma_s \cdot h_{SoilAboveEPS} + \gamma_{EPS} \cdot h_{EPS} \right) = 0.288 \cdot ksf$

$$P_{EH5} := p_{VSoilBelowEPS} \cdot h_{SoilBelowEPS} = 0.575 \cdot \frac{kip}{ft}$$
$$P_{EHWall} := P_{EH1} + P_{EH2} + P_{EH3} + P_{EH4} + P_{EH5} = 3.129 \cdot \frac{kip}{ft}$$

Total moment of the lateral earth load at the base of the wall

$$\begin{split} M_{EHWall} &\coloneqq P_{EH1} \cdot \left(\frac{1}{3} h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} \right) + P_{EH2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoilBelowEPS} \right) \cdots \\ &+ P_{EH3} \cdot \left(\frac{1}{3} \cdot h_{EPS} + h_{SoilBelowEPS} \right) + P_{EH4} \cdot \frac{1}{3} \cdot h_{SoilBelowEPS} \cdots \\ &+ P_{EH5} \cdot \frac{1}{2} \cdot h_{SoilBelowEPS} \\ &M_{EHWall} = 29.331 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Footing

The lateral earth load on the backwall, abutment wall, and footing are defined using 7 profiles. The forces acting on the abutment wall from profiles 1 to 5 remain unchanged. Hence, the calculation of forces from the earth load profiles 6 and 7 is described below.

EH 6:

Lateral earth pressure due to the vertical load at the footing top surface elevation

Lateral earth load due to the vertical load at the footing top surface elevation

EH 7:

Lateral earth pressure from the soil located along the depth of the footing

Lateral earth load from the soil located along the depth of the footing

Total lateral earth load

 $P_{\text{EHFooting}} := P_{\text{EHWall}} + P_{\text{EH6}} + P_{\text{EH7}} = 4.37 \cdot \frac{\text{kip}}{\text{ft}}$

 $p_{\text{SoilSideFt}} := k_a \cdot (\gamma_s \cdot t_{\text{footing}}) = 0.108 \cdot \text{ksf}$

 $P_{EH7} := \frac{1}{2} \cdot p_{SoilSideFt} \cdot t_{footing} = 0.162 \cdot \frac{kip}{ft}$

 $P_{EH6} := p_{SoilAboveFt} \cdot (t_{footing}) = 1.079 \cdot \frac{kip}{ft}$

 $p_{SoilAboveFt} := k_a \cdot \begin{pmatrix} \gamma_s \cdot h_{SoilAboveEPS} & \cdots \\ + \gamma_{EPS} \cdot h_{EPS} + \gamma_s \cdot h_{SoilBelowEPS} \end{pmatrix}$

Total moment of the lateral earth load at the base of the footing

$$\begin{split} M_{EHFooting} &\coloneqq P_{EH1} \cdot \left(\frac{1}{3}h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} + t_{footing}\right) \cdots \\ &+ P_{EH2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoilBelowEPS} + t_{footing}\right) + P_{EH3} \cdot \left(\frac{1}{3} \cdot h_{EPS} + h_{SoilBelowEPS} + t_{footing}\right) \cdots \\ &+ P_{EH4} \cdot \left(\frac{1}{3} \cdot h_{SoilBelowEPS} + t_{footing}\right) + P_{EH5} \cdot \left(\frac{1}{2} \cdot h_{SoilBelowEPS} + t_{footing}\right) \cdots \\ &+ P_{EH6} \cdot \frac{1}{2} \cdot \left(t_{footing}\right) + P_{EH7} \cdot \frac{1}{3} \cdot \left(t_{footing}\right) \\ &\qquad M_{EHFooting} = 40.499 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Vertical Earth Load on the Footing

Back side (heel)

 $EV_{earthBk} := \gamma_s \cdot l_{heel} \cdot (h_{SoilAboveEPS} + h_{SoilBelowEPS}) + \gamma_{EPS} \cdot l_{heel} \cdot h_{EPS}$ 1.1.

ft

$$EV_{earthBk} = 4.795 \cdot \frac{klp}{ft}$$

 $= 0.36 \cdot \text{ksf}$

Front side (toe)

$$EV_{earthFt} := \gamma_{s} \cdot l_{toe} \cdot \left(h_{toeDepth} - t_{footing}\right) = 3.04 \cdot \frac{kip}{ft}$$

LRFD 3.11.6.4

Live Load Surcharge

A surcharge is applied to account for a vehicular live load acting on the backfill surface within a distance equal to one-half the wall height behind the back face of the wall.

The lateral component of the live load surcharge on the abutment wall consists of three parts, as shown in the previous figure:

LS 1: the lateral pressure across the soil located above the EPS blocks

LS 2: the lateral pressure across the EPS blocks due to the soil located above the blocks

LS 3: the lateral pressure across the soil located below the EPS blocks.

Height of the abutment	$h_{backwall} + h_{wall} + t_{footing} = 24.79 fm$	t
Equivalent height of soil for vehicular load	$h_{eq} := 2ft$	LRFD Table 3.11.6.4-1
Lateral surcharge pressure	$\sigma_p := k_a \cdot \gamma_s \cdot h_{eq} = 0.072 \cdot ksf$	LRFD Eq. 3.11.6.4-1
Backwall		
Lateral load	$P_{LSBackwall} \coloneqq \sigma_p \cdot h_{backwall} = 0.306$	$5.\frac{\text{kip}}{\text{ft}}$
Abutment wall		
Lateral load from the profile LS1	$P_{LSWall1} := \sigma_p \cdot h_{SoilAboveEPS} = 0.5$	$561 \cdot \frac{\text{kip}}{\text{ft}}$
Lateral load from the profile LS2	$P_{LSWall2} := \frac{1}{10} \gamma_{s} \cdot h_{eq} \cdot h_{EPS} = 0.288 \cdot 10^{-1}$	kip ft NCHRP w65
Lateral load from the profile LS3	$P_{LSWall3} := \sigma_p \cdot h_{SoilBelowEPS} = 0.1$	$44 \cdot \frac{\text{kip}}{\text{ft}}$
Total lateral load due to live load surcharge	$P_{LSWall} := P_{LSWall1} + P_{LSWall2} + P_{LSWall2}$	$P_{LSWall3} = 0.993 \cdot \frac{kip}{ft}$
Total moment at the base of the wall due to the	lateral component of the live load surcharge	

$$\begin{split} M_{LSWall} &\coloneqq P_{LSWall1} \cdot \left(\frac{1}{2}h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS}\right) \cdots \\ &+ P_{LSWall2} \cdot \left(\frac{1}{2} \cdot h_{EPS} + h_{SoilBelowEPS}\right) + P_{LSWall3} \cdot \left(\frac{1}{2}h_{SoilBelowEPS}\right) \\ M_{LSWall} &= 12.485 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Footing

The lateral component of the live load surcharge on the footing consists of three parts. The contribution of LS 1 and LS 2 is the same as the abutment wall. The contribution of LS 3 needs to be considered up to the bottom of the footing.

Lateral surcharge load from the
profile LS 1
$$P_{LSFooting1} \coloneqq \sigma_p \cdot h_{SoilAboveEPS} = 0.561 \cdot \frac{kip}{ft}$$
Lateral surcharge load
from the profile LS 2 $P_{LSFooting2} \coloneqq \frac{1}{10} \gamma_s \cdot h_{eq} \cdot h_{EPS} = 0.288 \cdot \frac{kip}{ft}$ Lateral surcharge load from
the profile LS 3 $P_{LSFooting3} \coloneqq \sigma_p \cdot (h_{SoilBelowEPS} + t_{footing}) = 0.36 \cdot \frac{kip}{ft}$ Total lateral load due to live
load surcharge $P_{LSFooting1} \coloneqq P_{LSFooting1} + P_{LSFooting2} = 1.209 \cdot \frac{kip}{ft}$

Total moment at the base of the footing due to the lateral component of the live load surcharge

$$\begin{split} M_{\text{LSFooting}} &\coloneqq P_{\text{LSFooting1}} \cdot \left(\frac{1}{2}h_{\text{SoilAboveEPS}} + h_{\text{EPS}} + h_{\text{SoilBelowEPS}} + t_{\text{footing}}\right) \cdots \\ &\quad + P_{\text{LSFooting2}} \cdot \left(\frac{1}{2} \cdot h_{\text{EPS}} + h_{\text{SoilBelowEPS}} + t_{\text{footing}}\right) \cdots \\ &\quad + P_{\text{LSFooting3}} \cdot \frac{1}{2} \cdot \left(h_{\text{SoilBelowEPS}} + t_{\text{footing}}\right) \\ M_{\text{LSFooting}} &= 15.788 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}} \\ \text{Vertical load} \\ \end{split}$$

•

Step 3.5 Combined Load Effects

Description

This step presents the procedure for combining all load effects and calculating total factored forces and moments acting at the base of the abutment wall and footing. The total factored forces and moments at the base of the backwall are similar to those ones in Step 2.5.

▶

Page Contents

102 Forces and Moments at the Base of the Abutment Wall

106 Forces and Moments at the Base of the Footing

Forces and Moments at the Base of the Abutment Wall

Load Cases I, III, and IV are considered. More specifically, superstructure dead load, superstructure live load, and uniform temperature induced loads are considered in addition to the dead load of the backwall, dead load of the abutment wall, lateral earth pressure, and lateral surcharge pressure.



Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75 LS + 0.5TU

Load Case I

Factored vertical force at the base of
the wall
$$F_{VWallLC1StrI} := 1.25 \cdot (DC_{backwall} + DC_{wall}) = 11.61 \cdot \frac{kip}{ft}$$
Factored shear force parallel to the
transverse axis of the abutment wall $V_{uWallLC1StrI} := 1.5 \cdot P_{EHWall} = 4.693 \cdot \frac{kip}{ft}$ The backwall weight reduces the critical moment at the base of the abutment wall. ThisLRFD 3.4.1

The backwall weight reduces the critical moment at the base of the abutment wall. This requires the use of a minimum load factor of 0.9 for DC instead of the factor 1.25 in the Strength I combination.

This is the same for the moment calculated about the longitudinal axis of the abutment wall for all the load cases and limit states.

Factored moment about the longitudinal axis of the abutment wall

$$M_{uWallLC1StrI} := 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + 1.5 \cdot M_{EHWall} = 43.28 \cdot \frac{kip \cdot ft}{ft}$$

Load Case III

Factored vertical force at the base of the wall

$$F_{VWallLC3StrI} \coloneqq 1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall}\right) + 1.5DW_{Sup} + 1.75R_{LLWallMax}$$

$$F_{VWallLC3StrI} = 29.861 \cdot \frac{kip}{ft}$$
Factored shear force parallel to the transverse axis of the abutment wall
$$V_{uWallLC3StrI} \coloneqq 1.5 \cdot P_{EHWall} = 4.693 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC3StrI} &\coloneqq 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLWallMax}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ 1.5 \cdot M_{EHWall} \\ M_{uWallLC3StrI} &= 56.969 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force at the base of the wall

$$F_{VWallLC4StrI} \coloneqq 1.25 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} \right) + 1.5 DW_{Sup} = 20.012 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall

$$V_{uWallLC4StrI} := 1.5 \cdot P_{EHWall} + 1.75 \cdot P_{LSWall} + 0.5TU = 6.57 \cdot \frac{k_{IP}}{ft}$$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} \mathbf{M}_{uWallLC4StrI} &\coloneqq 0.9 \cdot \mathrm{DC}_{backwall} \cdot \frac{\left(\mathbf{t}_{backwall} - \mathbf{t}_{wall}\right)}{2} + \left(1.25 \cdot \mathrm{DC}_{Sup} + 1.5 \cdot \mathrm{DW}_{Sup}\right) \cdot \left(\mathbf{l}_{brtowall} - \frac{\mathbf{t}_{wall}}{2}\right) \dots \\ &+ 1.5 \cdot \mathrm{M}_{EHWall} + 1.75 \cdot \mathrm{M}_{LSWall} + 0.5 \cdot \mathrm{TU} \cdot \mathbf{h}_{wall} \end{split}$$

$$M_{uWallLC4StrI} = 73.864 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Load Case I

Factored vertical force at the base of the wall	$F_{VWallLC1SerI} := DC_{backwall} + DC_{wall} = 9.288 \cdot \frac{kip}{ft}$
Factored shear force parallel to the transverse axis of the abutment wall	$V_{uWallLC1SerI} := P_{EHWall} = 3.129 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the abutment wall

$$M_{uWallLC1SerI} \coloneqq DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + M_{EHWall}$$
$$M_{uWallLC1SerI} = 28.535 \cdot \frac{kip \cdot ft}{ft}$$

Load Case III

Factored vertical force at the base of the wall

$$F_{VWallLC3SerI} := (DC_{Sup} + DC_{backwall} + DC_{wall}) + DW_{Sup} + R_{LLWallMax}$$
$$F_{VWallLC3SerI} = 21.46 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall

$$V_{uWallLC3SerI} := P_{EHWall} = 3.129 \cdot \frac{kip}{ff}$$

1

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC3SerI} &\coloneqq DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} \dots \\ &+ \left(DC_{Sup} + DW_{Sup} + R_{LLWallMax}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ M_{EHWall} \end{split}$$

$$M_{uWallLC3SerI} = 37.664 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Load Case IV

Factored vertical force at the base of the wall

$$F_{VWallLC4SerI} := (DC_{Sup} + DC_{backwall} + DC_{wall}) + 1.0DW_{Sup}$$
$$F_{VWallLC4SerI} = 15.832 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the abutment wall

$$V_{uWallLC4SerI} := P_{EHWall} + P_{LSWall} + TU = 4.399$$

Factored moment about the longitudinal axis of the abutment wall

$$\begin{split} M_{uWallLC4SerI} &\coloneqq DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + \left(1.0 \cdot DC_{Sup} + 1.0 \cdot DW_{Sup}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ 1.0 \cdot M_{EHWall} + 1.0 \cdot M_{LSWall} + 1.0 \cdot TU \cdot h_{wall} \\ M_{uWallLC4SerI} &= 50.795 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

kip

ft

Summary of the Forces and Moments at the Base of the Abutment Wall

Factored vertical force, F_{VWall} (kip/ft)

	Strength I	Service I
LC I	11.61	9.29
LC III	29.86	21.46
LC IV	20.01	15.83

Factored shear force parallel to the transverse axis of the
abutment wall, V _{uWall} (kip/ft)

	Strength I	Service I
LC I	4.69	3.13
LC III	4.69	3.13
LC IV	6.57	4.40

Factored moment about the longitudinal axis of the abutment wall, MuWall (kip ft/ft)

	Strength I	Service I
LC I	43.28	28.53
LC III	56.97	37.66
LC IV	73.86	50.80

The forces and moments presented in the above tables are used for the structural design presented in Step 3.8. As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the abutment wall after excluding the lateral earth load within the EPS backfill zone. This summary is presented for informational purposes only.

Factored vertical force, F_{VWall} (kip/ft)

	Strength I	Service I
LC I	11.61	9.29
LC III	29.86	21.46
LC IV	20.01	15.83

Factored shear force parallel to the transverse axis of the abutment wall, $V_{u\mbox{Wall}}\ (\mbox{kip/ft})$

	Strength I	Service I
LC I	4.29	2.86
LC III	4.29	2.86
LC IV	6.31	4.41

Factored moment about the longitudinal axis of the abutment wall, MuWall (kip ft/ft)

	Strength I	Service I
LC I	40.87	26.93
LC III	54.56	36.06
LC IV	73.89	54.06

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered. In addition to all the loads considered for the abutment wall, weight of soil (earth load) on the footing toe and heel along with live load surcharge on the heel are considered.

LRFD 3.6.2.1

The dynamic load allowance is excluded from the live load for foundation components located entirely below ground level.



Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU

Load Case I

Factored vertical force at the base of the footing

$$F_{VFtLC1StrI} \coloneqq 1.25 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 29.781 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC1StrI} := 1.5 \cdot P_{EHFooting} = 6.555 \cdot \frac{kip}{ft}$$

The vertical earth load of the backfill soil reduces the critical moment about the footing longitudinal axis. This requires the use of a minimum load factor of 1.0 for EV instead of the factor 1.35 in the Strength I combination.

LRFD 3.4.1

The same is applied for the moment calculated about the footing's longitudinal axis for all the load cases and limit states.

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC1StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot M_{EHFooting} + 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC1StrI} = 38.136 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case III

Factored vertical force at the base of the footing

 $F_{VFtLC3StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) + 1.5DW_{Sup} + 1.75R_{LLFootingMax} + 1.35 \cdot (EV_{earthBk} + EV_{earthFt})$

 $V_{uFtLC3StrI} := 1.5 \cdot P_{EHFooting} = 6.555 \cdot \frac{kip}{ft}$

$$F_{VFtLC3StrI} = 47.733 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot M_{EHFooting} + 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3StrI} = 30.656 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force at the base of the footing

$$F_{VFtLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) + 1.5DW_{Sup} \dots + 1.35 \cdot (EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFooting}$$

$$F_{VFtLC4StrI} = 39.863 \cdot \frac{Kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

 $V_{uFtLC4StrI} \coloneqq 1.5 \cdot P_{EHFooting} + 1.75 \cdot P_{LSFooting} + 0.5TU = 8.809 \cdot \frac{kip}{ft}$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC4StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot M_{EHFooting} + 1.75M_{LSFooting} + 1.75V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ 0.5 \cdot TU \cdot \left(h_{wall} + t_{footing} \right) \end{split}$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Load Case I

Factored vertical force at the base of the footing

$$F_{VFtLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 23.198 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC1SerI} := P_{EHFooting} = 4.37 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC1SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall'} \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \\ &+ M_{EHFooting} + EV_{earthBk'} \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt'} \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC1SerI} = 16.982 \cdot \frac{kip \cdot ft}{ft} \end{split}$$
Load Case III

Factored vertical force at the base of the footing

$$F_{VFtLC3SerI} \coloneqq DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFootingMax} + (EV_{earthFt} + EV_{earthBk})$$

$$F_{VFtLC3SerI} = 35.199 \cdot \frac{kip}{ft}$$
shear force parallel to the
$$V_{uFtLC3SerI} \coloneqq P_{EHFooting} = 4.37 \cdot \frac{kip}{\rho}$$

Factored shear force parallel to the transverse axis of the footing

he
$$V_{uFtLC3SerI} := P_{EHFooting} = 4$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} + R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ M_{EHFooting} + EV_{earthBk'} \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3SerI} = 11.982 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force at the
base of the footing
$$F_{VFtLC4SerI} \coloneqq DC_{Sup} + DC_{backwall} + DC_{footing} + DW_{Sup} \dots + (EV_{earthFt} + EV_{earthBk}) + V_{LSFooting}$$
$$F_{VFtLC4SerI} = 30.702 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC4SerI} := P_{EHFooting} + P_{LSFooting} + TU = 5.856 \cdot \frac{kip}{ft}$$

ft

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC4SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) + M_{EHFooting} \dots \\ &+ EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + M_{LSFooting} + TU \cdot \left(h_{wall} + t_{footing} \right) \\ &M_{uFtLC4SerI} = 31.183 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Summary of Forces and Moments at the Base of the Footing

Factored vertical force, F_{VFt} (kip/ft)

	Strength I	Service I
LC I	29.78	23.20
LC III	47.73	35.20
LC IV	39.86	30.70

Factored shear force parallel to the transverse axis of the footing, V_{uFt} (kip/ft)

	Strength I	Service I
LC I	6.55	4.37
LC III	III 6.55 ²	
LC IV	8.81	5.86

Factored moment about the longitudinal axis of the footing, MuFt (kip ft/ft)

	Strength I	Service I
LC I	38.14	16.98
LC III	30.66	11.98
LC IV	57.13	31.18

The forces and moments presented in the tables above are used for the designs presented in Step 3.6. and 3.9. As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the abutment wall after excluding the lateral earth load within the EPS backfill zone. This summary is presented for informational purposes only.

Factored vertical force, F_{VFt} (kip/ft)

	Strength I Service I	
LC I	29.78	23.20
LC III	СШ 47.73 35.2	
LC IV	39.86	30.70

Factored shear force parallel to the transverse axis of the footing, $V_{u\text{Ft}}\xspace$ (kip/ft)

	Strength I Service I	
LC I	6.15 4.10	
LC III	6.15	4.10
LC IV	8.55	5.87

Factored moment about the longitudinal axis of the footing, $M_{uFt} \left(\text{kip} \cdot ft/ft \right)$

	Strength I	Service I
LC I	34.52	14.57
LC III	СШ 27.04 9.5	
LC IV	56.37	34.47

+

Step 3.6 Geotechnical Design of the Footing

Description

This step presents the geotechnical design of a spread footing considering the following strength and serviceability limit states:

LRFD 10.6.1.1

- 1. bearing resistance strength limit states:
- 2. settlement service limit state
- 3. sliding resistance strength limit state
- 4. load eccentricity (overturning) strength limit state.

The evaluation of structural resistance of the footing (internal stability) is presented later in Step 3.9.

Page Contents

- 112 Summary of Forces and Moments at the Base of the Footing
- **112 Bearing Resistance Check**
- 116 Settlement Check
- 116 Sliding Resistance Check
- 118 Eccentric Load Limitation (Overturning) Check

Summary of Forces and Moments at the Base of the Footing

As per the MDOT practice reflected in BDS, the lateral earth load within the EPS backfill zone is excluded. The following tables present the forces and moments at the base of the footing after including the lateral earth load within the EPS backfill zone. The forces and moments presented in these tables are used for the designs presented in Step 3.6. and 3.9.

	Strength I	Service I
LC I	29.78	23.20
LC III	47.73	35.20
LC IV	39.86	30.70

Factored vertical force, F_{VFt} (kip/ft)

Factored shear force parallel to the transverse axis of the footing, V_{uFt} (kip/ft)

	Strength I	Service I
LC I	6.55	4.37
LC III	6.55	4.37
LC IV	8.81	5.86

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/ft)

	Strength I Service	
LC I	38.14	16.98
LC III	сш 30.66 11.9	
LC IV	57.13	31.18

Bearing Resistance Check

For eccentrically loaded footings, the use of a reduced effective area is allowed for bearing resistance or settlement calculation. The point of load application shall be at the centroid of the reduced area.

Note: As a practice, the average pressure and the values at the toe and heel under different load cases and limit states are provided to the MDOT Geotechnical Services Section for verification.

This example presents the LRFD and MDOT methods.

Load Case I, Strength I

Factored vertical force	$F_{VFtLC1StrI} = 29.781 \cdot \frac{k_{IP}}{ft}$
Factored moment about footing longitudinal axis	$M_{uFtLC1StrI} = 38.136 \cdot \frac{kip \cdot ft}{ft}$
Eccentricity in the footing width direction	$e_{\rm B} \coloneqq \frac{M_{\rm u} FtLC1StrI}{F_{\rm V} FtLC1StrI} = 1.281 {\rm ft}$

LRFD method

A reduced effective footing width is used for bearing resistance and settlement design.

LRFD 10.6.1.3

LRFD 10.6.1.3

$ng - 2 \cdot e_B = 10.939 \text{ft}$	LRFD Eq. 10.6.1.3-1
ľ	$h_{ing} - 2 \cdot e_{B} = 10.939 \text{ft}$

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case III, Strength I

Factored vertical force

Factored moment about footing longitudinal axis

Eccentricity in the footing width direction

LRFD method

Effective footing width

Bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case IV, Strength I

Factored vertical force

Factored moment about footing longitudinal axis

Eccentricity in the footing width direction

$$q_{\text{bearing}_LC1} \coloneqq \frac{F_{\text{VFtLC1StrI}}}{B_{\text{eff}}} = 2.722 \cdot \text{ksf}$$

$$q_{avgLC1} := \frac{F_{VFtLC1StrI}}{B_{footing}} = 2.206 \cdot ksf$$

$$q_{toeLC1} := \frac{F_{VFtLC1StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.461 \cdot ksf$$

$$q_{heelLC1} := \frac{F_{VFtLC1StrI}}{P_{FtLC1StrI}} \cdot \left(1 - \frac{6 \cdot e_B}{P_{FtLC1StrI}}\right) = 0.95 \cdot ksf$$

heelLC1 :=
$$\frac{1 \text{ VFtLC1Strl}}{\text{B}_{\text{footing}}} \cdot \left(1 - \frac{0.0\text{B}}{\text{B}_{\text{footing}}}\right) = 0.95 \cdot \text{ksf}$$

$$F_{VFtLC3StrI} = 47.733 \cdot \frac{kip}{ft}$$

$$M_{uFtLC3StrI} = 30.656 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC3StrI}}{F_{VFtLC3StrI}} = 0.642 \text{ ft}$$

 $B_{eff} := B_{footing} - 2 \cdot e_B = 12.216 \text{ ft}$ LRFD Eq. 10.6.1.3-1 $\frac{F_{VFtLC3StrI}}{B_{eff}} = 3.908 \cdot ksf$ q_{bearing_LC3} :=

$$q_{avgLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} = 3.536 \cdot ksf$$

$$q_{toeLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 4.545 \cdot ksf$$

$$q_{heelLC3} \coloneqq \frac{F_{VFtLC3StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 2.527 \cdot ksf$$

$$F_{VFtLC4StrI} = 39.863 \cdot \frac{kip}{ft}$$

$$M_{uFtLC4StrI} = 57.133 \cdot \frac{k_{1}p \cdot ft}{ft}$$

$$e_{\rm B} := \frac{M_{\rm uFtLC4StrI}}{F_{\rm VFtLC4StrI}} = 1.433 \, {\rm ft}$$

LRFD method

Effective footing width

Bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case I, Service I

Factored vertical force

Factored moment about footing longitudinal axis

Eccentricity in the footing width direction

LRFD method

Effective footing width

Footing bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case III, Service I

Factored vertical force

Factored moment about footing longitudinal axis

Eccentricity in the footing width direction

 $B_{eff} \coloneqq B_{footing} - 2 \cdot e_{B} = 10.634 \text{ ft} \qquad LRFD Eq. 10.6.1.3-1$ $q_{bearing_LC4} \coloneqq \frac{F_{VFtLC4StrI}}{B_{eff}} = 3.749 \cdot \text{ksf}$

$$q_{avgLC4} := \frac{F_{VFtLC4StrI}}{B_{footing}} = 2.953 \cdot ksf$$

$$q_{\text{toeLC4}} \coloneqq \frac{\text{FvFtLC4StrI}}{\text{B}_{\text{footing}}} \cdot \left(1 + \frac{6 \cdot \text{e}_{\text{B}}}{\text{B}_{\text{footing}}}\right) = 4.834 \cdot \text{ksf}$$
$$q_{\text{heelLC4}} \coloneqq \frac{\text{FvFtLC4StrI}}{\text{B}_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot \text{e}_{\text{B}}}{\text{B}_{\text{footing}}}\right) = 1.072 \cdot \text{ksf}$$

$$F_{VFtLC1SerI} = 23.198 \cdot \frac{kip}{ft}$$

$$M_{uFtLC1SerI} = 16.982 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC1SerI}}{F_{VFtLC1SerI}} = 0.732 \text{ ft}$$

 $B_{eff} := B_{footing} - 2 \cdot e_{B} = 12.036 \text{ ft} \qquad \text{LRFD Eq. 10.6.1.3-1}$ $q_{bearing_LC1SerI} := \frac{F_{VFtLC1SerI}}{B_{eff}} = 1.927 \cdot \text{ksf}$

$$q_{avgLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} = 1.718 \cdot ksf$$

$$q_{toeLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 2.277 \cdot ksf$$

$$q_{heelLC1SerI} \coloneqq \frac{F_{VFtLC1SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.159 \cdot ksf$$

$$F_{VFtLC3SerI} = 35.199 \cdot \frac{kip}{ft}$$
$$M_{uFtLC3SerI} = 11.982 \cdot \frac{kip \cdot ft}{ft}$$
$$e_{B} := \frac{M_{uFtLC3SerI}}{F_{VFtLC3SerI}} = 0.34 \text{ ft}$$

LRFD method

Effective footing width

Bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

Load Case IV, Service I

Factored vertical force

Factored moment about footing longitudinal axis

Eccentricity in the footing width direction

LRFD method

Effective footing width

Bearing pressure

MDOT method

Average bearing pressure

Toe bearing pressure

Heel bearing pressure

$$B_{eff} := B_{footing} - 2 \cdot e_{B} = 12.819 \text{ ft} \qquad LRFD Eq. 10.6.1.3-1$$
$$q_{bearing_LC3SerI} := \frac{F_{VFtLC3SerI}}{B_{eff}} = 2.746 \cdot \text{ksf}$$

$$q_{avgLC3SerI} \coloneqq \frac{F_{VFtLC3SerI}}{B_{footing}} = 2.607 \cdot ksf$$
$$q_{toeLC3SerI} \coloneqq \frac{F_{VFtLC3SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.002 \cdot ksf$$

$$q_{\text{heelLC3SerI}} := \frac{F_{\text{VFtLC3SerI}}}{B_{\text{footing}}} \cdot \left(1 - \frac{6 \cdot e_{\text{B}}}{B_{\text{footing}}}\right) = 2.213 \cdot \text{ksf}$$

$$F_{VFtLC4SerI} = 30.702 \cdot \frac{k_{IP}}{ft}$$

$$M_{uFtLC4SerI} = 31.183 \cdot \frac{k_{IP} \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC4SerI}}{F_{VFtLC4SerI}} = 1.016 \text{ ft}$$

$$B_{eff} := B_{footing} - 2 \cdot e_B = 11.469 \text{ ft}$$
 LRFD Eq. 10.6.1.3-1

$$q_{\text{bearing}_LC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{eff}} = 2.677 \cdot \text{ksf}$$

$$q_{avgLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} = 2.274 \cdot ksf$$

$$q_{toeLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.301 \cdot ksf$$

$$q_{heelLC4SerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 1.248 \cdot ksf$$

Summary

LRFD method

The controlling bearing pressure under strength limit states

 $q_b := \max(q_{bearing LC1}, q_{bearing LC3}, q_{bearing LC4}) = 3.908 \cdot ksf$

The controlling bearing pressure needs to be checked with the factored bearing resistance of the soil provided by the Geotechnical Services Section.

MDOT method

A summary of bearing pressure values (in psf) is shown in the following table:

	Toe	Avg	Heel	Toe	Avg	Heel
	(Service I)	(Serivce I)	(Service I)	(Strength I)	(Strength I)	(Strength I)
LC I	2277	1718	1159	3461	2206	950
LC III	3002	2607	2213	4545	3536	2527
LC IV	3301	2274	1248	4834	2953	1072

The Geotechnical Services Section uses these values for the verification of bearing resistance and settlement limits. If the bearing pressure exceeds the bearing strength of the soil, the size of the footing needs to be increased. See BDM 7.03.02.G for more information.

Settlement Check

The Geotechnical Services Section uses the controlling bearing pressure from the service limit state to check if the total settlement of foundation is less than 1.5 in., the allowable limit.

BDM 7.03.02G 2b

For LRFD method, the controlling bearing pressure for settlement analysis is

 q_b settlement := max($q_{bearing LC1SerI}, q_{bearing LC3SerI}, q_{bearing LC4SerI}) = 2.746 \cdot ksf$

The Geotechnical Services Section uses this controlling bearing pressure to calculate the foundation's total settlement.

For the MDOT method, the bearing pressures under service limit state are provided to the Geotechnical Services Section to calculate the settlement.

Note: Besides the total settlement, considerations should be given to prevent the differential settlement between the abutments and pier from exceeding the tolerable differential settlement limit. Differential settlement limits are given in the *Steel Plate Girder Design Example*.

Sliding Resistance Check

Spread footings must be designed to resist lateral loads without sliding. The sliding resistance of a footing on cohesionless soil is a function of the normal force and the interface friction between the foundation and the soil.

The Geotechnical Services Section should provide a coefficient of sliding resistance (μ) for a design. MDOT typically uses a sliding resistance coefficient of 0.5 for cast-in-place concrete footings. Consult the Geotechnical Services Section to identify the most suitable coefficient for a specific design.

Coefficient of sliding resistance



LRFD 10.6.3.4

The strength limit states are used for this check. Since the resistance is proportional to the vertical loads, the following conditions are used:

- Minimum load factors are used for all vertical loads.
- Maximum load factors are used for the loads that contribute to horizontal sliding forces.
- Since DW is the future wearing surface load, it is excluded from all load combinations.

Load Case I

Factored shear force parallel to the transverse axis of the footing

Factored sliding force

Minimum vertical load

$$F_{VFtLC1StrIMin} := 0.9 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 21.662 \cdot \frac{kip}{ft}$$

 $\phi_{\tau} \coloneqq 0.8$

 $V_{uFtLC1StrI} = 6.555 \cdot \frac{kip}{\alpha}$

 $V_{\text{sliding}} \coloneqq V_{\text{uFtLC1StrI}} = 6.555 \cdot \frac{\text{kip}}{\text{ft}}$

 $V_{\text{resistance}} := \phi_{\tau} \cdot \mu \cdot F_{\text{VFtLC1StrIMin}} = 8.665 \cdot \frac{\text{kip}}{\Phi}$

Check := if (V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"

Resistance factor for sliding

Sliding resistance

Check if V_{resistance} > V_{sliding}

Load Case III

Factored shear force parallel to the transverse axis of the footing

Factored sliding force

When calculating the minimum vertical force for sliding and eccentric load limitation checks, the live load on the superstructure is excluded to develop a conservative design.

 $V_{uFtLC3StrI} = 6.555 \cdot \frac{kip}{ft}$

 $V_{sliding} := V_{uFtLC3StrI} = 6.555 \cdot \frac{kip}{ft}$

$$F_{VFtLC3StrIMin_noLL} = 26.754 \cdot \frac{kip}{ft}$$

$$V_{resistance} := \phi_{\tau} \cdot \mu \cdot F_{VFtLC3StrIMin_noLL} = 10.702 \cdot \frac{kip}{ft}$$

$$Check := if(V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"$$

BDM 7.03.02.F, LRFD Table 10.5.5.5.2-1

Load Case IV

Sliding resistance

Two cases need to be considered: without and with the live load surcharge.

Without live load surcharge:

Check if V_{resistance} > V_{sliding}

Factored shear force parallel to the transverse axis of the footing

Factored sliding force without the live load surcharge

$$V_{uFtLC4StrI} = 8.809 \cdot \frac{kip}{ft}$$
$$V_{sliding} \coloneqq V_{uFtLC4StrI} - 1.75P_{LSFooting} = 6.693 \cdot \frac{kip}{ft}$$

Minimum vertical load without the live load surcharge

$$\begin{split} F_{VFtLC4StrIMin_noLS} &\coloneqq 0.9 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} \right) ... \\ &+ 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) \\ F_{VFtLC4StrIMin_noLS} &= 26.754 \cdot \frac{kip}{ft} \\ V_{resistance} &\coloneqq \varphi_{\tau} \cdot \mu \cdot F_{VFtLC4StrIMin_noLS} = 10.702 \cdot \frac{kip}{ft} \\ Check &\coloneqq if \left(V_{resistance} > V_{sliding}, "OK", "Not OK" \right) = "OK" \end{split}$$

With live load surcharge:

Check if $V_{resistance} > V_{sliding}$

Sliding resistance

Factored shear force parallel to the transverse axis of the footing

Factored sliding force

Minimum vertical load with the live load surcharge

 $V_{uFtLC4StrI} = 8.809 \cdot \frac{kip}{ft}$ $V_{sliding} \coloneqq V_{uFtLC4StrI} = 8.809 \cdot \frac{kip}{ft}$

 $F_{VFtLC4StrIMin} \coloneqq 0.9 \cdot \left(DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} \right) \dots + 1.0 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) + 1.75 V_{LSFooting}$

 $V_{\text{resistance}} := \phi_{\tau} \cdot \mu \cdot F_{\text{VFtLC4StrIMin}} = 11.374 \cdot \frac{\text{kip}}{\text{ft}}$

Check := if (V_{resistance} > V_{sliding}, "OK", "Not OK") = "OK"

 $F_{VFtLC4StrIMin} = 28.434 \cdot \frac{kip}{ft}$

Sliding resistance

Check if V_{resistance} > V_{sliding}

Eccentric Load Limitation (Overturning) Check

The eccentricity of loading at the strength limit state, evaluated based on factored loads, shall not exceed one-sixth of the corresponding dimension measured from the centerline of the footing for stability.

The eccentricity in the abutment length direction is not a concern. The following calculations present the evaluation of the eccentricity in the abutment width direction for the Strength I limit state:

Load Case I

Luau Case I	kip
Minimum vertical load	$F_{VFtLC1StrIMin} = 21.662 \cdot \frac{1}{ft}$
Maximum moment about the longitudinal axis of the footing	$M_{uFtLC1StrI} = 38.136 \cdot \frac{kip \cdot ft}{ft}$
Eccentricity in the footing width direction measured from the centerline	$e_{\rm B} := \frac{M_{\rm u} FtLC1StrI}{F_{\rm V} FtLC1StrIMin} = 1.761 {\rm ft}$
1/6 of footing width	$\frac{B_{\text{footing}}}{6} = 2.25 \text{ft}$
Check if the eccentric load limitation is satisfied	Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK" \right) = "OK"$

Load Case III

Two cases need to be considered: without and with live load.

Without live load:

Minimum vertical force without the live load

Moment about the longitudinal axis of the footing (with live load)

$$F_{VFtLC3StrIMin_noLL} = 26.754 \cdot \frac{kip}{ft}$$
$$M_{uFtLC3StrI} = 30.656 \cdot \frac{kip \cdot ft}{ft}$$

 $e_{\rm B} := \frac{M_{\rm uFtLC3StrI_noLL}}{F_{\rm VFtLC3StrIMin_noLL}} = 1.295 \, {\rm ft}$

Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK" \right) = "OK"$

Moment about the longitudinal axis of the footing (without the live load)

$$M_{uFtLC3StrI_noLL} := M_{uFtLC3StrI} - \left(1.75 \cdot R_{LLFootingMax}\right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2}\right) = 34.635 \cdot \frac{kip \cdot ft}{ft}$$

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

With live load:

Minimum vertical force with the live load

Moment about the longitudinal axis of the footing (with the live load)

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

Load Case IV

Two cases need to be considered: without and with live load surcharge.

Without live load surcharge:

Minimum vertical force without the live load surcharge

Moment about the longitudinal axis of the footing (with the live load surcharge)

$$F_{VFtLC4StrIMin_noLS} = 26.754 \cdot \frac{kip}{ft}$$

$$M_{uFtLC4StrI} = 57.133 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Moment about the longitudinal axis of the footing (without the live load surcharge)

$$\begin{split} M_{uFtLC4StrI_noLS} &\coloneqq M_{uFtLC4StrI} - 1.75 V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \\ &+ (-1.75) \cdot P_{LSFooting} \cdot \frac{\left(h_{backwall} + h_{wall} + t_{footing} \right)}{2} \\ & M_{uFtLC4StrI_noLS} = 38.891 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

= "OK'

$$F_{VFtLC3StrIMin} = 36.304 \cdot \frac{kip}{ft}$$

$$M_{uFtLC3StrI} = 30.656 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC3StrI}}{F_{VFtLC3StrIMin}} = 0.844 \text{ ft}$$
Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not Check \right)$

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

With live load surcharge:

Minimum vertical force with the live load surcharge

Moment about the longitudinal axis of the footing

Eccentricity in the footing width direction measured from the centerline

Check if the eccentric load limitation is satisfied

$$e_{B} := \frac{M_{u}FtLC4StrI_noLS}{F_{v}FtLC4StrIMin_noLS} = 1.454 \text{ ft}$$

Check := if $\left(e_{B} < \frac{B_{footing}}{6}, "OK", "Not OK"\right) = "OK"$

$$F_{VFtLC4StrIMin} = 28.434 \cdot \frac{kip}{ft}$$

$$M_{uFtLC4StrI} = 57.133 \cdot \frac{kip \cdot ft}{ft}$$

$$e_{B} := \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrIMin}} = 2.009 \text{ ft}$$

$$F_{VFtLC4StrIMin} = 0.009 \text{ ft}$$

Check := if $\left(e_{\mathbf{B}} < \frac{B_{\text{footing}}}{6}, "OK", "Not OK" \right) = 1$	"OK"
--	------

Step 3.7 Backwall Design

Description

Please refer to the design calculations and details presented in Step 2.7. The backwall forces and moments used in Step 2.7. are not impacted by the use of EPS blocks as the backfill material since EPS blocks are located below the backwall.

Step 3.8 Abutment Wall Design

Description

This step presents the design of the abutment wall.

PageContents123Forces and Moments at the Base of the Abutment Wall

- **123** Design for Flexure
- 126 Design for Shear
- 128 Development Length of Reinforcement
- 129 Shrinkage and Temperature Reinforcement

Forces and Moments at the Base of the Abutment Wall

Step 3.5 presents the load effects at the base of the abutment wall under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, F_{VWall} (kip/ft)

	Strength I	Service I
LC I	11.61	9.29
LC III	29.86	21.46
LC IV	20.01	15.83

Factored shear force parallel to the transverse axis of
the abutment wall, V _{uWall} (kip/ft)

	Strength I	Service I
LC I	4.69	3.13
LC III	4.69	3.13
LC IV	6.57	4.40

Factored moment about the longitudinal axis of the abutment wall, M_{uWall} (kip ft/ft)

	Strength I	Service I
LC I	43.28	28.53
LC III	56.97	37.66
LC IV	73.86	50.80

Design for Flexure

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the flexural design.

Moment demand at the base of the wall

$$M_{\text{DemandWall}} := M_{\text{uWallLC4StrI}} = 73.864 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

LRFD 5.6.3.2

Flexure Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 8	
Nominal diameter of a reinforcing steel bar	$d_{\text{bar}} := \text{Dia}(\text{bar}) = 1 \cdot \text{in}$	
Cross-section area of the bar	$A_{bar} := Area(bar) = 0.79 \cdot in^2$	
The spacing of the main reinforcing steel bars in v lesser of 1.5 times the thickness of the member or	valls and slabs shall not be greater than the 18 in.	LRFD 5.10.3.2
The spacing of shrinkage and temperature reinfor wall thickness is greater than 18 in.	cement shall not exceed 12 in. when the	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a ma	aximum of 18 in.	BDG 5.22.01
Wall thickness	$t_{wall} = 38 \cdot in$	
Select a spacing for reinforcing steel bars	$s_{bar} := 12 \cdot in$	
Select a 1-ft wide strip for the design.		

har - 8

Effective deph
$$d_e := t_{wall} - \operatorname{Cover}_{wall} = 35 \cdot in$$
Resistance factor for flexure $\phi_f := 0.9$ LRFD 5.5.4.2Width of the compression face of
the member $b := 12in$ Stress block factor $\beta_1 := \min \left[\max \left[0.85 - 0.05 \cdot \left(\frac{f_e}{e} - 4ksi \right) , 0.65 \right], 0.85 \right] = 0.85$ LRFD
5.6.2.2Solve the following equation of A, to calculate the required area of steel to satisfy the moment demand. Use an
assumed initial A, value to solve the equation.Initial assumptionA_s := 1in^2Initial assumptionA_s := 1in^2Given
M_DemandWall' ft = $\phi_f \cdot A_{s'} f_{y'} \left[d_e - \frac{1}{2} \cdot \left(\frac{A_s' f_y'}{0.85 \cdot f_e' \cdot b} \right) \right]$ LRFD
5.6.3.2Required area of steelA_sRequired := Find(A_s) = 0.475 \cdot in^2LRFD
5.6.3.2Check if A_showided > A_stequiredCheck := if (A_sProvided > A_sRequired ...OK", "Not OK") = "OK"Moment capacity of the section
with the provided steel areaMCapacityWall := $\phi_f \cdot A_s Provided' fy$ Distance from the extreme
compression fiber to the neutral axis $c := \frac{A_s Provided' f_y}{0.85 \cdot f_e' \beta_1 \cdot b} = 1.82 \cdot in$ Check the validity of assumption $f_s = f_y$ Check := if $\left(\frac{e}{e} < 0.6$, "OK", "Not OK" $\right) = "OK"$ Limits for Reinforcement
provided must develop a factored flexural resistance equal to the lesser of the cracking
moment or 1.33 times the factored moment from the applicable steringh limit state load combinations.Flexual cracking variability factor $\gamma_1 := 1.6$ For concrete structures that are not precast segmental

 $\gamma_3 \coloneqq 0.67$

 $A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.79 \cdot in^2$

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Area of reinforcing steel provided in a

1-ft wide section

For ASTM A615 Grade 60 reinforcement

124

Section modulus
$$S_c := \frac{1}{6} \cdot b \cdot t_{wall}^2 = 2.888 \times 10^3 \cdot in^3$$
Cracking moment $M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 107.246 \cdot \frac{kip \cdot ft}{ft}$ 1.33 times the factored moment demand $1.33 \cdot M_{DemandWall} = 98.239 \cdot \frac{kip \cdot ft}{ft}$ Required moment to satisfy the
minimum reinforcement requirement $M_{req} := min(1.33M_{DemandWall}, M_{cr}) = 98.239 \cdot \frac{kip \cdot ft}{ft}$ Check the adequacy of the section capacityCheck := if(M_{CapacityWall} > M_{req}, "OK", "Not OK") = "OK"

 $s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$

 $\gamma_e := 1.00$

Control of Cracking by Distribution of Reinforcement

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirements for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The position of the cross-section's neutral axis is determined ual stress in the reinforcement. This process starts with an ass hown below.

Assumed distance from the extreme compression fiber to the neutral axis

Given

Position of the neutral axis

Tensile force in the reinforcing steel due to service limit state moment

Stress in the reinforcing steel due to service limit state moment

 f_{ss} (not to exceed 0.6 f_{v})

$$d_c := \text{Cover}_{\text{wall}} = 3 \cdot \text{in}$$

 $\beta_s := 1 + \frac{d_c}{0.7(t_{\text{wall}} - d_c)} = 1.122$
ned through an iterative process to calculate the act

2 :...

LRFD 5.6.7

LRFD Eq. 5.6.7-1

$$0.7(t_{wall} - u_c)$$

ned through an iterative process to cal
sumed position of the neutral axis as s

$$\frac{1}{2} \cdot \mathbf{b} \cdot \mathbf{x}^2 = \frac{\mathbf{E}_s}{\mathbf{E}_c} \cdot \mathbf{A}_{s \text{Provided}} \cdot (\mathbf{d}_e - \mathbf{x})$$

$$x_{na} := Find(x) = 5.568 \cdot in$$

$$T_{s} := \frac{M_{u}WallLC4SerI}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 18.4 \cdot kip$$
$$f_{ss1} := \frac{T_{s}}{A_{s}Provided} = 23.279 \cdot ksi$$

$$f_{ss} := \min(f_{ss1}, 0.6f_y) = 23.279 \cdot ksi$$

Required reinforcement spacing
SharRequired :=
$$\frac{700 \cdot \gamma_e \cdot \frac{kip}{in}}{\beta_s \cdot f_{ss}} - 2 \cdot d_c = 20.789 \cdot in$$

Check if the spacing provided <
the required spacing
Check := if $(s_{bar} < s_{barRequired}, "OK", "Not OK") = "OK"$

Shrinkage and Temperature Reinforcement Requirement

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the abutment wall.

For bars, the area of reinforcement per foot (A_s),
on each face and in each direction, shall satisfy
and

$$A_{S} \ge \frac{1.3bh}{2(b+h)f_{y}}$$

$$LRFD 5.10.6$$

$$0.11 in^{2} \le A_{S} \le 0.6in^{2}$$
Minimum area of shrinkage and
temperature reinforcement

$$A_{shrink.temp} := \min \left[\begin{array}{c} \left(0.60 \frac{in^{2}}{ft} \right) \\ \left(0.11 \frac{in^{2}}{ft} \right) \\ \left[\frac{1.3 \cdot h_{wall} \cdot t_{wall} \cdot \frac{kip}{in \cdot ft}}{2(h_{wall} + t_{wall}) \cdot f_{y}} \right] \right] \right] \cdot ft = 0.349 \cdot in^{2}$$
Check if the provided area of steel >
the required area of shrinkage and
temperature steel

Design for Shear

According to the loads in the summary tables, Load Case IV under the Strength I limit state is the governing load case for the shear design.

The maximum factored shear force
at the base of the abutment wall
$$V_{uWallLC4StrI} = 6.57 \cdot \frac{kip}{ft}$$
Effective width of the section $b_V := b = 12 \cdot in$ Depth of equivalent rectangular
stress block $a := \frac{A_s Provided \cdot fy}{0.85 \cdot f_c \cdot b} = 1.549 \cdot in$ Effective shear depth $d_V := max \left(d_e - \frac{a}{2}, 0.9 \cdot d_e, 0.72 \cdot t_{wall} \right) = 34.225 \cdot in$ Nate: Since there is no temperature minimum time temperature is the well and the event lear difference to the provided temperature of the well is meter then 16

Note: Since there is no transverse reinforcement in the wall and the overall depth of the wall is greater than 16 in., the simplified procedure in LRFD 5.7.3.4.1 cannot be used. Instead, the general procedure outlined in LRFD 5.7.3.4.2 is used..

The factored N_u , V_u , and M_u are calculated at the critical section for shear, which is located at a distance d_v from the base of the abutment wall. The critical section is located in the wall segment with EPS backfill.

Factored axial force at the critical section (use negative if compression)

$$N_{uWallShear} := -\begin{bmatrix} 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} - d_{v} \cdot t_{wall} \cdot W_{c}) & \dots \\ + 1.5DW_{Sup} & \end{bmatrix}$$
$$N_{uWallShear} = -18.318 \cdot \frac{kip}{ft}$$

The lateral earth load component at the critical section for shear consists of three parts. Part 1 is the lateral load from the soil located above the EPS blocks, which is the same as that calculated in Step 3.4. Part 2 is the lateral load from the EPS due to the vertical load at the top of the EPS blocks. Part 3 is the lateral load from the soil located behind the EPS blocks above the critical section for shear.

EH 1: the lateral load from the soil located above the EPS blocks

EH 2: the lateral load from the EPS due to the vertical load at the top of the EPS blocks

EH 3: the lateral load from the soil located behind the EPS blocks and above the critical section for shear.

$$P_{\text{EHWall2Shear}} \coloneqq p_{\text{VEPS}} \cdot \left(h_{\text{EPS}} + h_{\text{SoilBelowEPS}} - d_{\text{v}}\right) = 1.042 \cdot \frac{\text{kip}}{\text{ft}}$$

$$P_{\text{EHWall3Shear}} \coloneqq \frac{1}{2} k_{\text{EPS}} \cdot \gamma_{\text{s}} \cdot \left(h_{\text{EPS}} + h_{\text{SoilBelowEPS}} - d_{\text{v}}\right)^2 = 0.231 \cdot \frac{\text{kip}}{\text{ft}}$$

$$P_{\text{EHWallShear}} \coloneqq P_{\text{EH1}} + P_{\text{EH2}} + P_{\text{EHWall3Shear}} = 2.445 \cdot \frac{\text{kip}}{\text{ft}}$$

The lateral live load surcharge at the critical section consists of two parts.

LS 1: the lateral load from the soil located above the EPS blocks due to the live load surcharge

LS 2: the lateral load from the EPS blocks located above the critical section due the the live load surcharge

$$P_{LSWall2Shear} := \frac{1}{10} \gamma_{s} \cdot h_{eq} \cdot \left(h_{EPS} + h_{SoilBelowEPS} - d_{v}\right) = 0.268 \cdot \frac{kip}{ft}$$
$$P_{LSWallShear} := P_{LSWall1} + P_{LSWall2Shear} = 0.828 \cdot \frac{kip}{ft}$$

Factored shear force at the critical section for shear (demand)

$$V_{uWallShear} := 1.5 \cdot P_{EHWallShear} + 1.75 \cdot P_{LSWallShear} + 0.5TU = 5.256 \cdot \frac{\kappa_{1P}}{ft}$$

Factored moment at the critical section for shear

$$\begin{split} M_{u}WallShear &\coloneqq 0.9 \cdot DC_{backwall} \cdot \frac{\left(t_{backwall} - t_{wall}\right)}{2} + \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup}\right) \cdot \left(l_{brtowall} - \frac{t_{wall}}{2}\right) \dots \\ &+ 1.5P_{EH1} \cdot \left(\frac{1}{3}h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} - d_{v}\right) \dots \\ &+ 1.5P_{EH2} \cdot \frac{1}{2}\left(h_{EPS} + h_{SoilBelowEPS} - d_{v}\right) \dots \\ &+ 1.75P_{LSWall1} \cdot \left(\frac{1}{2}h_{SoilAboveEPS} + h_{EPS} + h_{SoilBelowEPS} - d_{v}\right) \dots \\ &+ 1.75 \cdot P_{LSWall2Shear} \cdot \frac{\left(h_{EPS} + h_{SoilBelowEPS} - d_{v}\right)}{2} + 0.5 \cdot TU \cdot \left(h_{wall} - d_{v}\right) \\ &M_{u}WallShear = 56.896 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Check M_u since it cannot be taken less than $V_u d_v$	$M_{uWallShear} := max(M_{uWallShear}, V_{uWallShear})$	allShear $d_v = 56.896 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$
Net longitudinal tensile strain in the section at the centroid of the tension reinforcement ε_s	$_{s} := \frac{\left(\frac{M_{u}WallShear}{d_{v}} + 0.5 \cdot N_{u}WallShear} + V_{u}WallShear}{E} + \frac{V_{u}WallShear}{E} + V_{$	$\frac{\text{allShear}}{2} = 7.004 \times 10^{-4}$
	E _s . <u>ft</u>	LRFD Eq. 5.7.3.4.2-4
Crack spacing parameter	$s_{X} := d_{V} = 2.852 \text{ ft}$	
Maximum aggregate size (in.)	a _g := 1.5 MDOT S for Const	Standard Specifications truction Table 902-1
Crack spacing parameter as influenced by the aggregate size	$s_{xe} := \min\left[\begin{bmatrix} 80in \\ 12in \\ s_{x} \cdot \frac{1.38}{a_{g} + 0.63} \end{bmatrix} \right] = 22$	2.174·in LRFD Eq. 5.7.3.4.2-7
Factor indicating the ability of diagonally cracked concrete to transmit tension and shear	$\beta := \frac{4.8}{\left(1 + 750 \cdot \varepsilon_{s}\right)} \cdot \frac{51}{\left(39 + \frac{s_{xe}}{in}\right)} = 2.624$	LRFD Eq. 5.7.3.4.2-2
Nominal shear resistance of concrete, V _n , is calc	culated as follows:	
	$V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 60.3 \cdot kip$	LRFD Eq. 5.7.3.3-3
	$V_{c2} := 0.25 f_c \cdot b \cdot d_e = 315 \cdot kip$	LRFD Eq. 5.7.3.3-2
	$V_n := \min(V_{c1}, V_{c2}) = 60.31 \cdot kip$	
Resistance factor for shear	$\phi_{v} \coloneqq 0.9$	LRFD 5.5.4.2
Factored shear resistance (capacity)	$V_r := \phi_V \cdot V_n = 54.279 \cdot kip$	
Check if the capacity > the demand	Check := $if\left(\frac{V_r}{ft} > V_uWallShear, "OK", "N$	Not OK'' = " OK''
Development Length of Reinforce	ment	
The flexural reinforcing steel must be developed section for its full development length.	d on each side of the critical	LRFD 5.10.8.1.2, 5.10.8.2.1
Basic development length	$l_{db} := 2.4 \cdot d_{bar} \cdot \frac{f_y}{\sqrt{f_c \cdot ksi}} = 6.928 \text{ ft}$	LRFD Eq. 5.10.8.2.1a-2
Reinforcement location factor	$\lambda_{rl} := 1$ No more than 12 in. concret	te below
Coating factor	$\lambda_{cf} := 1.5$ Epoxy coated bars with less	than 3d _b cover
Distance from center of the bar to the nearest concrete surface	$c_b := \frac{d_{bar}}{2} + Cover_{wall} = 3.5 \cdot in$	

Reinforcement confinement factor	$\lambda_{\rm rc} := \frac{d_{\rm bar}}{c_{\rm b}} = 0.286$	
Excess reinforcement factor	$\lambda_{\rm er} := \frac{A_{\rm s}Required}{A_{\rm s}Provided} = 0.602$	
For normal weight concrete	$\lambda := 1$	
Required development length	$l_{d} := l_{db} \cdot \frac{\left(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er}\right)}{\lambda} = 1.786 \text{ ft}$	LRFD Eq. 5.10.8.2.1a-1
Since the footing thickness is 3 ft, adequate space is available for straight bars. However, the common practice is to use hooked bars which are set on the bottom reinforcing steel layer.		
Shrinkage and Temperature Reinforcement		

The following calculations check the required amou to control shrinkage and temperature stresses in the a	nt of reinforcing steel in the secondary direction abutment wall.	
The reinforcement at the front face of the abutment wall and the horizontal reinforcement at the interior should satisfy the shrinkage and temperature reinforcement requirements.		LRFD 5.10.6
The spacing of shrinkage and temperature reinforcement shall not exceed the following: L 12 in. for walls and footings greater than 18 in.		LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a maxi	mum of 18 in.	BDG 5.16.01
Select a trial bar size	bar := 6	
Nominal diameter of a reinforcing steel bar	$d_{bST} := Dia(bar) = 0.75 \cdot in$	
Cross-section area of the bar	$A_{barST} := Area(bar) = 0.44 \cdot in^2$	
Select a spacing for reinforcing steel bars	$s_{barST} := 12 \cdot in$	
Reinforcing steel area provided in the section	$A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{{}^{s}barST} = 0.44 \cdot in^2$	
The required minimum shrinkage and temperature re calculated during the design of flexural reinforceme	einforcement area at the abutment wall was previously nt.	

Required shrinkage and temperature steel area	$A_{shrink.temp} = 0.349 \cdot in^2$
Check if the provided steel area >	Check := $if(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"$
temperature steel	

The abutment wall design presented in this step provides the following details:

- No. 8 bars @ 12.0 in. spacing ($A_s = 0.79 \text{ in.}^2/\text{ft}$) as the back face flexural reinforcement
- No. 6 bars @ 12.0 in. spacing $(A_s = 0.44 \text{ in.}^2/\text{ft})$ as the front face vertical shrinkage and temperature reinforcement
- No. 6 bars @ 12.0 in. spacing ($A_s = 0.44 \text{ in.}^2/\text{ft}$) as the front and back face horizontal shrinkage and temperature • reinforcement.

Step 3.9 Structural Design of the Footing

Description

This step presents the structural design process for the abutment footing.

Page	Contents
131	Forces and Moments at the Base of the Footing
131	Toe Design
137	Heel Design
146	Shrinkage and Temperature Reinforcement

Forces and Moments at the Base of the Footing

Step 3.5 presents the load effects at the base of the footing under different load cases and limit states. A summary is presented in the following tables:

Factored vertical force, FVFt (kip/ft)

	Strength I	Service I
LC I	29.78	23.20
LC III	47.73	35.20
LC IV	39.86	30.70

of the footing, V _{uFt} (kip/ft)			
	Strength I	Service I	
LC I	6.55	4.37	
LC III	6.55	4.37	
LC IV	8.81	5.86	

Factored shear force parallel to the transverse axis

Factored moment about the longitudinal axis of the footing, M_{uFt} (kip ft/ft)

	Strength I	Service I
LC I	38.14	16.98
LC III	30.66	11.98
LC IV	57.13	31.18

Note: The length of the footing and the abutment wall is 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Toe Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:



For structural design of an eccentrically loaded foundation, a triangular or trapezoidal bearing pressure distribution is used.

LRFD 10.6.5

According to the loads in the summary tables, Load Case IV under the Strength I limit state is identified as the governing load case for the design of flexure and shear at the toe.

$$F_{VFtLC4StrI} = 39.863 \cdot \frac{kip}{ft} \qquad M_{uFtLC4StrI} = 57.133 \cdot \frac{kip \cdot ft}{ft}$$

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

The critical section for flexural design is at the front face of the wall.

Bearing pressure at the critical section

A simplified analysis method is used in this example to determine the maximum moments at the front face of the wall by selecting load factors to produce the maximum bearing pressure and minimum resisting loads. This method is conservative and eliminates the need for using multiple combinations.

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum moment at the front face of the wall.

The moment demand at the critical section

$$M_{rDemand} := q_{toe} \cdot \frac{l_{toe}^2}{2} + (q_{max} - q_{toe}) \cdot \frac{l_{toe}^2}{3} - 0.9 \cdot W_c \cdot t_{footing} \cdot \frac{l_{toe}^2}{2} - 1.0 \gamma_s \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{l_{toe}^2}{2}$$
$$M_{rDemand} = 67.396 \cdot \frac{kip \cdot ft}{ft}$$

Flexure Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 8	
Nominal diameter of a reinforcing steel bar	$d_{bar} := Dia(bar) = 1 \cdot in$	
Cross-section area of a bar on the flexural tension side	$A_{\text{bar}} := \text{Area}(\text{bar}) = 0.79 \cdot \text{in}^2$	
The spacing of the main reinforcing steel bars in walls and lesser of 1.5 times the thickness of the member or 18 in.	d slabs shall not be greater than the	LRFD 5.10.3.2
The spacing of shrinkage and temperature reinforcement 12 in. for walls and footings greater than 18 in.	shall not exceed the following:	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a maximum	of 18 in.	BDG 5.16.01 and 5.22.01
Footing thickness	$t_{footing} = 3 ft$	
Select a spacing for reinforcing steel bars	$s_{bar} := 12 \cdot in$	
Select a 1-ft wide strip for the design. Area of tension steel provided in a 1-ft wide strip	$A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.79$	$2 \cdot \ln^2$

$$e_{B} := \frac{M_{uFtLC4StrI}}{F_{VFtLC4StrI}} = 1.433 \cdot ft$$

$$q_{max} := \frac{F_{VFtLC4StrI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 4.834 \cdot ksf$$

$$q_{min} := \frac{F_{VFtLC4StrI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 1.072 \cdot ksf$$

 $q_{\text{toe}} \coloneqq q_{\min} + \frac{\left(q_{\max} - q_{\min}\right)}{B_{\text{footing}}} \cdot \left(B_{\text{footing}} - l_{\text{toe}}\right) = 3.069 \cdot \text{ksf}$

LRFD 5.6.3.2

Effective depth	$d_e := t_{footing} - Cover_{ft} = 32$	2. in
Resistance factor for flexure	$\phi_{f} := 0.9$	LRFD 5.5.4.2
Width of the compression face of the section	b := 12in	
Stress block factor β_1	$:= \min\left[\max\left[0.85 - 0.05 \cdot \left(\frac{f_c - 4ksi}{ksi}\right)\right]\right]$	[0.65], 0.85 = 0.85 LRFD 5.6.2.2
Solve the following equation of A_s to calculate the assumed initial A_s value to solve the equation.	ne required area of steel to satisfy the mom	ent demand. Use an
The initial assumption	$A_s := 1in^2$	
	Given $M_{rDemand}$ ft = ϕ_{f} .	$\mathbf{A}_{\mathbf{s}} \cdot \mathbf{f}_{\mathbf{y}} \cdot \left[\mathbf{d}_{\mathbf{e}} - \frac{1}{2} \cdot \left(\frac{\mathbf{A}_{\mathbf{s}} \cdot \mathbf{f}_{\mathbf{y}}}{0.85 \cdot \mathbf{f}_{\mathbf{c}} \cdot \mathbf{b}} \right) \right]$
Required area of steel	$A_{sRequired} := Find(A_s) = 0$	$.475 \cdot \text{in}^2$
Check if $A_{sProvided} > A_{sRequired}$	Check := if $(A_{sProvided} > A_{sRee})$	quired, "OK", "Not OK") = "OK"
Moment capacity of the section with the provided steel	$M_{Provided} := \phi_f \cdot A_{sProvided}$	$f_{y} \cdot \frac{\left[d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s}Provided \cdot f_{y}}{0.85 \cdot f_{c} \cdot b}\right)\right]}{ft}$
	$M_{\text{Provided}} = 111.007 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$	
Distance from the extreme compression fiber to the neutral axis	$c := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot \beta_{1} \cdot b} = 1.82 \cdot in$	
Check the validity of the assumption, $f_s = f_y$	Check_ $f_s := if\left(\frac{c}{d_e} < 0.6, "OF$	$K^{"}, "\operatorname{Not} OK^{"} = "OK^{"}$

Limits for Reinforcement

The tensile reinforcement provided must develop a factored flexural resistance equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

1.33 times the factored moment demand

$$\gamma_{1} := 1.6 \quad \text{For concrete structures that are not precast segmental}$$

$$\gamma_{3} := 0.67 \quad \text{For ASTM A615 Grade 60 reinforcement}$$

$$S_{c} := \frac{1}{6} \cdot b \cdot t_{\text{footing}}^{2} = 2.592 \times 10^{3} \cdot \text{in}^{3}$$

$$M_{cr} := \frac{\gamma_{3} \cdot \gamma_{1} \cdot f_{r} \cdot S_{c}}{ft} = 96.254 \cdot \frac{\text{kip} \cdot \text{ft}}{ft}$$

$$1.33 \cdot M_{r}\text{Demand} = 89.637 \cdot \frac{\text{kip} \cdot \text{ft}}{ft}$$

LRFD 5.6.3.3

Required moment to satisfy the minimum reinforcement requirement

$$M_{req} := \min(1.33M_{rDemand}, M_{cr}) = 89.637 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$

Check := if $(M_{Provided} > M_{req}, "OK", "Not OK") = "OK"$

Check the adequacy of section capacity

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest bar

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer nearest the tension face

The calculation of tensile stress in nonprestressed re-, requires establishing the neutral axis location and the moment demand a

The position of the cross-section's neutral axis is de o calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme compression fiber to the neutral axis

Given

$$\frac{1}{2} \cdot b \cdot x^{2} = \frac{E_{s}}{E_{c}} \cdot A_{sProvided} \cdot (d_{e} - x)$$

$$x_{na} := Find(x) = 5.303 \cdot in$$

Position of the neutral axis

The vertical force and moment at the base of the footing from Load Case IV under the Service I limit state are:

$$F_{VFtLC4SerI} = 30.702 \cdot \frac{kip}{ft}$$
 $M_{uFtLC4SerI} = 31.183 \cdot \frac{kip \cdot ft}{ft}$

Eccentricity in the footing width direction under Service I limit state

Maximum and minimum bearing pressure under Service I limit state

$$e_{BSerI} \coloneqq \frac{M_{uFtLC4SerI}}{F_{VFtLC4SerI}} = 1.016 \cdot ft$$

$$q_{maxSerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{BSerI}}{B_{footing}}\right) = 3.301 \cdot ksf$$

$$q_{minSerI} \coloneqq \frac{F_{VFtLC4SerI}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{BSerI}}{B_{footing}}\right) = 1.248 \cdot ksf$$

LRFD Eq. 5.6.7-1

LRFD 5.6.7

 $s \le \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$

 $\gamma_{e} := 1.00$

$$d_{c} := \text{Cover}_{ft} + \frac{d_{bar}}{2} = 4.5 \cdot \text{in}$$
$$d_{s} := 1 + \frac{d_{c}}{2} = 1.2$$

$$\beta_{\rm s} := 1 + \frac{d_{\rm c}}{0.7(t_{\rm footing} - d_{\rm c})} = 1.204$$

einforcement at the service limit state,
$$f_{ss}$$

at the critical section.

Bearing pressure at the critical section under Service I limit state

The moment at the critical section under the Service I limit state:

$$M_{rSerI} := q_{toeSerI} \cdot \frac{l_{toe}^{2}}{2} + (q_{maxSerI} - q_{toeSerI}) \cdot \frac{l_{toe}^{2}}{3} - W_{c} \cdot t_{footing} \cdot \frac{l_{toe}^{2}}{2} - \gamma_{s} \cdot (h_{toeDepth} - t_{footing}) \cdot \frac{l_{toe}^{2}}{2}$$

$$M_{rSerI} = 41.109 \cdot \frac{kip \cdot ft}{ft}$$
Tensile force in the reinforcing steel due to the service limit state moment
$$T_{s} := \frac{M_{rSerI}}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 16.3 \cdot kip$$
Stress in the reinforcing steel due to the service limit state moment
$$f_{ss1} := \frac{T_{s}}{A_{sProvided}} = 20.655 \cdot ksi$$
Required reinforcement spacing
$$s_{barRequired} := \frac{700 \cdot \gamma_{e} \cdot \frac{kip}{in}}{\beta_{s} \cdot f_{ss}} - 2 \cdot d_{c} = 19.146 \cdot in$$
Check if the spacing provided < the check := if (s_{bar} < s_{barRequired}, "OK", "Not OK") = "OK"
Strinkage and Temperature Reinforcement Requirement
$$LRFD 5.10.6$$

 $q_{toeSerI} = 2.338 \cdot ksf$

 $q_{toeSerI} \coloneqq q_{minSerI} + \frac{\left(q_{maxSerI} - q_{minSerI}\right)}{B_{footing}} \cdot \left(B_{footing} - l_{toe}\right)$

Shrinkage and Temperature Reinforcement Requirement

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the toe:

 $A_{\text{shrink.temp}} \coloneqq \min \left[\begin{array}{c} \left(0.60 \frac{\text{in}^2}{\text{ft}} \right) \\ \left(0.11 \frac{\text{in}^2}{\text{ft}} \right) \\ \left[\frac{1.3 \cdot \text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}}}{2(\text{B}_{\text{footing}} \cdot \text{t}_{\text{footing}}) \cdot \text{f}_{\text{v}}} \right] \end{array} \right] \right] \cdot \text{ft} = 0.319 \cdot \text{in}^2$ Minimum area of shrinkage and temperature reinforcement Check := if $(A_{sProvided} > A_{shrink.temp}, "OK", "Not OK") = "OK"$ the required area of shrinkage and

Check if the provided area of steel >

temperature steel

Design for Shear

Effective width of the section $b = 12 \cdot in$ Depth of equivalent rectangular stress block $a := \frac{A_s Provided \cdot f_y}{0.85 \cdot f_c \cdot b} = 1.549 \cdot in$

Effective shear depth

$$d_{V} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{footing}\right) = 31.225 \cdot \text{in}$$
 LRFD
5.7.2.8

The critical section for shear at the toe is located at a distance d_v from the front face of the wall.

Distance from the toe to the critical section

$$l_{shear} \coloneqq l_{toe} - d_{v} = 3.731 \text{ ft}$$
$$q_{d} \coloneqq q_{min} + \frac{\left(q_{max} - q_{min}\right)}{B_{footing}} \cdot \left(B_{footing} - l_{shear}\right) = 3.794 \cdot \text{ksf}$$

Check := if $(l_{toe} < 3 \cdot d_V, "Yes", "No") = "Yes"$

Bearing pressure at the shear critical section

As shown below, minimum load factors are used for the resisting forces (such as the overburden and footing self-weight) to calculate the maximum shear at the shear critical section.

Factored shear force (demand) at the shear critical section

$$V_{uFtToe} := \frac{(q_{max} + q_d)}{2} \cdot l_{shear} - 0.9 \cdot W_c \cdot t_{footing} \cdot l_{shear} - 1.0 \cdot \gamma_s \cdot (h_{toeDepth} - t_{footing}) \cdot l_{shear}$$
$$V_{uFtToe} = 12.794 \cdot \frac{kip}{ft}$$

The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than 3d_v.

 $\beta := 2$

Check if the distance l_{toe} is less than $3d_v$

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n , is calculated as follows:

	$V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 42 \cdot kip$	LRFD Eq. 5.7.3.3-3
	$V_{c2} := 0.25 f_c \cdot b \cdot d_e = 288 \cdot kip$	LRFD Eq. 5.7.3.3-2
	$V_n := \min(V_{c1}, V_{c2}) = 42.035 \cdot \text{kip}$	
Resistance factor for shear	$\phi_{V} := 0.9$	LRFD 5.5.4.2
Factored shear resistance (capacity)	$V_r := \phi_V \cdot V_n = 37.831 \cdot kip$	
Check if the capacity > the shear demand	Check := $if\left(\frac{V_r}{ft} > V_{uFtToe}, "OK", "Note$	(OK'') = "OK''

Development Length of Reinforcement			
The flexural reinforcing steel must be developed on each full development length.	n side of the critic	cal section for its	LRFD 5.10.8.1.2
Available length for rebar development	l _{d.available} ∺	$= l_{toe} - Cover_{ft} = 6 ft$	
Basic development length	$l_{db} := 2.4 \cdot d_b$	$\operatorname{ar} \cdot \frac{\mathrm{f}_{\mathrm{y}}}{\sqrt{\mathrm{f}_{\mathrm{c}} \cdot \mathrm{ksi}}} = 6.928 \mathrm{ft}$	LRFD Eq. 5.10.8.2.1a-2
Reinforcement location factor	$\lambda_{rl} := 1$	No more than 12 in. conc	crete below
Coating factor	$\lambda_{\rm cf} \coloneqq 1.5$	Epoxy coated bars with k	ess than 3d _b cover
Reinforcement confinement factor	$\lambda_{\rm rc} := 0.4$	For $c_b > 2.5$ in. and No. 8	bars or smaller
Excess reinforcement factor	$\lambda_{\rm er} := \frac{A_{\rm sRec}}{A_{\rm sPro}}$	$\frac{\text{quired}}{\text{ovided}} = 0.601$	LRFD Eq. 5.10.8.2.1c-4
Factor for normal weight concrete	$\lambda := 1$		
Required development length	l _{d.required} :=	$l_{db} \cdot \frac{\left(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er}\right)}{\lambda} =$	LRFD Eq. = 2.499 ft 5.10.8.2.1a-1
Check if $l_{d.available} > l_{d.required}$	Check := if(]	d.available > ld.required	, "OK", "Not OK" = "OK"

Heel Design

The necessary dimensions, loads, and the bearing pressure distribution are shown in the following figure:



The self-weight of the footing, the weight of soil, live load surcharge and the bearing pressure act on the heel. The critical load combination for the design selects the load factors to produce the minimum vertical loads and maximum eccentricities resulting in the minimum bearing pressure.

The critical location for the design of flexure is located at the back face of the wall.

In the general case of a cantilever abutment wall, where the downward load on the heel is larger than the upward reaction of the soil under the heel, the top of the heel is in tension. Therefore, the critical section for shear is taken at the back face of the abutment wall.

Load cases I, III, and IV under the Strength I limit state are used to calculate the maximum moment and shear at the critical sections.

Load Case I

Minimum vertical force	$F_{VFtLC1StrIMin} = 21.662 \cdot \frac{kip}{ft}$	Step 3.6, sliding resistance check
Factored moment about the longitudinal axis of the footing	$M_{uFtLC1StrI} = 38.136 \cdot \frac{kip \cdot ft}{ft}$	Step 3.6, eccentric load limitation check
Eccentricity in the footing width direction	$e_{B} := \frac{M_{uFtLC1StrI}}{F_{VFtLC1StrIMin}} = 1.761 \cdot ft$	

Maximum and minimum bearing pressure

$$q_{max} := \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 2.86 \cdot ksf$$
$$q_{min} := \frac{F_{VFtLC1StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.349 \cdot ksf$$

 $q_{heelLC1StrI} := q_{min} + (q_{max} - q_{min}) \frac{l_{heel}}{B_{footing}} = 1.093 \cdot ksf$

LRFD 5.12.8.4

LRFD C5.12.8.6.1

Bearing pressure at the critical section

Factored moment at the critical section

$$M_{rLC1StrI} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|heel^{2}}{2} + 1.35 EV_{earthBk} \cdot \frac{|heel}{2} - q_{min} \cdot l_{heel} \cdot \frac{|heel}{2} - \frac{1}{6} (q_{heelLC1StrI} - q_{min}) l_{heel}^{2}$$
$$M_{rLC1StrI} = 12.671 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC1StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC1StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC1StrI} = 5.839 \cdot \frac{kip}{ft}$$

Load Case III

Two cases need to be considered: without and with the live load.

Without the live load:

Minimum vertical force

$$F_{VFtLC3StrIMin_noLL} = 26.754 \cdot \frac{kip}{ft}$$
 Step 3.6, sliding
resistance check

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

$$\begin{split} M_{uFtLC3StrI_noLL} &= 34.635 \, \text{ft} \cdot \frac{\text{kip}}{\text{ft}} & \text{Step 3.6, eccentric} \\ \text{load limitation check} \\ e_{B} &\coloneqq \frac{M_{uFtLC3StrI_noLL}}{F_{VFtLC3StrIMin_noLL}} = 1.295 \cdot \text{ft} \\ q_{max} &\coloneqq \frac{F_{VFtLC3StrIMin_noLL}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 3.122 \cdot \text{ksf} \\ q_{min} &\coloneqq \frac{F_{VFtLC3StrIMin_noLL}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 0.842 \cdot \text{ksf} \end{split}$$

$$q_{\text{heelLC3StrI}} \coloneqq q_{\text{min}} + (q_{\text{max}} - q_{\text{min}}) \frac{l_{\text{heel}}}{B_{\text{footing}}} = 1.517 \cdot \text{ksf}$$

Factored moment at the critical section

Bearing stress at the critical section

$$M_{rLC3StrI_noLL} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|hee|^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{|hee|}{2} - q_{min} \cdot l_{heel} \cdot \frac{|hee|}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) l_{heel}^{2} M_{rLC3StrI_noLL} = 8.913 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC3StrI_noLL} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC3StrI_noLL} = 4.006 \cdot \frac{kip}{ft}$$

With the live load:

Minimum vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

Bearing pressure at the critical section

$$F_{VFtLC3StrIMin} = 36.304 \cdot \frac{kip}{ft}$$
 Step 3.6, sliding
resistance check

 $M_{uFtLC3StrI} = 30.656 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

$$e_{\rm B} := \frac{M_{\rm u} FtLC3StrI}{F_{\rm V} FtLC3StrIMin} = 0.844 \cdot ft$$

$$q_{max} := \frac{F_{VFtLC3StrIMin}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 3.698 \cdot ksf$$

$$q_{min} := \frac{F_{VFtLC3StrIMin}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 1.68 \cdot ksf$$

$$q_{heelLC3StrI} := q_{min} + \left(q_{max} - q_{min}\right) \frac{l_{heel}}{B_{footing}} = 2.278 \cdot ksf$$

Factored moment at the critical section

$$M_{rLC3StrI} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|heel|^{2}}{2} + 1.35 EV_{earthBk} \cdot \frac{|heel|}{2} - q_{min} \cdot t_{heel} \cdot \frac{|heel|}{2} - \frac{1}{6} (q_{heelLC3StrI} - q_{min}) t_{heel}^{2}$$
$$M_{rLC3StrI} = 2.413 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC3StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC3StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC3StrI} = 0.808 \cdot \frac{kip}{ft}$$

Load Case IV

Two cases need to be considered: without and with the live load surcharge.

Without the live load surcharge:

Minimum vertical force
$$F_{VFtLC4StrIMin_noLS} = 26.754 \cdot \frac{kip}{ft}$$
 $Step 3.6, sliding resistance checkFactored moment about the longitudinal axis of the footing $M_{uFtLC4StrI_noLS} = 38.891 \cdot \frac{kip \cdot ft}{ft}$ $Step 3.6, eccentric load limitation checkEccentricity in the footing width direction $e_B := \frac{M_uFtLC4StrI_noLS}{F_{VFtLC4StrIMin}} = 1.368 \cdot ft$ $Step 3.6, eccentric load limitation checkMaximum and minimum bearing pressures $q_{max} := \frac{F_{VFtLC4StrIMin_noLS}}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_B}{B_{footing}}\right) = 3.186 \cdot ksf$ $q_{min} := \frac{F_{VFtLC4StrIMin_noLS}}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_B}{B_{footing}}\right) = 0.777 \cdot ksf$ Bearing pressure at the critical section $q_{heelLC4StrI := q_{min} + (q_{max} - q_{min})\frac{l_{heel}}{B_{footing}}} = 1.491 \cdot ksf$ Factored moment at the critical section $heel^2 + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} - q_{min} \cdot l_{heel} \cdot \frac{1}{2} - \frac{1}{6}(q_{heelLC4StrI - q_{min})l_{heel}^2$ $M_{rLC4StrI_noLS} = 9.327 \cdot \frac{kip \cdot ft}{ft}$$$$

Factored shear force at the critical section

 $V_{uHeelLC4StrI_noLS} := 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC4StrI} - q_{min}) \cdot l_{heel}$ $V_{uHeelLC4StrI_noLS} = 4.187 \cdot \frac{kip}{ft}$

2

With the live load surcharge:

Minimum vertical force

Factored moment about the longitudinal axis of the footing

Eccentricity in the footing width direction

Maximum and minimum bearing pressure

$$e_{B} := \frac{M_{u}FtLC4StrI}{F_{V}FtLC4StrIMin} = 2.009 \cdot ft$$

$$q_{max} := \frac{F_{V}FtLC4StrIMin}{B_{footing}} \cdot \left(1 + \frac{6 \cdot e_{B}}{B_{footing}}\right) = 3.987 \cdot ksf$$

$$q_{min} := \frac{F_{V}FtLC4StrIMin}{B_{footing}} \cdot \left(1 - \frac{6 \cdot e_{B}}{B_{footing}}\right) = 0.225 \cdot ksf$$

Step 3.6, sliding

resistance check

Step 3.6, summary table

 $F_{VFtLC4StrIMin} = 28.434 \cdot \frac{kip}{ft}$

 $M_{uFtLC4StrI} = 57.133 \cdot \frac{kip \cdot ft}{ft}$

$$q_{\text{heelLC4StrI}} \coloneqq q_{\min} + (q_{\max} - q_{\min}) \frac{q_{\text{heel}}}{B_{\text{footing}}} = 1.34 \cdot \text{kst}$$

Factored moment at the critical section

Bearing stress at the critical section

$$M_{rLC4StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot \frac{|hee|^{2}}{2} + 1.35 EV_{earthBk} \cdot \frac{|hee|}{2} - q_{min} \cdot l_{heel} \cdot \frac{|hee|}{2} - \frac{1}{6} (q_{heelLC4StrI} - q_{min}) l_{heel}^{2}$$
$$M_{rLC4StrI} = 12.672 \cdot \frac{kip \cdot ft}{ft}$$

Factored shear force at the critical section

$$V_{uHeelLC4StrI} \coloneqq 1.25 \cdot W_{c} \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} - q_{min} \cdot l_{heel} - \frac{1}{2} \cdot (q_{heelLC4StrI} - q_{min}) \cdot l_{heel}$$
$$V_{uHeelLC4StrI} = 5.593 \cdot \frac{kip}{ft}$$

Moment demand at the critical section

 $M_{\text{HeelDemand}} \coloneqq \max \left(M_{\text{rLC1StrI}}, M_{\text{rLC3StrI_noLL}}, M_{\text{rLC3StrI}}, M_{\text{rLC4StrI_noLS}}, M_{\text{rLC4StrI}} \right) = 12.672 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$ Shear demand at the critical section

$$V_{\text{HeelDemand}} \coloneqq \max \left(V_{\text{uHeelLC1StrI}}, V_{\text{uHeelLC3StrI}} \text{ noLL}, V_{\text{uHeelLC3StrI}}, V_{\text{uHeelLC4StrI_noLS}}, V_{\text{uHeelLC4StrI}} \right)$$
$$V_{\text{HeelDemand}} = 5.839 \cdot \frac{\text{kip}}{\text{ft}}$$

Flexure Resistance

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 6
Nominal diameter of a reinforcing steel bar	$d_{\text{bar}} := \text{Dia}(\text{bar}) = 0.75 \cdot \text{in}$
Cross-section area of a bar on the flexural tension side	$A_{\text{bar}} := \text{Area}(\text{bar}) = 0.44 \cdot \text{in}^2$

2

LRFD 5.6.3.2

The spacing of the main reinforcing steel bars in walls lesser of 1.5 times the thickness of the member or 18 in	and slabs shall not be greater than the 1.	LRFD 5.10.3.2
The spacing of shrinkage and temperature reinforcements 12 in. for walls and footings greater than 18 in	ent shall not exceed the following: n.	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a maximum	um of 18 in. BDG	5.16.01 and 5.22.01
Footing thickness	$t_{footing} = 3 ft$	
Selected spacing of reinforcing bars	$s_{bar} := 12 \cdot in$	
Select a 1-ft wide strip for the design.		
Area of tension steel provided in a 1-ft wide strip	$A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.44 \cdot in^2$	2
Effective depth	$d_e := t_{footing} - Cover_{ft} = 32 \cdot in$	
Resistance factor for flexure	$\phi_{f} \coloneqq 0.9$	LRFD 5.5.4.2
Width of the compression face of the section	b := 12in	
Stress block factor	$\beta_1 = 0.85$	
Solve the following equation of A_s to calculate the requassumed initial A_s value to solve the equation.	uired area of steel to satisfy the moment dema	and. Use an
Initial assumption	$A_a := 1 in^2$	
ľ	Given $M_{\text{HeelDemand}} \cdot \text{ft} = \phi_f \cdot A_s \cdot f$	$\mathbf{\hat{f}_y} \left[\mathbf{d_e} - \frac{1}{2} \cdot \left(\frac{\mathbf{A_s} \cdot \mathbf{f_y}}{0.85 \cdot \mathbf{f_c} \cdot \mathbf{b}} \right) \right]$
Required area of steel	$A_{sRequired} := Find(A_s) = 0.088 \cdot in^2$	
Check if $A_{sProvided} > A_{sRequired}$	Check := $if(A_{sProvided} > A_{sRequir})$	ed, "OK", "Not OK") = "OK"
Moment capacity of the section with the provided steel	$M_{\text{Provided}} \coloneqq \phi_{f} \cdot A_{s\text{Provided}} \cdot f_{y} \cdot \underbrace{\begin{bmatrix} d_{e} \\ & \\ & \\ & \\ & \\ M_{\text{Provided}} = 62.506 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}} \end{bmatrix}}_{\text{ft}}$	$\frac{1}{2} \cdot \left(\frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) $ ft
Distance from the extreme compression fiber to the neutral axis	$c := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot \beta_{1} \cdot b} = 1.01 \cdot in$	
Check the validity of the assumption, $f_s = f_y$	$\text{Check}_{f_{S}} := \text{if}\left(\frac{c}{d_{e}} < 0.6, "\text{OK"}, "\text{N}\right)$	ot OK") = "OK"
Limits for Reinforcement		LRFD 5.6.3.3
The tensile reinforcement provided must be adequate t	o develop a factored flexural resistance at lea	ast equal to the

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor

Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement

Section modulus

Cracking moment

1.33 times the factored moment demand

Required factored moment to satisfy the minimum reinforcement requirement

Check the adequacy of the section capacity

Control of Cracking by Distribution of Reinforcement

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest flexural reinforcement

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, f_{ss} requires establishing

the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual f4. stress in the reinforcement. This process starts with an ass

Given

Assumed distance from the extreme compression fiber to the neutral axis

Position of the neutral axis

Maximum and minimum bearing pressure under Service I limit state (from the toe design)

Bearing pressure at the critical section

$$S_{c} := \frac{1}{6} \cdot b \cdot t_{footing}^{2} = 2.592 \times 10^{3} \cdot in^{3}$$
$$M_{cr} := \frac{\gamma_{3} \cdot \gamma_{1} \cdot f_{r} \cdot S_{c}}{ft} = 96.254 \cdot \frac{kip \cdot ft}{ft}$$

 $1.33 \cdot M_{\text{HeelDemand}} = 16.854 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

$$M_{req} := \min(1.33M_{HeelDemand}, M_{cr}) = 16.854 \cdot \frac{kip \cdot ft}{ft}$$

Check := if
$$(M_{Provided} > M_{req}, "OK", "Not OK") = "OK"$$

$$d_c := Cover_{ft} = 4 \cdot in$$

$$\beta_{\rm s} \coloneqq 1 + \frac{d_{\rm c}}{0.7\left(t_{\rm footing} - d_{\rm c}\right)} = 1.179$$

$$\mathbf{x} := 5 \cdot \mathbf{in}$$

$$\frac{1}{2} \cdot \mathbf{b} \cdot \mathbf{x}^2 = \frac{\mathbf{E}_s}{\mathbf{E}_c} \cdot \mathbf{A}_{s\text{Provided}} \cdot (\mathbf{d}_e - \mathbf{x})$$

$$\mathbf{x}_{na} := \text{Find}(\mathbf{x}) = 4.049 \cdot \mathbf{in}$$

 $q_{minSerI} = 1.248 \cdot ksf$ $q_{maxSerI} = 3.301 \cdot ksf$

 $q_{\text{HeelSerI}} := q_{\text{minSerI}} + \frac{\left(q_{\text{maxSerI}} - q_{\text{minSerI}}\right)}{B_{\text{footing}}} \cdot l_{\text{heel}} = 1.856 \cdot \text{ksf}$

$$\leq \frac{100 \text{ He}}{\beta_{s} \cdot f_{ss}} - 2 \cdot d_{c}$$
LRFD Eq. 5.6.7-1

e := 1.00

$$\gamma_e := 1.00$$

 $d_c := Cover_{ft} = 4 \cdot in$

$$s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$$

LRFD 5.6.7

144

The moment at the critical section under the Service I limit state

$$\begin{split} M_{heelSerI} &\coloneqq W_{c} \cdot t_{footing} \cdot \frac{|heel}{2}^{2} + EV_{earthBk} \cdot \frac{|heel}{2} \dots \\ &+ V_{LSFooting} \cdot \frac{|heel}{2} - q_{minSerI} \cdot \frac{|heel}{2}^{2} - (q_{HeelSerI} - q_{minSerI}) \cdot \frac{|heel}{6}^{2} \\ &M_{heelSerI} = 3.507 \cdot \frac{kip \cdot ft}{ft} \\ \text{teel due} \\ T_{s} &\coloneqq \frac{M_{heelSerI}}{d_{e} - \frac{x_{na}}{3}} \cdot ft = 1.4 \cdot kip \\ e \text{ to the} \\ f_{ss1} &\coloneqq \frac{T_{s}}{A_{sProvided}} = 3.12 \cdot ksi \\ f_{ss} &\coloneqq min(f_{ss1}, 0.6f_{y}) = 3.12 \cdot ksi \\ s_{barRequired} &\coloneqq \frac{700 \cdot \gamma_{e} \cdot \frac{kip}{in}}{\beta_{s} \cdot f_{ss}} - 2 \cdot d_{c} = 182.337 \cdot in \\ \text{the} \\ \end{split}$$

Tensile force in the reinforcing steel due to the service limit state moment

Stress in the reinforcing steel due to the service limit state moment

 f_{ss} (not to exceed 0.6 f_y)

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement

The required minimum shrinkage and temperature reinforcement area was calculated previously for the toe.

Required shrinkage and temperature steel area

Design for Shear

The critical section for shear in the heel is located at the back face of the abutment wall.

Shear demand at the critical section (max. from the load cases)

Effective width of the section

Depth of the equivalent rectangular stress block

Effective shear depth

$$A_{shrink.temp} = 0.319 \cdot in^2$$

 $V_{\text{HeelDemand}} = 5.839 \cdot \frac{\text{kip}}{\text{ft}}$

Check := if
$$(A_{sProvided} > A_{shrink.temp}, "OK", "Not OK") = "OK"$$

$$b = 12 \cdot in$$

$$a := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} = 0.863 \cdot \text{in}$$
$$d_{v} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{footing}\right) = 31.569 \cdot \text{in} \qquad \begin{array}{c} \text{LRFD} \\ \text{5.7.2.8} \end{array}$$

LRFD 5.10.6
The simplified procedure for nonprestressed sections can be used for the design of shear in concrete footings when the distance from the point of zero shear to the face of the wall is less than $3d_{y}$.

Check := if
$$(l_{heel} < 3 \cdot d_V, "Yes", "No") = "Yes"$$

LRFD 5.7.3.4.1

Check if the distance $l_{heel} < 3d_v$

Check if the

Therefore, the simplified procedure is used.

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n, is calculated as follows:

	$V_{c1} := 0.0316 \cdot \beta \cdot \sqrt{f_c \cdot ksi} \cdot b \cdot d_e = 42 \cdot kip$	LRFD Eq. 5.7.3.3-3
	$V_{c2} := 0.25 f_c \cdot b \cdot d_e = 288 \cdot kip$	LRFD Eq. 5.7.3.3-2
	$V_n := \min(V_{c1}, V_{c2}) = 42.035 \cdot kip$	
Resistance factor for shear	$\phi_{V} := 0.9$	LRFD 5.5.4.2
Factored shear resistance (capacity)	$V_r := \phi_V \cdot V_n = 37.831 \cdot kip$	
Check if the shear capacity > the demand	Check := if $\left(\frac{V_r}{ft} > V_{HeelDemand}, "OK"\right)$, "Not OK") = "OK"

 $\beta := 2$

Development Length of Reinforcement

The flexural reinforcing steel must be developed on each side of the critical section for its LRFD 5.10.8.1.2 full development length. $l_{d.available} := l_{heel} - Cover_{ft} = 44 \cdot in$ Available length for rebar development $l_{db} := 2.4 \cdot d_{bar} \cdot \frac{f_y}{\sqrt{f_c \cdot ksi}} = 5.196 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-2 Basic development length Reinforcement location factor More than 12 in. concrete below $\lambda_{r1} := 1.3$ $\lambda_{\rm cf} \coloneqq 1.5$ Epoxy coated bars with less than 3db cover Coating factor Reinforcement confinement factor $\lambda_{\rm rc} := 0.4$ For $c_b > 2.5$ in. and No. 8 bars or smaller $\lambda_{\text{er}} \coloneqq \frac{A_{\text{sRequired}}}{A_{\text{sProvided}}} = 0.201$ LRFD Eq. 5.10.8.2.1c-4 Excess reinforcement factor $\lambda := 1$ Factor for normal weight concrete $l_{d.required} := l_{db} \cdot \frac{(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er})}{\lambda} = 9.754 \cdot in$ LRFD Eq. 5.10.8.2.1a-1 Required development length Check := if $(l_{d.available} > l_{d.required}, "OK", "Not OK") = "OK"$

Check if $l_{d.available} > l_{d.required}$

Shrinkage and Temperature Reinforcement Design

 The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing.
 LRFD 5.10.6

 The reinforcement along the longitudinal direction of the footing at the top and bottom should satisfy the shrinkage and temperature reinforcement requirements.
 LRFD 5.10.6

 The spacing of shrinkage and temperature reinforcement shall not exceed the following:
 LRFD 5.10.6

 12 in. for walls and footings greater than 18 in.
 18

bar := 6

Note: MDOT limits reinforcement spacing to a maximum of 18 in.

Select a trial bar size

Nominal diameter of a reinforcing steel bar

Cross-section area of the bar

Select a spacing for reinforcing steel bars

Reinforcing steel area provided in the section

Required minimum area of shrinkage and temperature reinforcement in the footing

Check if the provided steel area > the required area for shrinkage and temperature steel $d_{bST} := \text{Dia}(bar) = 0.75 \cdot \text{in}$ $A_{barST} := \text{Area}(bar) = 0.44 \cdot \text{in}^2$ $s_{barST} := 12 \cdot \text{in}$ $A_{sProvidedST} := \frac{A_{barST} \cdot 12\text{in}}{s_{barST}} = 0.44 \cdot \text{in}^2$

$$A_{\text{shrink.temp}} = 0.319 \cdot \text{in}^2$$

Check := if $(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"$

BDG 5.16.01 and 5.22.01

The footing design presented in this step provides the following details:

- No. 6 bars @ 12.0 in. spacing ($A_s = 0.44$ in.²/ft) as the transverse flexural reinforcement at the top of the footing
- No. 8 bars @ 12.0 in. spacing (A_s = 0.79 in.²/ft) as the transverse flexural reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing (A_s=0.44 in.²/ft) as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.



Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

References

MDOT Geotechnical Manual (2019).

https://www.michigan.gov/-/media/Project/Websites/MDOT/Programs/Bridges-and-Structures/Geotechnical-Services/Geotechnical-Manual.pdf?rev=00901c15702e4493963ee866d0ed4c01 (Last accessed: 09/30/2022)

Stark, T. D., Arellano, D., Horvath, J. S., and Leshchinsky, D. (2004). "Geofoam Applications in the Design and Construction of Highway Embankments," the National Cooperative Highway Research Program, the Transportation Research Board, Washington, D.C. 20001

https://trb.org/publications/nchrp/nchrp_w65.pdf (Last accessed: 09/30/2022)

Section 4 Abutment with Piles

Step 4.1 Preliminary Abutment Dimensions

Description

►

This step presents the selected preliminary abutment dimensions.

The design criteria, bridge information, material properties, reinforcing steel cover requirements, soil types and properties, along with superstructure loads are taken from Section 2.

148

This section presents the design of a full-depth reinforced concrete cantilever abutment with pile supports.

The structural design of the backwall and abutment wall is presented in Section 2. The pile design presented in this example covers structural design aspects assuming that the geotechnical design is performed by the Geotechnical Services Section.

The designers select the preliminary dimensions based on state-specific standards and past experience. The following figure shows the abutment geometry and dimensional variables:



The abutment has an independent backwall with a sliding deck.BDC 6.20.03Backwall height $h_{backwall} := 4.25ft$ Backwall thickness $l_{backwall} := 1ft + 6in = 1.5 ft$ Abutment wall height $h_{wall} := 17.54ft$ Abutment wall height $h_{wall} := 3ft + 2in = 3.167 ft$ Distance from the too to the front face of the abutment wall $l_{too} := 1ft + 3in = 1.25 ft$ Distance from the heel to the back face of the abutment wall $l_{heel} := 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width $B_{footing} := l_{toe} + l_{heel} + t_{wall} = 11 ft$ Footing length $L_{footing} := L_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on either side. $I_{too ing} := 3ft$ Toe fill depth to the bottom of the footing $h_{tooDepth} := 7ft$ Note: Bottoms of footings are normally set 4 ft below the existing \lor proposed ground line to avoid first heave. The depth of embedment could be deep:BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Abutment length	$L_{abut} := W_{deck} = 63.75 \text{ ft}$	
Backwall heighthbackwall := 4.25ftBackwall hicknessbackwall := 1ft + 6in = 1.5 ftAbutment wall heighthwall := 17.54ftAbutment wall hicknesstwall := 3ft + 2in = 3.167 ftDistance from the toe to the front face of the abutment wallltoe := 1ft + 3in = 1.25 ftDistance from the heel to the back face of the abutment walllbetowall := 2ft + 4in = 2.333 ftDistance from center of the bearing pad to the back face of the abutment walllbetowall := 2ft + 4in = 2.333 ftPooting widthBfooting := ltoe + lheel + twall = 11 ftFooting lengthLfooting := Labut + 1ft + 1ft = 65.75 ftNote: The footing extends 1-ft beyond the end of the wall or : sociaf the abutm of the footingh hoeDepth := 7ftStatic footing is are normally set 4 ft below the existing or proposed ground line to avoid fiost heave. The depth of embedment could be decey when pavement sections are over the top of the footing.BDM 7.03.02 ID	he abutment has an independent backwall with a sliding decl	ζ.	BDG 6.20.03A
Backwall hickness $t_{backwall} := 1ft + 6in = 1.5 ft$ Abutment wall height $h_{wall} := 17.54ft$ Abutment wall hickness $t_{wall} := 3ft + 2in = 3.167 ft$ Distance from the too to the front face of the abutment wall $t_{too} := 1ft + 3in = 1.25 ft$ Distance from the heel to the back face of the abutment wall $l_{heel} := 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width $B_{footing} := t_{toe} + t_{heel} + t_{wall} = 11 ft$ Footing length $L_{footing} := L_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on ether side. $t_{footing} := 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ ot: Bottoms of footings are normally set 4 ft below the existing r proposed ground line to avoid frost heave. The depth of embedment could be decerve. when pavement sections are over the top of the footing.BDM 7.03.02 IFPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Backwall height	$h_{backwall} := 4.25 ft$	
Abutment wall height $h_{wall} := 17.54ft$ Abutment wall thickness $t_{wall} := 3ft + 2in = 3.167 ft$ Distance from the toe to the front face of the abutment wall $l_{toe} := 1ft + 3in = 1.25 ft$ Distance from the heel to the back face of the abutment wall $l_{heel} := 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width $B_{footing} := l_{toe} + l_{heel} + t_{wall} = 11 ft$ Footing lengthLfooting := Labut + 1ft + 1ft = 65.75 ftNote: The footing extends 1-ft beyond the end of the wall on either side.Footing thicknessFooting thickness $t_{footing} := 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ Bott: Bottoms of footings are normally set 4 ft below the existing r proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 IFPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Backwall thickness	$t_{backwall} \coloneqq 1ft + 6in = 1.5 ft$	
Abutment wall thickness $t_{wall} := 3ft + 2in = 3.167 ft$ Distance from the toe to the front face of the abutment wall $l_{toe} := 1ft + 3in = 1.25 ft$ Distance from the heel to the back face of the abutment wall $l_{heel} := 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} := 2ft + 4in = 2.333 ft$ Postance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width Footing length $B_{footing} := l_{toe} + l_{heel} + t_{wall} = 11 ft$ Note: The footing extends 1-ft beyond the end of the wall on either side.Footing i:= L_abut + 1ft + 1ft = 65.75 ftNote: The footing extends 1-ft beyond the end of the wall on either side.Footing i:= 3ftToe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ ot: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Abutment wall height	$h_{wall} \coloneqq 17.54 ft$	
Distance from the toe to the front face of the abutment wall $I_{toe} := 1ft + 3in = 1.25 ft$ Distance from the heel to the back face of the abutment wall $I_{heel} := 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $I_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width $B_{footing} := 1_{toe} + 1_{heel} + t_{wall} = 11 ft$ Footing width $B_{footing} := 1_{toe} + 1_{heel} + t_{wall} = 11 ft$ Footing length $L_{footing} := L_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on either side.Footing i:= 3ftToe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ ot:: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 FPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Abutment wall thickness	$t_{wall} := 3ft + 2in = 3.167 ft$	
Distance from the heel to the back face of the abutment wall $l_{heel} \coloneqq 6ft + 7in = 6.583 ft$ Distance from center of the bearing pad to the back face of the abutment wall $l_{brtowall} \coloneqq 2ft + 4in = 2.333 ft$ Footing width $B_{footing} \coloneqq l_{toe} + l_{heel} + t_{wall} = 11 ft$ Footing width $L_{footing} \coloneqq l_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on $\dashv ter side$.Footing thickness $t_{footing} \coloneqq 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} \coloneqq 7ft$ Footing sare normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 FPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Distance from the toe to the front face of the abutment wall	$l_{toe} := 1 ft + 3 in = 1.25 ft$	
Distance from center of the bearing pad to the back face of the abutment wall $I_{brtowall} := 2ft + 4in = 2.333 ft$ Footing width $B_{footing} := I_{toe} + I_{heel} + t_{wall} = 11 ft$ Footing length $L_{footing} := L_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on either side.Footing thicknessFooting thickness $t_{footing} := 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ Toe fill depth to the bottom of the footing.BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Distance from the heel to the back face of the abutment wall	$l_{heel} := 6ft + 7in = 6.583 ft$	
Footing width $B_{footing} \coloneqq l_{toe} + l_{heel} + t_{wall} = 11 \text{ ft}$ Footing length $L_{footing} \coloneqq L_{abut} + 1\text{ ft} + 1\text{ ft} = 65.75 \text{ ft}$ Note: The footing extends 1-ft beyond the end of the wall on either side.Footing thickness $t_{footing} \coloneqq 3\text{ ft}$ Toe fill depth to the bottom of the footing $h_{toeDepth} \coloneqq 7\text{ ft}$ Note: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 FPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Distance from center of the bearing pad to the back face of the abutment wall	$l_{brtowall} := 2ft + 4in = 2.333 ft$	t
Footing length $L_{footing} \coloneqq L_{abut} + 1ft + 1ft = 65.75 ft$ Note: The footing extends 1-ft beyond the end of the wall on either side.Footing thickness $t_{footing} \coloneqq 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} \coloneqq 7ft$ Toe fill depth to the bottom of the footing.BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Footing width	$B_{footing} \coloneqq l_{toe} + l_{heel} + t_{wall}$	= 11 ft
Note: The footing extends 1-ft beyond the end of the wall on either side.Footing thickness $t_{footing} := 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ Note: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Footing length	$L_{footing} := L_{abut} + 1ft + 1ft =$	65.75 ft
Footing thickness $t_{footing} := 3ft$ Toe fill depth to the bottom of the footing $h_{toeDepth} := 7ft$ Jote: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing.BDM 7.03.02 DPassive earth pressure is excluded from the footing design.BDM 7.03.02 F	Note: The footing extends 1-ft beyond the end of the wall on	either side.	
Toe fill depth to the bottom of the footing htoeDepth := 7ft Iote: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing. BDM 7.03.02 D Passive earth pressure is excluded from the footing design. BDM 7.03.02 F	Footing thickness	$t_{footing} := 3ft$	
Jote: Bottoms of footings are normally set 4 ft below the existing or proposed ground line to avoid frost heave. The depth of embedment could be deeper when pavement sections are over the top of the footing. BDM 7.03.02 D Passive earth pressure is excluded from the footing design. BDM 7.03.02 F	Toe fill depth to the bottom of the footing	$h_{toeDepth} := 7ft$	
Passive earth pressure is excluded from the footing design. BDM 7.03.02 F	te: Bottoms of footings are normally set 4 ft below the existing avoid frost heave. The depth of embedment could be deep over the top of the footing.	g or proposed ground line to per when pavement sections are	BDM 7.03.02 D
	Passive earth pressure is excluded from the footing design.		BDM 7.03.02 F

Step 4.2 Application of Dead Load

Description

This step describes the application of the dead load on the abutment.

The common practice is to apply superstructure dead load as a uniformly distributed load over the length of the abutment. This is accomplished by adding exterior and interior girder end dead load reactions and dividing this quantity by the abutment length.

Dead load of superstructure

Weight of structural components and non-structural attachments (DC)

Weight of the future wearing surface (DW)

Backwall weight

Abutment wall weight

Footing weight

$$DC_{Sup} := \frac{2 \cdot R_{DCEx} + (N_{beams} - 2) \cdot R_{DCIn}}{L_{abut}} = 5.658 \cdot \frac{kip}{ft}$$

$$DW_{Sup} := \frac{2 \cdot R_{DWEx} + (N_{beams} - 2) \cdot R_{DWIn}}{L_{abut}} = 0.886 \cdot \frac{kip}{ft}$$

$$DC_{backwall} := h_{backwall} \cdot t_{backwall} \cdot W_{c} = 0.956 \cdot \frac{kip}{ft}$$

$$DC_{wall} := h_{wall} \cdot t_{wall} \cdot W_{c} = 8.332 \cdot \frac{kip}{ft}$$

$$DC_{footing} := B_{footing} \cdot t_{footing} \cdot W_{c} = 4.95 \cdot \frac{kip}{ft}$$

Step 4.3 Application of Live Load

Description

►

Please refer to Step 2.3 for the application of live load on the structure.

Step 4.4 Application of Other Loads

Description

►

This step typically includes the calculation of braking force, wind load, earth load, and temperature load.

Since piles and a pile cap are selected to replace the spread footing in Section 2, all other dimensions of the abutment remain consistent. Only the calculation of the earth load is different from Step 2.4. Therefore, please refer to Step 2.4 for the rest of the calculations.

154

Earth Load

The earth load includes lateral earth pressure, live load surcharge, and vertical earth pressure on the footing. As per the Geotechnical Services Section, the groundwater table is not located in the vicinity of the foundation. Therefore, the effect of hydrostatic pressure is excluded. The hydrostatic pressure should be avoided, if possible, at abutments and retaining walls through the design of an appropriate drainage system.

Lateral Load Due to Lateral Earth Pressure

The lateral loads due to earth pressure are calculated.

Backwall $p_{bw} := k_a \cdot \gamma_s \cdot h_{backwall} = 0.153 \cdot ksf$ LRFD Eq. 3.11.5.1-1 Lateral earth pressure at the base $P_{\text{EHBackwall}} \coloneqq \frac{1}{2} \cdot p_{\text{bw}} \cdot h_{\text{backwall}} = 0.325 \cdot \frac{\text{kip}}{\text{ft}}$ Lateral load Abutment Wall $p_{wall} \coloneqq k_a \cdot \gamma_s \cdot (h_{backwall} + h_{wall}) = 0.784 \cdot ksf$ Lateral earth pressure at the base $P_{EHWall} := \frac{1}{2} \cdot p_{wall} \cdot (h_{backwall} + h_{wall}) = 8.546 \cdot \frac{kip}{ft}$ Lateral load Footing $p_{ff} := k_a \cdot \gamma_s \cdot (h_{backwall} + h_{wall} + t_{footing}) = 0.892 \cdot ksf$ Lateral earth pressure at the base $P_{\text{EHFooting}} \coloneqq \frac{1}{2} \cdot p_{\text{ft}} \cdot \left(h_{\text{backwall}} + h_{\text{wall}} + t_{\text{footing}} \right) = 11.062 \cdot \frac{\text{kip}}{\text{ft}}$ Lateral load Vertical Earth Load on the Footing $EV_{earthBk} := \gamma_s \cdot l_{heel} \cdot (h_{backwall} + h_{wall}) = 17.214 \cdot \frac{kip}{r}$ Back side (heel) $EV_{earthFt} := \gamma_s \cdot l_{toe} \cdot (h_{toeDepth} - t_{footing}) = 0.6 \cdot \frac{kip}{ft}$ Front side (toe) Live Load Surcharge LRFD 3.11.6.4

Live load surcharge is applied to account for a vehicular live load acting on the backfill surface within a distance equal to one-half the wall height behind the back face of the wall.

Height of the abutment	$h_{backwall} + h_{wall} + t_{footing} = 24.7$	79 ft
Equivalent height of soil for vehicular load	$h_{eq} := 2ft$	LRFD Table 3.11.6.4-1
Lateral surcharge pressure	$\sigma_{\mathbf{p}} \coloneqq \mathbf{k}_{\mathbf{a}} \cdot \gamma_{\mathbf{s}} \cdot \mathbf{h}_{\mathbf{eq}} = 0.072 \cdot \mathbf{ksf}$	LRFD Eq. 3.11.6.4-1
Backwall		
Lateral load	$P_{LSBackwall} \coloneqq \sigma_p \cdot h_{backwall} = 0.$	$306 \cdot \frac{\text{kip}}{\text{ft}}$
Abutment Wall	<i>,</i>	kin
Lateral load	$P_{LSWall} := \sigma_p \cdot (h_{backwall} + h_{wall})$	$= 1.569 \cdot \frac{mp}{ft}$
Footing		
Lateral load	$P_{LSFooting} := \sigma_p \cdot (h_{backwall} + h_w)$	$\operatorname{all} + \operatorname{t_{footing}} = 1.785 \cdot \frac{\operatorname{kip}}{\operatorname{ft}}$
Vertical load	$V_{LSFooting} \coloneqq \gamma_s \cdot l_{heel} \cdot h_{eq} = 1.58$	kip ft

Step 4.5 Combined Load Effects

Description

►

This step describes the procedure for combining all load effects and calculating the total factored forces and moments acting at the base of the backwall, abutment wall, and footing.

The total factored forces and moments at the base of the backwall and abutment wall are similar to the ones in Step 2.5. Therefore, this step only shows the calculation of the total factored forces and moments at the base of the footing.

156

Forces and Moments at the Base of the Footing

Load Cases I, III, and IV are considered. In addition to all the loads considered for the abutment wall, weight of soil (earth load) on the toe and heel, along with live load surcharge on the heel, are considered.

LRFD 3.6.2.1

The dynamic load allowance is excluded from the live load for foundation components that are located entirely below the ground level.









Strength I

Strength I = 1.25DC + 1.5DW + 1.75LL + 1.75BR + 1.5EH + 1.35EV + 1.75LS + 0.5TU

Load Case I

Factored vertical force at the base of the footing

$$F_{VFtLC1StrI} := 1.25 \cdot \left(DC_{backwall} + DC_{wall} + DC_{footing} \right) + 1.35 \cdot \left(EV_{earthBk} + EV_{earthFt} \right) = 41.846 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

 $V_{uFtLC1StrI} \coloneqq 1.5 \cdot P_{EHFooting} = 16.593 \cdot \frac{kip}{ft}$

LRFD 3.4.1

The vertical earth load of the backfill soil reduces the critical moment about the footing longitudinal axis. This requires using the minimum load factor of 1.0 for EV instead of the factor 1.35 in the Strength I combination.

This is the same for the moment calculated about the longitudinal axis of the footing for all the load cases and limit states.

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC1StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHFooting} \cdot \frac{(h_{backwall} + h_{wall} + t_{footing})}{3} + 1.35EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \\ &\qquad M_{uFtLC1StrI} = 133.008 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case III

Factored vertical force at the base of the footing

 $F_{VFtLC3StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) + 1.5DW_{Sup} + 1.75R_{LLFootingMax} + 1.35 \cdot (EV_{earthBk} + EV_{earthFt})$

$$F_{VFtLC3StrI} = 59.798 \cdot \frac{k_{IP}}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC3StrI} \coloneqq 1.5 \cdot P_{EHFooting} = 16.593 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} + 1.75 \cdot R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots \\ &+ 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3StrI} = 194.344 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force at the base of the footing

$$F_{VFtLC4StrI} := 1.25 \cdot (DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing}) + 1.5DW_{Sup} \dots + 1.35 \cdot (EV_{earthFt} + EV_{earthBk}) + 1.75V_{LSFooting}$$

 $F_{VFtLC4StrI} = 53.013 \cdot \frac{kip}{ft}$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC4StrI} := 1.5 \cdot P_{EHFooting} + 1.75 P_{LSFooting} + 0.5TU = 19.855 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC4StrI} &\coloneqq 1.25 \cdot DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + 1.25DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(1.25 \cdot DC_{Sup} + 1.5 \cdot DW_{Sup} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.5 \cdot P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} + 1.75V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.75 \cdot P_{LSFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{2} + 1.0 \cdot EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ 1.35 \cdot EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) + 0.5 \cdot TU \cdot \left(h_{wall} + t_{footing} \right) \\ &M_{uFtLC4StrI} = 197.175 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Service I

Service I = 1.0DC + 1.0DW + 1.0LL + 1.0BR + 1.0WS + 1.0WL + 1.0EH + 1.0EV + 1.0LS + 1.0TU

Load Case I

Factored vertical force at the base of the footing

$$F_{VFtLC1SerI} := DC_{backwall} + DC_{wall} + DC_{footing} + EV_{earthBk} + EV_{earthFt} = 32.052 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing
$$V_{uFtLC1SerI} := P_{EHFooting} = 11.062 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} \text{M}_{uFtLC1SerI} &\coloneqq \text{DC}_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + \text{DC}_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots \\ &+ \text{EV}_{earthBk'} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + \text{EV}_{earthFt'} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &\qquad M_{uFtLC1SerI} = 80.288 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}} \end{split}$$

Load Case III

Factored vertical force at the base of the footing

$$F_{VFtLC3SerI} := DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} + R_{LLFootingMax} + (EV_{earthFt} + EV_{earthBk})$$

$$F_{VFtLC3SerI} = 44.053 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

$$V_{uFtLC3SerI} := P_{EHFooting} = 11.062 \cdot \frac{kip}{ft}$$

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC3SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} + R_{LLFootingMax} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) \dots \\ &+ P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing}}{3} \right)}{3} \dots \\ &+ EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \\ &M_{uFtLC3SerI} = 121.293 \cdot \frac{kip \cdot ft}{ft} \end{split}$$

Load Case IV

Factored vertical force at the base of the footing

$$F_{VFtLC4SerI} \coloneqq DC_{Sup} + DC_{backwall} + DC_{wall} + DC_{footing} + DW_{Sup} \dots + EV_{earthFt} + EV_{earthBk} + V_{LSFooting}$$

$$F_{VFtLC4SerI} = 40.176 \cdot \frac{kip}{ft}$$
the
$$V_{uFtLC4SerI} \coloneqq P_{EHFooting} + P_{LSFooting} + TU = 13.124 \cdot \frac{kip}{ft}$$

Factored shear force parallel to the transverse axis of the footing

Factored moment about the longitudinal axis of the footing

$$\begin{split} M_{uFtLC4SerI} &\coloneqq DC_{backwall} \cdot \left(l_{heel} + \frac{t_{backwall}}{2} - \frac{B_{footing}}{2} \right) + DC_{wall} \cdot \left(l_{heel} + \frac{t_{wall}}{2} - \frac{B_{footing}}{2} \right) \dots \\ &+ \left(DC_{Sup} + DW_{Sup} \right) \cdot \left(l_{heel} + l_{brtowall} - \frac{B_{footing}}{2} \right) + P_{EHFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing} \right)}{3} \dots \\ &+ EV_{earthBk} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + EV_{earthFt} \cdot \left(\frac{B_{footing}}{2} - \frac{l_{toe}}{2} \right) \dots \\ &+ V_{LSFooting} \cdot \left(\frac{l_{heel}}{2} - \frac{B_{footing}}{2} \right) + P_{LSFooting} \cdot \frac{\left(\frac{h_{backwall} + h_{wall} + t_{footing} \right)}{2} \dots \\ &+ TU \cdot \left(h_{wall} + t_{footing} \right) \end{split}$$

Summary of Forces and Moments at the Base of the Footing

Factored vertical force, F_{VFt} (kip/ft)

	Strength I	Service I
LC I	41.85	32.05
LC III	59.80	44.05
LC IV	53.01	40.18

Factored shear force parallel to the transverse axis of the footing, $V_{uFt}(\mbox{kip/ft})$

	Strength I	Service I
LC I	16.59	11.06
LC III	16.59	11.06
LC IV	19.85	13.12

Factored moment about the longitudinal axis of the footing, $M_{uFt} \left(kip \, ft/ft \right)$

	Strength I	Service I
LC I	133.01	80.29
LC III	194.34	121.29
LC IV	197.18	126.98

Step 4.6 Pile Size and Layout Design

Description

This step presents the pile type, size, and preliminary layout.

This example uses steel H piles since it is the most commonly used pile type in Michigan. Typically, the pile type is selected after evaluating other possibilities, such as ground improvement techniques, other foundation types, and constructability. Pile embedment into the footing Pile embd := 6inBDM 7.03.09.A5 Note: A tremie seal is not used for this footing. If a tremie seal is used, the pile embedment into the footing is 1 ft. A tremie seal design is given in Appendix 4.A. The following parameters are considered to determine the pile layout: 1. Pile spacing: The depth of commonly used H-piles ranges from 10 to 14 inches. LRFD 10.7.1.2 The minimum pile spacing is controlled by the greater of 30 inches or 2.5 times the pile diameter. As a practice, MDOT uses 3 times the pile diameter as the spacing. Selected pile section HP 12x53 $b_{f} := 12.0in$ $d_{\text{pile}} := 11.8 \text{in}$ $\text{Spacing}_{\min} := 3 \cdot d_{\text{pile}} = 2.95 \text{ ft}$ Minimum spacing $(3d_{nile})$ BDM 7.03.09.A7 2. Edge distance: The usual minimum edge distance for piles is 18 inches. PileEdgeDist := 18in Pile edge distance Use two rows of piles. $N_{MaxPiles} := \frac{L_{footing} - 2 \cdot PileEdgeDist}{Spacing_{min}} = 21.271$ Maximum number of piles in each row the footing can accommodate $S_B := B_{footing} - 2 \cdot PileEdgeDist = 8 ft$ Spacing between two rows The loads acting on the two rows of piles are determined as follows: Load Case III under the Strength I limit state is identified as the governing load case by examining the summary tables presented at the end of Step 4.5. Therefore: $P_{vert} := F_{VFtLC3StrI} \cdot L_{footing} = 3.932 \times 10^3 \cdot kip$ Total vertical force Total moment about the $M_{long} := M_{uFtLC3StrI} L_{footing} = 1.278 \times 10^4 \cdot kip \cdot ft$ longitudinal axis of the footing P В SB R Total vertical loads on each row of piles are calculated based on static equilibrium. $R_{rv} := \frac{\left(\frac{M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_D}}{= 3.563 \times 10^3 \cdot kip} \qquad R_B := P_{vert} - R_{rv} = 368.598 \cdot kip$

Selected batter for the front row piles	3V:1H	BDM 7.03.09.A9
	$Pile_{batter} := \frac{3}{1}$	
Total axial load on the front row piles	$R_{r} := R_{rv} \cdot \frac{\sqrt{Pile_{batter}^{2}} + \frac{1}{Pile_{batter}}}{Pile_{batter}}$	$\frac{1^2}{1} = 3.756 \times 10^3 \cdot \text{kip}$
Consult the Geotechnical Services Section to s selected section.	elect a nominal pile resistance fo	r the BDM 7.03.09.B
Nominal pile resistance	$R_n := 350 kip$	
Assume that the Nominal Pile Driving Resistar Formula, and no PDA test or static load tests ar	nce (R _{ndr}) is verified using the FF e performed.	IWA-modified Gates Dynamic
The resistance factor for driven piles	$\varphi_{dyn} \coloneqq 0.5$	BDM 7.03.09.B2
Factored nominal pile resistance	$\mathbf{R}_{\mathbf{R}} \coloneqq \boldsymbol{\varphi}_{dyn} \cdot \mathbf{R}_{n} = 175 \cdot \mathbf{k} \mathbf{i}$	p
Required number of piles in the front row	$n_{\text{front}_{\text{required}}} := \frac{R_{\text{r}}}{R_{\text{R}}} =$	21.462 N _{MaxPiles} = 21.271
Check if the required number of piles in the front row exceeds the maximum number of piles the footing can accommodate	Check := if (n _{front_} required <	< N _{MaxPiles} , "OK", "Not OK") = "Not OK"
If the required number of piles in the front row accommodated within the selected footing dim	is greater than the maximum nu ensions, consider a larger pile se	mber of piles that can be ection.
Selected pile section	HP 14X73 $b_f := 14.5$	85in $d_{pile} \approx 13.61in$
Consult the Geotechnical Services Section to s section.	elect a nominal pile resistance fo	r the selected BDM 7.03.09.B
Nominal pile resistance	$R_n := 500 kip$	BDM 7.03.09.B
Factored nominal pile resistance	$R_R := \varphi_{dyn} \cdot R_n = 250 \cdot ki$	p
Required number of piles in the front row	$n_{\text{front}} \coloneqq \frac{R_{\text{r}}}{R_{\text{R}}} = 15.023$	
	$n_{front} := trunc(n_{front}) +$	1 = 16
Pile spacing	spacing := $\frac{\left(L_{\text{footing}} - 2\right)}{n_{\text{from}}}$	$\frac{\text{PileEdgeDist}}{\text{nt} - 1} = 50.2 \cdot \text{in}$
Number of pile selected for the front row	$N_{front} \coloneqq 16$	
Selected pile spacing	FrontPileSpacing := 50in	
Select 16 front row piles spaced at 4 ft-2 in., m	ax = 62 ft 9 in.	

Check if the spacing of the piles is greater than $3d_{pile}$

Piles in the Back Row

Number of pile selected for the back row

Selected pile spacing

Select 7 back row piles spaced at 10 ft 5.5 in.

Note: As per the AASHTO LRFD Article 10.7.5, the effects of corrosion and deterioration from environmental conditions shall be considered in the selection of the pile type and cross-section. The soil conditions should be examined to ensure that there is no indication of contamination that would cause piles to corrode. Consult the Geotechnical Services Section to determine a suitable pile type and cross-section for the selected site.

BackPileSpacing := $10ft + 5.5in = 125.5 \cdot in$

N_{back} :=

The preliminary pile layout is shown in the following figure.





Step 4.7 Pile Capacity Check

Description

This step presents the pile axial and lateral load calculations along with pile capacity checks.

Strength I Limit State

Load Case I

Total vertical load	$P_{vert} := F_{VFtLC1StrI} \cdot L_{footing} = 2.751 \times 10^3 \cdot kip$
Total shear force parallel to the transverse axis of the footing	$P_{lat} := V_{uFtLC1StrI} \cdot L_{footing} = 1.091 \times 10^3 \cdot kip$
Total moment about the longitudinal axis of the footing	$M_{long} := M_{uFtLC1StrI}L_{footing} = 8.745 \times 10^3 \cdot kip \cdot ft$

The total vertical loads on the front and back row of piles are calculated based on the static equilibrium of the footing.

$$R_{rv} := \frac{\left(M_{long} + P_{vert} \cdot \frac{S_B}{2}\right)}{S_B} = 2.469 \times 10^3 \cdot kip \qquad R_B := P_{vert} - R_{rv} = 282.533 \cdot kip$$

Vertical component of the axial force on a front row battered pile

1

$$R_{rv}SingleLC1StrI := \frac{R_{rv}}{n_{front}} = 154.304 \cdot kip$$

ъ

$$R_{r_SingleLC1StrI} := R_{rv_SingleLC1StrI} \cdot \frac{\sqrt{Pile_{batter}^{2} + 1^{2}}}{Pile_{batter}} = 162.65 \cdot kip$$

Pile section selected in Step 4.6

Axial force on a front row

battered pile

Factored nominal pile resistance

Check if R_R>Axial force

Horizontal component of the axial force on a front row battered pile

Total lateral force resisted by the battered piles (i.e. the horizontal component of the axial force)

The required lateral load resistance

of a pile

HP 14x73

 $R_R = 250 \cdot kip$

Check := if
$$(R_R > R_r_SingleLC1StrI, "OK", "Not OK") = "OK"$$

 $R_{rh_SingleLC1StrI} := \frac{R_r_SingleLC1StrI}{\sqrt{Pile_{batter}^2 + 1^2}} = 51.435 \cdot kip$

 $P_{HBatteredPiles} := R_{rh} SingleLC1StrI^{n} front = 822.952 \cdot kip$

Check if the lateral load capacity of the battered piles is greater than the lateral load demand

BDM 7.03.09.A.11

Check := $if(P_{HBatteredPiles} > P_{lat}, "Yes", "No, check if the vertical piles can resist the remaining later load")$

Check = "No, check if the vertical piles can resist the remaining later load"

Note: Per MDOT practice, the typical lateral resistance of a vertical pile is 12 kips. A pile bending (p-y) analysis may be performed by incorporating soil-pile interaction to determine the more accurate lateral load resistance of the piles. Consult the Geotechnical Services Section for more information.

$$P_{latReqd_LC1StrI} \coloneqq \frac{\left(P_{lat} - P_{HBatteredPiles}\right)}{\left(N_{front} + N_{back}\right)} = 11.653 \cdot kip$$

Lateral load resistance of a pile (from the Geotechnical Services Section)

Check if the lateral load resistance > the required lateral load resistance

Vertical force on a back row pile

Check if $R_R > Axial$ force

Load Case III

Total vertical load

Total shear force parallel to the transverse axis of the footing

Vertical component of the axial force on a front row battered pile

Axial force on a front row

Check if R_R>Axial force

Horizontal component of the axial force on a front row battered pile

battered pile

Total moment about the longitudinal axis of the footing

The total vertical loads on the front and back row of piles are calculated based on static equilibrium of the footing.

 $P_{latProvided} := 12kip$

 $R_{B_SingleLC1StrI} := \frac{R_B}{N_{hack}} = 40.362 \cdot kip$

 $P_{vert} \coloneqq F_{VFtLC3StrI} \cdot L_{footing} = 3.932 \times 10^3 \cdot kip$

 $P_{lat} := V_{uFtLC3StrI} \cdot L_{footing} = 1.091 \times 10^{3} \cdot kip$

 $M_{long} := M_{uFtLC3StrI}L_{footing} = 1.278 \times 10^4 \cdot kip \cdot ft$

$$R_{\rm rv} := \frac{\left(\frac{M_{\rm long} + P_{\rm vert} \cdot \frac{S_{\rm B}}{2}\right)}{S_{\rm B}} = 3.563 \times 10^3 \cdot \rm kip$$

$$R_B := P_{vert} - R_{rv} = 368.598 \cdot kip$$

Check := $if(P_{latProvided} > P_{latReqd_LC1StrI}, "OK", "Not OK") = "OK"$

Check := if $(R_R > R_B \text{ SingleLC1Str1}, "OK", "Not OK") = "OK"$

$$R_{rv}SingleLC3StrI := \frac{R_{rv}}{n_{front}} = 222.695 \cdot kip$$

$$R_{r}SingleLC3StrI := R_{rv}SingleLC3StrI \cdot \frac{\sqrt{Pile_{batter}^{2} + 1^{2}}}{Pile_{batter}} = 234.741 \cdot kip$$

$$Check := if(R_{R} > R_{r}SingleLC3StrI, "OK", "Not OK") = "OK"$$

$$R_{rh}SingleLC3StrI := \frac{R_{r}SingleLC3StrI}{\sqrt{Pile_{batter}^{2} + 1^{2}}} = 74.232 \cdot kip$$

$$P_{\text{HBatteredPiles}} \coloneqq R_{\text{rh}}_{\text{SingleLC3StrI}} \cdot n_{\text{front}} = 1.188 \times 10^3 \cdot \text{kip}$$

Check if the lateral load capacity of the battered piles is greater than the lateral load demand**BDM 7.03.09.A.11**Check := if
$$(P_{HBatteredPiles} > P_{lat}, "Yes", "No, check if the vertical piles can resist the remaining later load") = "Yes"The required lateral load resistanceof a pile $P_{latReqd_LC3StrI} := 0$ Vertical force on a back row pile $R_{B_SingleLC3StrI} := \frac{R_B}{N_{back}} = 52.657 \cdot kip$ Check if $R_R > Axial$ force $Check := if (R_R > R_B_SingleLC3StrI, "OK", "Not OK") = "OK"$$$

DDM 7 02 00 A 11

Load Case IV

Total vertical load	$P_{vert} := F_{VFtLC4StrI} \cdot L_{footing} = 3.486 \times 10^3 \cdot kip$
Total shear force parallel to the transverse axis of the footing	$P_{lat} := V_{uFtLC4StrI} \cdot L_{footing} = 1.305 \times 10^3 \cdot kip$
Total moment about the longitudinal axis of the footing	$M_{long} := M_{uFtLC4StrI}L_{footing} = 1.296 \times 10^4 \cdot kip \cdot ft$

The total vertical loads on the front and back row of piles are calculated based the static equilibrium of the footing.

$$R_{rv} := \frac{\left(\frac{M_{long} + P_{vert} \cdot \frac{\sigma_B}{2}\right)}{S_B}}{= 3.363 \times 10^3 \cdot kip} \qquad R_B := P_{vert} - R_{rv} = 122.275 \cdot kip$$

Sp)

Vertical component of the axial force on a front row battered pile

Axial force on a front row

Check if R_R>Axial force

Horizontal component of the axial force on a front row battered pile

Total lateral force resisted by

the battered piles

battered pile

1

$$R_{rv}_{SingleLC4StrI} := \frac{R_{rv}}{n_{front}} = 210.209 \cdot kip$$

$$R_{r_SingleLC4StrI} := R_{rv_SingleLC4StrI} \cdot \frac{\sqrt{Pile_{batter}^{2} + 1^{2}}}{Pile_{batter}} = 221.58 \cdot kip$$

Check := if
$$(R_R > R_r \text{ SingleLC4StrI}, "OK", "Not OK") = "OK"$$

$$R_{rh_SingleLC4StrI} := \frac{R_{r_SingleLC4StrI}}{\sqrt{Pile_{batter}^{2} + 1^{2}}} = 70.07 \cdot kip$$

$$P_{HBatteredPiles} := R_{rh_SingleLC4StrI} \cdot n_{front} = 1.121 \times 10^3 \cdot kip$$

Check if the lateral load capacity of the battered piles is greater than the lateral load demand BDM 7.03.09.A.11

Check := if
$$(P_{HBatteredPiles} > P_{lat}, "Yes", "No, check if the vertical piles can resist the remaining later load")$$

Check = "No, check if the vertical piles can resist the remaining later load"

The required lateral load resistance of a pile

Lateral load resistance of a pile (from the Geotechnical Services Section)

Check if the lateral load resistance > the required lateral load resistance

Vertical force on a back row pile

Check if R_R>Axial force

$$P_{latReqd_LC4StrI} := \frac{(P_{lat} - P_{HBatteredPiles})}{(N_{front} + N_{back})} = 8.015 \cdot kip$$

 $P_{latProvided} = 12 \cdot kip$

Check := if
$$(P_{latProvided} > P_{latReqd LC1StrI}, "OK", "Not OK") = "OK"$$

$$R_{B_SingleLC4StrI} \coloneqq \frac{R_B}{N_{back}} = 17.468 \cdot kip$$

Check := $if(R_R > R_B_{SingleLC4StrI}, "OK", "Not OK") = "OK"$

Summary of Forces Acting on a Single Pile

A summary of forces acting on a single pile under different Strength I limit state load cases is listed in the following tables. The pile penetration depth design, driveability analysis, and settlement analysis are performed by the Geotechnical Services Section to evaluate the adequacy of the selected design.

Axial force on a battered pile in the front row (kip)

Axial force on a pile in the back row (kip)

	Strength I
LC I	162.65
LC III	234.74
LC IV	221.58

	Strength I
LC I	40.36
LC III	52.66
LC IV	17.47

Required lateral force resistance of a pile (kip)

	Strength I
LC I	11.65
LC III	0.00
LC IV	8.02

Step 4.8 Backwall Design

Description

Since the backwall forces and moments used in Step 2.7 are not impacted by the use of piles, please refer to the design calculations and details presented in Step 2.7.

Step 4.9 Abutment Wall Design

Description

Since the abutment wall forces and moments used in Step 2.8 are not impacted by the use of piles, please refer to the design calculations and details presented in Step 2.8.

Step 4.10 Structural Design of the Footing

Description

This step presents the structural design of the abutment footing.

Page	Contents
174	Design for Flexure
178	Design for Shear
181	Development Length of Reinforcement
181	Shrinkage and Temperature Reinforcement

Note: In this example, the length of the footing and the abutment wall are 65.75 ft and 63.75 ft, respectively. Since the cantilevered length of the footing in the longitudinal direction is limited to 1 ft on each side, the shear and moment acting on the footing in the longitudinal direction are small and do not require flexural and shear designs.

Design for Flexure

In a typical spread footing, the critical section for flexure, due to the loads acting on the toe, is at the front face of the wall. As shown below, since the front row piles are located behind the critical section, the flexural capacity of the pile cap is not evaluated.

For the heel of the footing, the critical section is located at the back face of the wall. The footing is designed considering the flexural demand at this section since the back row of piles is located closer to the edge of the heel.



As per the summary tables presented at the end of Step 4.7, the maximum and minimum Strength I limit state axial forces at the back row piles are from LC III and LC IV, respectively.

The maximum total axial load on the back row piles	$R_{backMax} := R_{B_{singleLC3StrI} \cdot N_{back}} = 368.598 \cdot kip$
The minimum total axial load on the back row piles	$R_{backMin} := R_{B_SingleLC4StrI} \cdot N_{back} = 122.275 \cdot kip$
Distance from center of the pile to the critical section	$d_{arm} := l_{heel} - PileEdgeDist = 5.083 ft$

Bottom of the footing stresses at the critical section

The tension at the bottom of the footing is developed due to the axial forces at the back row piles. The self-weight of the footing and the vertical earth load on the heel develop the resisting moment. For a safe design, the maximum axial load at the back row piles is used with the minimum load factors for the resisting forces.

The minimum load factors for dead load and earth load are 0.9 and 1.0, respectively.

LRFD Table 3.4.1-2

The maximum moment at the critical section to develop tension at the bottom of the footing

$$M_{rb} := \frac{R_{backMax} \cdot d_{arm}}{L_{footing}} - 0.9W_{c} \cdot t_{footing} \cdot \frac{l_{heel}^{2}}{2} - EV_{earthBk} \cdot \frac{l_{heel}}{2} = -36.942 \cdot \frac{kip \cdot ft}{ft}$$

The negative moment does not require a design for the flexural reinforcement at the bottom of the footing.

Top of the footing stresses at the critical section

Load case IV under the Strength I limit state develops the minimum axial force at the back row piles. The same load case develops the maximum vertical downward loads on the heel due to self weight of the footing, vertical earth load, and live load surcharge.

The maximum moment at the critical section to develop tension at the top of the footing

$$M_{rt} := 1.25W_{c} \cdot t_{footing} \cdot \frac{l_{heel}^{2}}{2} + 1.35EV_{earthBk} \cdot \frac{l_{heel}}{2} + 1.75V_{LSFooting} \cdot \frac{l_{heel}}{2} - \frac{R_{backMin} \cdot d_{arm}}{L_{footing}} = 88.333 \cdot \frac{kip \cdot ft}{ft}$$

Flexure Resistance

LRFD 5.6.3.2

The design procedure consists of calculating the reinforcing steel area required to satisfy the moment demand and checking the selected steel area against the requirements and limitations for developing an adequate moment capacity, controlling crack width, and managing shrinkage and temperature stresses.

Select a trial bar size	bar := 8	
Nominal diameter of a reinforcing steel bar	$d_{\text{bar}} := \text{Dia}(\text{bar}) = 1 \cdot \text{in}$	
Cross-section area of a reinforcing steel bar on the flexural tension side	$A_{\text{bar}} := \text{Area}(\text{bar}) = 0.79 \cdot \text{in}^2$	
The spacing of the main reinforcing steel bars in walls and lesser of 1.5 times the thickness of the member or 18 in.	d slabs shall not be greater than the	LRFD 5.10.3.2
The spacing of shrinkage and temperature reinforcement 12 in. for walls and footings greater than 18 in.	shall not exceed the following:	LRFD 5.10.6
Note: MDOT limits reinforcement spacing to a maximum	n of 18 in.	BDG 5.16.01 and 5.22.01
Footing thickness	$t_{footing} = 3 ft$	
Select a spacing for reinforcing steel bars	$s_{bar} := 12 \cdot in$	
Select a 1-ft wide strip for the design.		
Area of tension steel provided in a 1-ft wide strip	$A_{sProvided} := \frac{A_{bar} \cdot 12in}{s_{bar}} = 0.79$	$2 \cdot \ln^2$
Effective depth	$d_e := t_{footing} - Cover_{ft} = 32 \cdot in$	
Resistance factor for flexure	$\phi_{f} \coloneqq 0.9$	LRFD 5.5.4.2
Width of the compression face of the section	b := 12in	
Stress block factor $\beta_1 := \min \left[\begin{array}{c} \beta_1 \\ \beta_1$	$\max\left[0.85 - 0.05 \cdot \left(\frac{f_c - 4ksi}{ksi}\right), 0.6\right]$	[5], 0.85 = 0.85 LRFD 5.6.2.2
Solve the following equation of A_s to calculate the require assumed initial A value to solve the equation.	ed area of steel to satisfy the moment of	lemand. Use an

١S

 $A_s := 1in^2$ The initial assumption for A_s

176

$$\begin{array}{ll} \mbox{Given} & M_{rt} \cdot ft = \varphi_{f} \cdot A_{s} \cdot f_{y} \cdot \left[d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) \right] \\ \mbox{Required steel area} & A_{sRequired} \coloneqq Find(A_{s}) = 0.625 \cdot in^{2} \\ \mbox{Check if } A_{sProvided} > A_{sRequired} & Check := if(A_{sProvided} > A_{sRequired}, "OK", "Not OK") = "OK" \\ \mbox{Moment capacity of the section} & M_{Provided} \coloneqq \varphi_{f} \cdot A_{sProvided}, fy \cdot \left[\frac{d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) \right]}{ft} \\ \mbox{Moment capacity of the section} & M_{Provided} \coloneqq \varphi_{f} \cdot A_{sProvided}, fy \cdot \left[\frac{d_{e} - \frac{1}{2} \cdot \left(\frac{A_{s} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} \right) \right]}{ft} \\ \mbox{Distance from the extreme compression} & c \coloneqq \frac{A_{s} \cdot Provided}{0.85 \cdot f_{c} \cdot \beta_{1} \cdot b} = 1.82 \cdot in \\ \mbox{Check the validity of the assumption, } f_{s} = f_{y} & Check_{f} \cdot f_{s} \coloneqq if\left(\frac{c}{d_{e}} < 0.6, "OK", "Not OK" \right) = "OK" \\ \end{array}$$

Limits for Reinforcement

The tensile reinforcement provided must be adequate to develop a factored flexural resistance at least equal to the lesser of the cracking moment or 1.33 times the factored moment from the applicable strength limit state load combinations.

Flexural cracking variability factor	$\gamma_1 := 1.6$ For concrete structures that are not precast segmental
Ratio of specified minimum yield strength to ultimate tensile strength of the nonprestressed reinforcement	$\gamma_3 := 0.67$ For ASTM A615 Grade 60 reinforcement
Section modulus	$S_{c} := \frac{1}{6} \cdot b \cdot t_{footing}^{2} = 2.592 \times 10^{3} \cdot in^{3}$
Cracking moment	$M_{cr} := \frac{\gamma_3 \cdot \gamma_1 \cdot f_r \cdot S_c}{ft} = 96.254 \cdot \frac{kip \cdot ft}{ft}$
1.33 times the factored moment demand	$1.33 \cdot M_{rt} = 117.482 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$
Required moment to satisfy the minimum reinforcement requirement	$M_{req} := \min(1.33M_{rt}, M_{cr}) = 96.254 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$
Check the adequacy of section capacity	Check := if $(M_{Provided} > M_{reg}, "OK", "Not OK") = "OK"$

Control of Cracking by Distribution of Reinforcement

Limiting the width of expected cracks under service conditions extends the service life. The width of potential cracks can be minimized through proper placement of the reinforcement. Checking for crack control assures that the actual stress in the reinforcement should not exceed the service limit state stress.

LRFD 5.6.3.3

LRFD 5.6.7

The spacing requirement for the mild steel reinforcement in the layer closest to the tension face

Exposure factor for the Class 1 exposure condition

Distance from extreme tension fiber to the center of the closest bar

Ratio of flexural strain at the extreme tension face to the strain at the centroid of the reinforcement layer closest to the tension face $s \leq \frac{700 \cdot \gamma_e}{\beta_s \cdot f_{ss}} - 2 \cdot d_c$

LRFD Eq. 5.6.7-1

 $\gamma_e := 1.00$

 $d_c := Cover_{ft} = 4 \cdot in$

 $\beta_{\rm S} \coloneqq 1 + \frac{\rm d_c}{0.7 \left(t_{footing} - \rm d_c\right)} = 1.179$

The calculation of tensile stress in nonprestressed reinforcement at the service limit state, f_{ss} , requires establishing the neutral axis location and the moment demand at the critical section.

The position of the cross-section's neutral axis is determined through an iterative process to calculate the actual stress in the reinforcement. This process starts with an assumed position of the neutral axis as shown below.

Assumed distance from the extreme compression fiber to the neutral axis

Given
$$\frac{1}{2} \cdot b \cdot x^2 = \frac{E_s}{E_c} \cdot A_{sProvided} \cdot (d_e - x)$$

 $x_{na} := Find(x) = 5.303 \cdot in$

Position of the neutral axis

The axial force in the back row piles (R_B) from Load Case IV under the Service I limit state is calculated as shown below.

Total vertical load	$P_{vert} := F_{VFtLC4SerI} \cdot L_{footing} = 2.642 \times 10^3 \cdot kip$
Total shear force parallel to the transverse axis of the footing	$P_{lat} := V_{uFtLC4SerI} \cdot L_{footing} = 862.914 \cdot kip$
Total moment about the longitudinal axis of the footing	$M_{long} := M_{uFtLC4SerI}L_{footing} = 8.349 \times 10^3 \cdot kip \cdot ft$

The total vertical loads on the front and back row of piles are calculated based on static equilibrium of the footing.

$$R_{rv} := \frac{\left(\frac{M_{long} + P_{vert} \cdot \frac{S_B}{2}}{S_B}\right)}{S_B} = 2.364 \times 10^3 \cdot kip \qquad R_B := P_{vert} - R_{rv} = 277.156 \cdot kip$$

The moment at the critical section under Service I limit state that generates tension at the top of the footing is:

$$M_{\text{heelTopSerI}} \coloneqq W_{\text{c}} \cdot t_{\text{footing}} \cdot \frac{l_{\text{heel}}^2}{2} + \text{EV}_{\text{earthBk}} \cdot \frac{l_{\text{heel}}}{2} + \text{V}_{\text{LSFooting}} \cdot \frac{l_{\text{heel}}}{2} - \frac{R_{\text{B}} \cdot d_{\text{arm}}}{L_{\text{footing}}} = 50.188 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$$
Tensile force in the reinforcing steel due
to the Service I limit state moment}
$$T_{\text{s}} \coloneqq \frac{M_{\text{heelTopSerI}}}{d_{\text{e}} - \frac{x_{\text{na}}}{3}} \cdot \text{ft} = 19.9 \cdot \text{kip}$$

Stress in the reinforcing steel due to the Service I limit state moment

 f_{ss} (not to exceed 0.6 f_{v})

$$f_{ss1} := \frac{T_s}{A_{sProvided}} = 25.216 \cdot ksi$$

$$f_{ss} := \min(f_{ss1}, 0.6f_v) = 25.216 \cdot ksi$$

 $bar_{spaReq} \coloneqq \frac{700 \cdot \gamma_e \cdot \frac{kip}{in}}{\beta_e \cdot f_{ee}} - 2 \cdot d_e = 15.554 \cdot in$

Check := if(s_{bar} < bar_{spaReq}, "OK", "Not OK") = "OK"

Required reinforcement spacing

Check if the spacing provided < the required spacing

Shrinkage and Temperature Reinforcement

LRFD 5.10.6

The following calculations check the adequacy of the flexural reinforcing steel to control shrinkage and temperature stresses in the heel:



Design for Shear

Shear design in abutment footings supported by piles provides adequate resistance against one-way action (beam action shear) and two-way action (punching shear). For both one-way and two-way actions, the design shear is taken at the critical section. For abutment footings, one-way action is checked at the toe and heel. The factored shear force at the critical section is computed by cutting the footing at the critical section and taking the summation of the pile loads or portions of pile loads that are outside the critical section. Two-way action in abutment footings supported by piles is generally checked by taking a critical perimeter around individual piles or around a group of piles when the critical perimeter of individual piles overlap.

One-way Shear

For one-way shear on the toe side, a shear check at the critical section or towards the toe is not required since the front row of piles is inside the critical section.

On the heel side, the downward load is larger than the upward axial force at the back row pile. Therefore, the top of the heel is in tension. As a result, the critical section for shear is taken at the back face of the abutment wall.

LRFD C5.12.8.6.1

Effective width of the section	$b = 12 \cdot in$
Provided flexural reinforcement area	$A_{sProvided} = 0.79 \cdot in^2$

Check if $l_{heel} < 3d_v$

Effective shear depth

Therefore, the simplified procedure is used.

Depth of equivalent rectangular stress block

The factored shear demand at the critical section for shear:

Factor indicating the ability of diagonally cracked concrete to transmit tension and shear

Nominal shear resistance of concrete, V_n, is calculated as follows:

 $b_{f} := 14.585 in$ $d_{pile} := 13.61 in$ The loads on the front piles are assumed to be identical. The critical case for a two-way shear is the piles at the end of the front row since the critical perimeter of these piles may be off the footing in both directions.

HP 14x73

$V_{-1} := 0.0316 \cdot \beta \cdot \sqrt{f_{-1} \cdot k_{si}} \cdot b \cdot d_{-1} = 42 \cdot k_{si} \cdot b \cdot d_{-1} = 42 \cdot k_{si}$

Resistance factor for shear

Factored shear resistance

Check if the factored shear resistance > the shear demand

Two-way Shear

For two-way shear, the critical perimeter of a pile, b_0 , is located at a minimum of $0.5d_v$ from the perimeter of the pile. If portions of the critical perimeter are located off the footing, that portion of the critical perimeter is limited by the footing edge.

Pile section selected in Step 4.6

Flange width and depth of the pile

 $\beta := 2$

 $V_r := \phi_V \cdot V_n = 37.831 \cdot kip$

 $a := \frac{A_{sProvided} \cdot f_{y}}{0.85 \cdot f_{c} \cdot b} = 1.549 \cdot in$

$$V_{uFtHeel} := 1.25 \cdot W_c \cdot t_{footing} \cdot l_{heel} + 1.35EV_{earthBk} + 1.75V_{LSFooting} - \frac{R_{backMin}}{L_{footing}} = 27.847 \cdot \frac{kip}{ft}$$

For a concrete footing in which the distance from point of zero shear to the face of the LRFD 5.7.3.4.1

 $d_{V} := \max\left(d_{e} - \frac{a}{2}, 0.9 \cdot d_{e}, 0.72 \cdot t_{footing}\right) = 31.225 \cdot in$ **LRFD** 5.7.2.8

LRFD 5.7.3.4.1

LRFD 5.12.8.6.3

wall is less than
$$3d_v$$
, the simplified procedure for nonprestressed sections can be used.
Check if $l_{heel} < 3d_v$, "Yes", "No") = "Y

$$V_{c2} := 0.25 f_{c} \cdot b \cdot d_{e} = 288 \cdot kip$$

$$V_{n} := \min(V_{c1}, V_{c2}) = 42.035 \cdot kip$$

$$\Phi_{v} := 0.9$$
LRFD 5.5.4.2

Check := if
$$\left(\frac{V_r}{ft} > V_{uFtHeel}, "OK", "Not OK"\right) = "OK"$$

heck :=
$$if(l_{heel} < 3 \cdot d_V, "Yes", "No") = "Yes"$$

Check if the critical perimeter is off the footing in the footing width direction

Check if the critical perimeter is off the footing in the footing length direction

Length of the critical perimeter side parallel to the footing width direction

Length of the critical perimeter side parallel to the footing length direction

Critical perimeter

Ratio of long side to short side of the rectangle through which the concentrated load is transmitted

Nominal shear resistance

$b_0 := (b_{01} + b_{02}) = 6.777$ $\beta_{c} := \frac{b_{f}}{d_{\text{pile}}} = 1.072$ $V_{n1}_{way} := \left(0.063 + \frac{0.126}{\beta_c}\right) \cdot \sqrt{f_c \cdot ksi} \cdot b_0 \cdot d_v = 794.229 \cdot kip$ LRFD Eq. V_{n2} 2way := $0.126 \cdot \left(\sqrt{f_c \cdot ksi} \cdot b_0 \cdot d_v \right) = 554.184 \cdot kip$ 5.12.8.6.3-1 $V_{n 2way} := \min(V_{n1 2way}, V_{n2 2way}) = 554.184 \cdot kip$

 $V_{r 2way} := \phi_V V_{n 2way} = 498.765 \cdot kip$

Factored shear resistance

According to the summary tables of the pile axial forces, LC III under the Strength I limit state developed the maximum pile axial force at the front row piles.

OffFooting1 := if $\left(\frac{d_{pile}}{2} + \frac{d_{v}}{2} > PileEdgeDist, "Yes", "No"\right)$

OffFooting1 = "Yes"

OffFooting2 := if
$$\left(\frac{b_f}{2} + \frac{d_v}{2} > PileEdgeDist, "Yes", "No" \right)$$

OffFooting2 = "Yes"

$$b_{01} := if \left(OffFooting1 = "Yes", \frac{d_{pile}}{2} + \frac{d_{V}}{2} + PileEdgeDist, d_{pile} + d_{V} \right)$$
$$b_{01} = 3.368 \text{ ft}$$
$$b_{02} := if \left(OffFooting2 = "Yes", \frac{b_{f}}{2} + \frac{d_{V}}{2} + PileEdgeDist, b_{f} + d_{V} \right)$$

$$b_{02} = 3.409 \text{ ft}$$

 $b_0 := (b_{01} + b_{02}) = 6.777 \text{ ft}$
Maximum two-way shear demand Check if the factored shear resistance > the maximum rile axial forma	$R_{r_SingleLC3StrI} = 234.741 \cdot kip$ Check := if (V _r 2 _{way} > R _r SingleI C3StrI, "OK", "Not OK") = "OK"				
Development Length of Reinforcement					
The flexural reinforcing steel must be developed of full development length.	on each side of the critical section for its LRFD 5.10.8.1.2				
Available development length	$l_{d.available} := l_{heel} - Cover_{ft} = 6.25 \text{ ft}$				
Basic development length	$l_{db} := 2.4 \cdot d_{bar} \cdot \frac{f_y}{\sqrt{f_c \cdot ksi}} = 6.928 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-2				
Reinforcement location factor	$\lambda_{rl} := 1.3$ More than 12 in. concrete below				
Coating factor	$\lambda_{cf} := 1.5$ Epoxy coated bars with less than $3d_b$ cover				
Reinforcement confinement factor	$\lambda_{rc} := 0.4$ For $C_b > 2.5$ in. and No. 8 bars or smaller				
Excess reinforcement factor	$\lambda_{\text{er}} := \frac{A_{\text{sRequired}}}{A_{\text{sProvided}}} = 0.792$ LRFD Eq. 5.10.8.2.1c-4				
Factor for normal weight concrete	$\lambda := 1$				
Required development length	$l_{d.required} \coloneqq l_{db} \cdot \frac{(\lambda_{rl} \cdot \lambda_{cf} \cdot \lambda_{rc} \cdot \lambda_{er})}{\lambda} = 4.278 \text{ ft}$ LRFD Eq. 5.10.8.2.1a-1				
Check if $l_{d.available} > l_{d.required}$	Check := if $(l_{d.available} > l_{d.required}, "OK", "Not OK") = "OK"$				

Shrinkage and Temperature Reinforcement

The following calculations check the required amount of reinforcing steel in the secondary direction to control shrinkage and temperature stresses in the footing.

The reinforcement along the longitudinal direction of the footing at the top and bottom should satisfy the shrinkage and temperature reinforcement requirement.		LRFD 5.10.6
The spacing of reinforcement shall not exceed 12 in. since the footing thickness is greater than 18 in.		LRFD 5.10.6
Note: MDOT practice is to use 18 in. as the maximum spacing.		BDG 5.16.01
Select a trial bar size	bar := 6	
Nominal diameter of a reinforcing steel bar	$d_{bST} := Dia(bar) = 0.75 \cdot in$	
Cross-section area of a bar on the flexural tension side	$A_{barST} := Area(bar) = 0.44 \cdot in^2$	

Select a spacing for reinforcing steel bars

Provided horizontal reinforcement area

Required minimum area of shrinkage and temperature reinforcement in the the footing

Check if the area of steel provided > the required area of shrinkage and temperature steel

$$s_{barST} := 12 \cdot in$$

$$A_{sProvidedST} := \frac{A_{barST} \cdot 12in}{s_{barST}} = 0.44 \cdot in^{2}$$

$$A_{shrink.temp} = 0.306 \cdot in^{2}$$
Check := if(A_{sProvidedST} > A_{shrink.temp}, "OK", "Not OK") = "OK"

The footing design presented in this step provides the following details:

- No. 8 bars @ 12.0 in. spacing ($A_s = 0.79$ in.²/ft) as the transverse flexural reinforcement at the top of the footing
- No. 6 bars @ 12.0 in. spacing ($A_s = 0.44$ in.²/ft) as the transverse shrinkage and temperature reinforcement at the bottom of the footing
- No. 6 bars @ 12.0 in. spacing ($A_s = 0.44 \text{ in.}^2/\text{ft}$) as the longitudinal shrinkage and temperature reinforcement at the top and bottom of the footing.



Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.

Appendix 4.A Tremie Seal Design

Description

This appendix presents the design of a tremie seal.

sed	
isions:	
$\underline{-\text{embd}} = 5.167 \text{ft}$	
- 5.107 10	
$(1 \mathrm{ft}) = 6 \mathrm{ft}$	
$ect_{toe} = 18.5 ft$	
$h_{\text{tremie}} = 11.008 \cdot \text{kip}$	
	185

BDM 7.03.06

BDM 7.03.06A

Unit weight of tremie concrete
$$\gamma_{tremie} := 140 \frac{1}{ft^3}$$
Consider a 1-ft wide strip of the tremie seal.As per the BDM, the cofferdam sheet piling is typically located at 18 in. outside theBDM 7.03.04So per the BDM, the cofferdam sheet piling is typically located at 18 in. outside theBDM 7.03.04Note: It is recommended to evaluate the possibility of battered piles hitting the cofferdam sheet piles during
the pile driving operation. Based on the pile layout design, evaluate the space requirements and
increase the distance between the footing outline and the cofferdam sheet piles. Use the revised
dimensions to calculate the length of the tremie seal. This example uses the following dimensions:Expected sheet pile embedment depth from the top of
the tremie seal (an estimate from the Geotechnical
Services Section)SP embd := 15ftMinimum clearance between the edge of the heel and
ad sheet pileSP clrns_heel := 1.5ftSelected clearance between the edge of the toe
and sheet pileSP clrns_select_toe := $(SP_{enbd} + Pile_embd)$
 $Pile_batterSelected clearance between the edge of thetoe and sheet pileSP clrns_select_toe := Ceil(SP clrns_toe, 1ft) = 6 ftLength of tremie sealItremie := Bfooting + SP clrns_heel + SP clrns_select_toe = 18.5 ftWremie := $\gamma_{tremie} \cdot I_{tremie} = 11.008 \cdot I_{tremie} \cdot I_{$$

Consult the Geotechnical Services Section for the hydrostatic pressure head and the related information. $H_{water} := 10ft$

Hydrostatic pressure head to the bottom of the footing (from the Geotechnical Services Section)

Unit weight of water

Unit islet of two with

Co

As fo

No

 $\gamma_{\text{water}} \coloneqq 62.4 \frac{\text{lb}}{\text{ft}^3}$ 140 lb

Generally, tremie seals should be used on all structures when the pumping of water down below the bottom of footing is expected to be challenging.

A tremie seal shall be designed to resist the hydrostatic pressure at the bottom of the tremie by a combination of its weight and the bond between the cofferdam and piles. The allowable bond strength between the tremie and piles is 10 psi. The allowable bond strength between the tremie and the cofferdam is 5 psi. The allowable tension from the bending of the tremie seal is 30 psi.

The design of a tremie seal consists of determining a concrete thickness that will be sufficient, in conjunction with other sources of resistance, to resist the buoyant force at the bottom of the seal.

Hydrostatic pressure head is defined from the bottom of a tremie seal up to the ordinary **BDM 7.03.06B** water surface elevation.

Bending Stress Check

While checking the flexural stress in the tremie seal, assume that the 1-ft wide tremie seal strip is simply supported at both ends by the cofferdam.

Section modulus of the 1-ft wide strip

$$S_{\text{tremie}} := \frac{1}{6} \cdot h_{\text{tremie}}^2 = 3.01 \cdot \text{ft}^2$$

 $F_c := \frac{M_{tremie}}{S_{tremie}} = 29.034 \cdot psi$

p_{CoffBond} := 5psi

HP14x73

Check := if $(F_c < 30psi, "OK", "Not OK") = "OK"$

 $P_{CoffBond} := p_{CoffBond} 2 \cdot 1 \text{ft} \cdot h_{tremie} = 6.12 \cdot \text{kip}$

Check := if $(P_{resist} > P_{buoy}, "OK", "Not OK") = "OK"$

BDM 7.03.06A

Max. bending moment in the tremie seal

 $M_{\text{tremie}} := \frac{1}{8} \Big[\gamma_{\text{water}} \cdot \left(H_{\text{water}} + h_{\text{tremie}} \right) - \gamma_{\text{tremie}} \cdot h_{\text{tremie}} \Big] \cdot l_{\text{tremie}}^2 = 12.586 \cdot \frac{\text{kip} \cdot \text{ft}}{\text{ft}}$

Max. tensile stress in the tremie seal

Check if the max. tensile stress is less than 30 psi

Friction Check

Bond strength between tremie and cofferdam

Bond force between tremie and cofferdam

From Step 4.6, the selected pile section

Note: For H piles, surface area of a pile is defined using a rectangular shape for a conservative design (i.e. 2 times the sum of the flange width and the section depth).

Flange width	$b_f = 14.585 \cdot in$	
Section depth	$d_{pile} = 13.61 \cdot in$	
Bond strength between tremie and piles	p _{PileBond} := 10psi	BDM 7.03.06A

Bond force between tremie and piles when a 1-ft wide strip is considered

$$P_{PileBond} \coloneqq p_{PileBond} \cdot \left(\frac{N_{front}}{L_{footing}} + \frac{N_{back}}{L_{footing}}\right) \cdot 2 \cdot 1 \text{ft} \cdot \left(b_{f} + d_{pile}\right) \cdot h_{tremie} = 10.06 \cdot \text{kip}$$
Total uplift resistance (capacity)
$$P_{resist} \coloneqq W_{tremie} + P_{CoffBond} + P_{PileBond}$$

$$P_{resist} = 27.188 \cdot \text{kip}$$
Buoyant force (demand)
$$P_{buoy} \coloneqq \gamma_{water} \cdot 1 \text{ft} l_{tremie} \cdot \left(H_{water} + h_{tremie}\right) = 16.45 \cdot \text{kip}$$

Check if the total resistance force > the buoyant force

186



Note: Refer to MDOT Bridge Design Guides for additional bars, laps, embedment, and keyway dimensions. They are not shown in this drawing for clarity of the main reinforcement.